

Key observables for TMD extraction from the experimental point of view

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INFN Ferrara

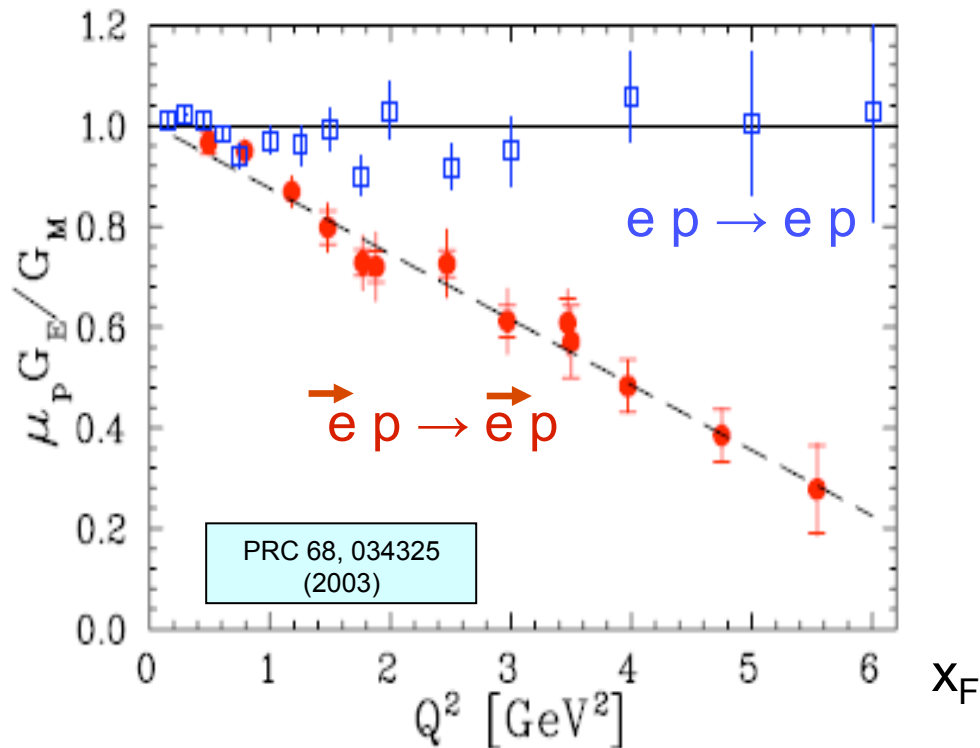
Structure of Nucleons and Nuclei

June 10, 2013 Como

The Spin Degree of Freedom

Spin degrees of freedom can explain otherwise surprising phenomena and bring new insights into nuclear matter structure

Fundamental: do not neglect it !!



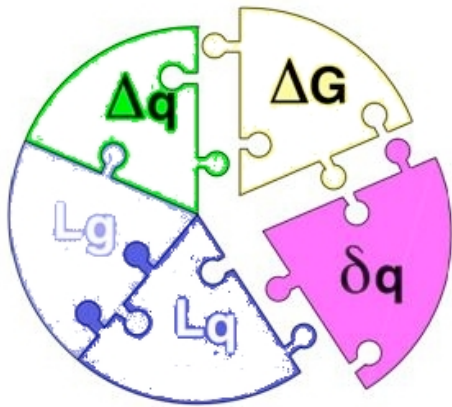
The Spin Degree of Freedom

In our exploration of the QCD micro-world

Fundamental: do not neglect spin !!

Two questions in Hadronic Physics
await explanation since too long

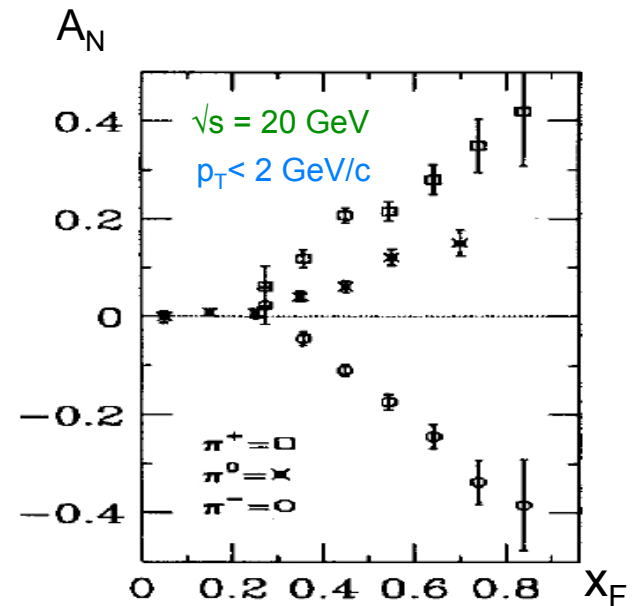
Proton Spin Budget



$$\frac{1}{2} = \frac{1}{2} \sum_f (q_f^+ - q_f^-) + L_q + \Delta G + L_g$$



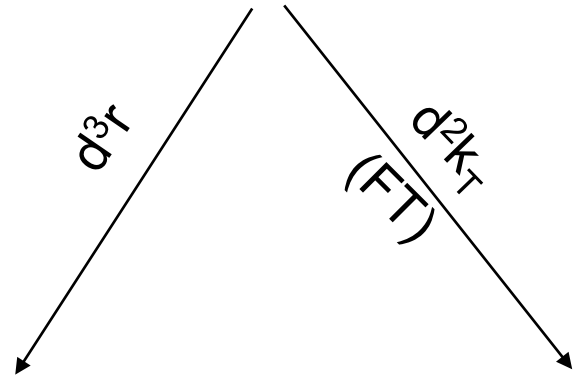
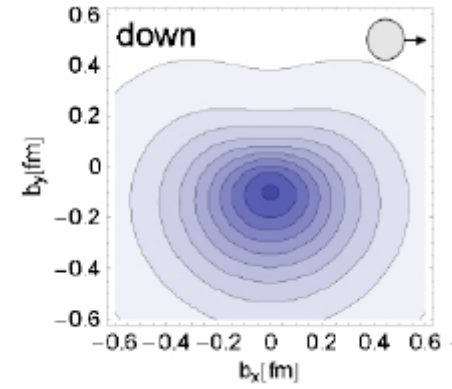
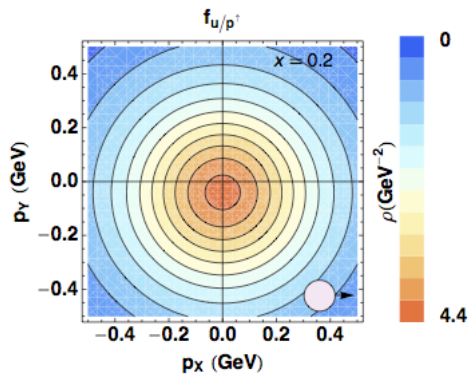
Single Spin Asymmetries



Quantum phase-space distributions of quarks

$W_p^q(x, k_T, r)$ "Mother" Wigner distributions

Probability to find a quark q in a nucleon P with a certain polarization in a position r & momentum k



TMD PDFs: $f_p^u(x, k_T), \dots$

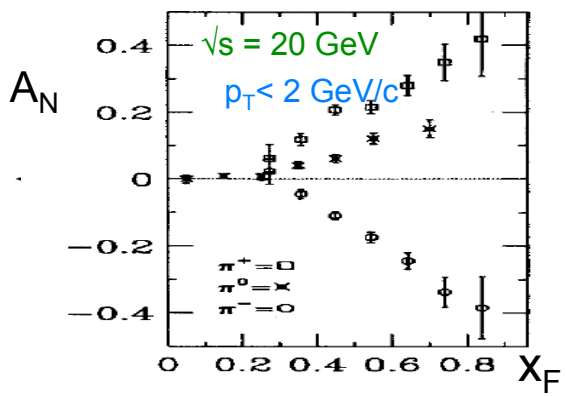
GPDs: $H_p^u(x, \xi, t), \dots$

Semi-inclusive measurements
Momentum transfer to quark
Direct info about momentum distribution

Exclusive Measurements
Momentum transfer to target
Direct info about spatial distribution

May explain SSA & Lam-Tung

May solve proton spin puzzle


















PDFs $f_p^u(x), \dots$

$$J_q = \frac{1}{2} \Delta \Sigma + L_q = \lim_{t \rightarrow 0} \int_{-1}^1 dx x [H(x, !, t) + E(x, !, t)]$$

Leading Twist TMDs

quark polarisation

		quark polarisation			
		N/q	U	L	T
nucleon polarisation	U		f_1  Number Density		h_1^\perp  -  Boer-Mulders
	L			g_1  -  Helicity	h_{1L}^\perp  -  Worm-gear
	T		f_{1T}^\perp  -  Sivers	g_{1T}^\perp  -  Worm-gear	h_1  -  Transversity h_{1T}^\perp  -  Pretzelosity

Number density and helicity:

Focusing here in transverse momentum dependence

Transversity:

Survives transverse momentum integration
(missing leading-twist collinear piece)

Differs from helicity due to relativistic effects and
no mix with gluons in the spin-1/2 nucleon

Off-diagonal elements:

Interference between wave functions with different angular momenta: contains information about parton orbital angular motion and spin-orbit effects
















Testing QCD at the amplitude level

T-odd elements:

- sign change between DY and SIDIS
 - universality of TMDs

Strict prediction from TMDs + QCD !

quark polarisation

		quark polarisation			
		N/q	U	L	T
nucleon polarisation	U		D_1  Unpolarized		H_1^\perp  -  Collins
	L			G_{1L}  - 	H_{1L}^\perp  - 
	T		D_{1T}^\perp  - 	G_{1T}  - 	H_1  -  H_{1T}^\perp  - 

First evidences

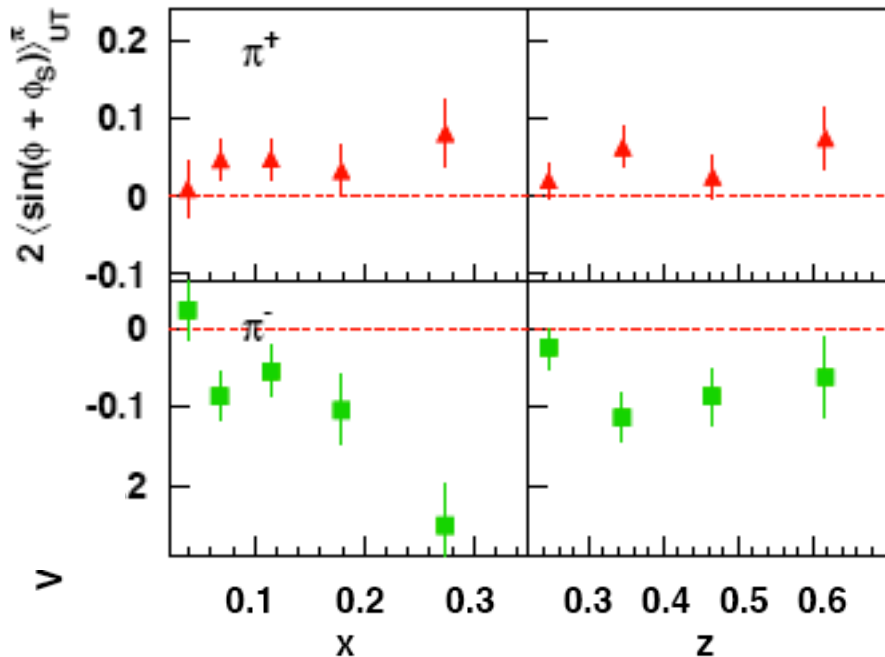
$$\sigma_{UT}^{\sin(\phi+\phi_S)} \propto h_1 \otimes H_1^\perp$$

SIDIS:
ep → e'hX

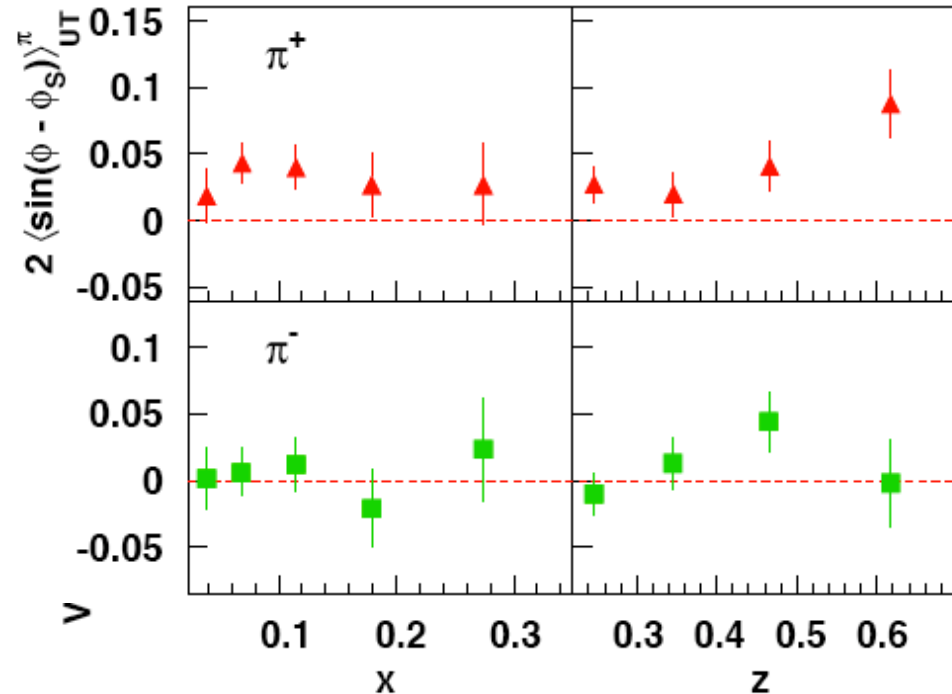
$$\sigma_{UT}^{\sin(\phi-\phi_S)} \propto f_{1T}^\perp \otimes D_1$$

2005: First evidence from HERMES measuring SIDIS on proton

A. Airapetian et al, Phys. Rev. Lett. 94 (2005) 012002

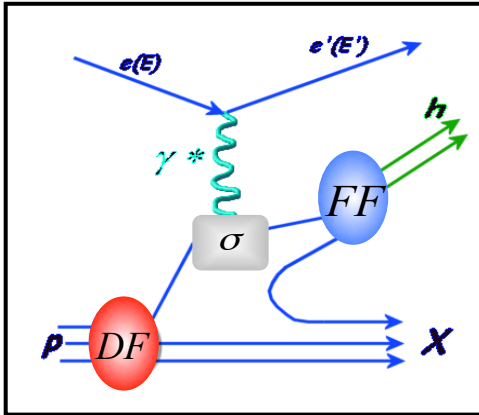


Non-zero transversity !!
Non-zero Collins function !!



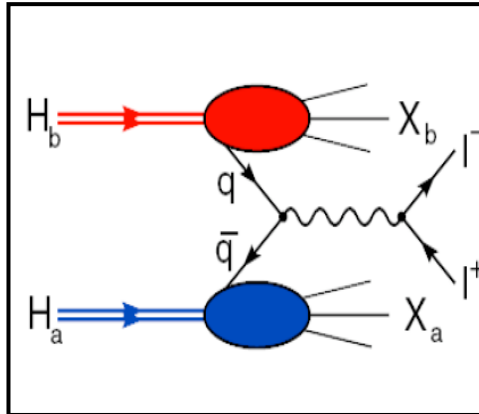
Non-zero Sivers function !!

Physics reactions



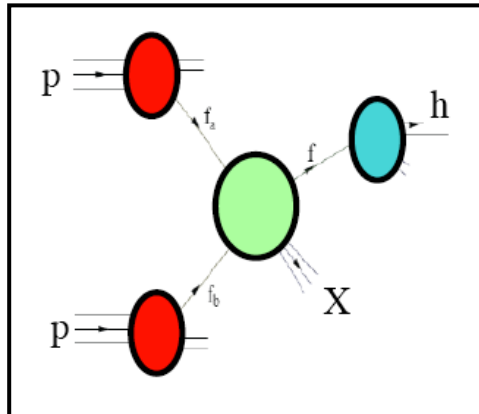
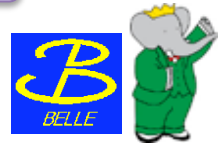
SIDIS: rich phenomenology, the most explored so far

$$\text{SIDIS} \quad \sigma^{ep \rightarrow ehX} = \sum_q \text{DF} \otimes \sigma^{eq \rightarrow eq} \otimes \text{FF}$$



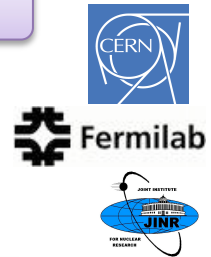
e⁺e⁻: B-factories as powerful fragmentation laboratories

$$e^+e^- \quad \sigma^{ee \rightarrow hhX} = \sum_q \sigma^{qq \rightarrow ee} \otimes \text{FF} \otimes \text{FF}$$



DY: challenging for experiments (only unpolarized so far)

$$\text{DY} \quad \sigma^{pp \rightarrow eeX} = \sum_q \text{DF} \otimes \text{DF} \otimes \sigma^{qq \rightarrow ee}$$


















Hadron reactions: challenging for theory (ISI + FSI)

$$pp \quad \sigma^{pp \rightarrow hX} = \sum_q \text{DF} \otimes \text{DF} \otimes \sigma^{qq \rightarrow qq} \otimes \text{FF}$$

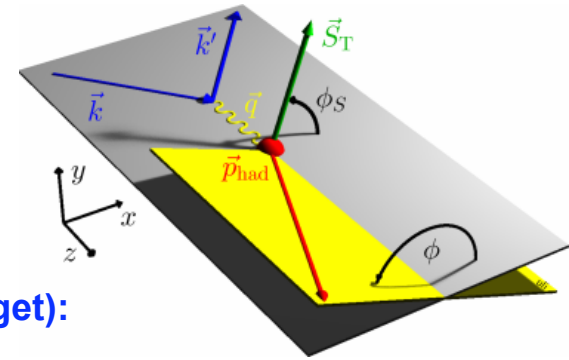


The SIDIS case

quark polarisation

N/q	U	L	T
U	f_1  Number Density		h_1^\perp  -  Boer-Mulders
L		g_1  -  Helicity	h_{1L}^\perp  -  Worm-gear
T	f_{1T}^\perp  -  Sivers	g_{1T}^\perp  -  Worm-gear	h_1  -  Transversity h_{1T}^\perp  -  Pretzelosity

SIDIS cross section
(transversely polarized target):



$$\frac{d^6\sigma}{dx dy dz d\phi_S d\phi dP_{h\perp}^2} \stackrel{\text{Leading}}{\propto} \stackrel{\text{Twist}}{S_T} \left\{ \sin(\phi - \phi_S) F_{UT,T}^{\sin(\phi - \phi_S)} \right\}$$

$$+ S_T \left\{ \varepsilon \sin(\phi + \phi_S) F_{UT}^{\sin(\phi + \phi_S)} + \varepsilon \sin(3\phi - \phi_S) F_{UT}^{\sin(3\phi - \phi_S)} \right\}$$

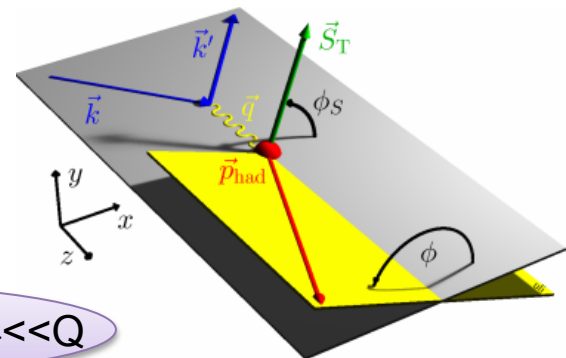
$$+ S_T \lambda_e \left\{ \sqrt{1 - \varepsilon^2} \cos(\phi - \phi_S) F_{LT}^{\cos(\phi - \phi_S)} \right\} + \dots$$

The SIDIS case

quark polarisation

N/q	U	L	T
U	f_1 Number Density		h_1^\perp - Boer-Mulders
L		g_1 - Helicity	h_{1L}^\perp - Worm-gear
T	f_{1T}^\perp - Sivers	g_{1T}^\perp - Worm-gear	h_1 - Transversity h_{1T}^\perp - Pretzelosity

SIDIS cross section
(transversely pol. target):



TMD factorization for $P_T \ll Q$

$$f \otimes D = \int_q e_q^2 d^2 p_T d^2 k_T \dots w(k_T, p_T) f^q(x, k_T^2) D^q(z, p_T^2)$$

Involved phenomenology due to the convolution over transverse momentum

$$h_1 \otimes H_1^\perp$$

$$\frac{d^6 \sigma}{dx dy dz d\phi_S d\phi dP_{h\perp}^2} \stackrel{\text{Leading}}{\propto} S_T \left\{ \sin(\phi - \phi_S) F_{UT,T}^{\sin(\phi - \phi_S)} \right\} \stackrel{\text{Twist}}{}$$

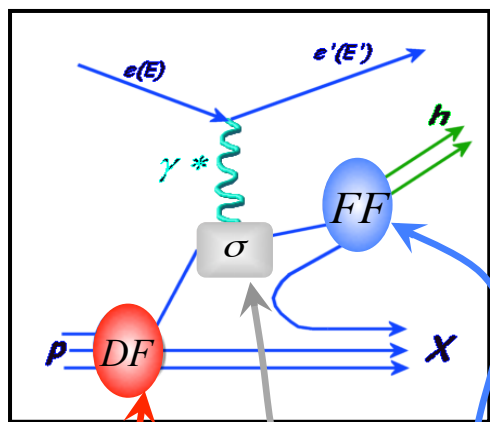
$$f_{1T}^\perp \otimes D_1$$

$$h_{1T}^\perp \otimes H_1^\perp$$

$$+ S_T \left\{ \varepsilon \sin(\phi + \phi_S) F_{UT}^{\sin(\phi + \phi_S)} + \varepsilon \sin(3\phi - \phi_S) F_{UT}^{\sin(3\phi - \phi_S)} \right\}$$

$$g_{1T}^\perp \otimes D_1$$

$$+ S_T \lambda_e \left\{ \sqrt{1 - \varepsilon^2} \cos(\phi - \phi_S) F_{LT}^{\cos(\phi - \phi_S)} \right\} + \dots$$


















$$\sigma^{ep \rightarrow ehX} = \sum_q DF \otimes \sigma^{eq \rightarrow eq} \otimes FF$$

Parton Number Density



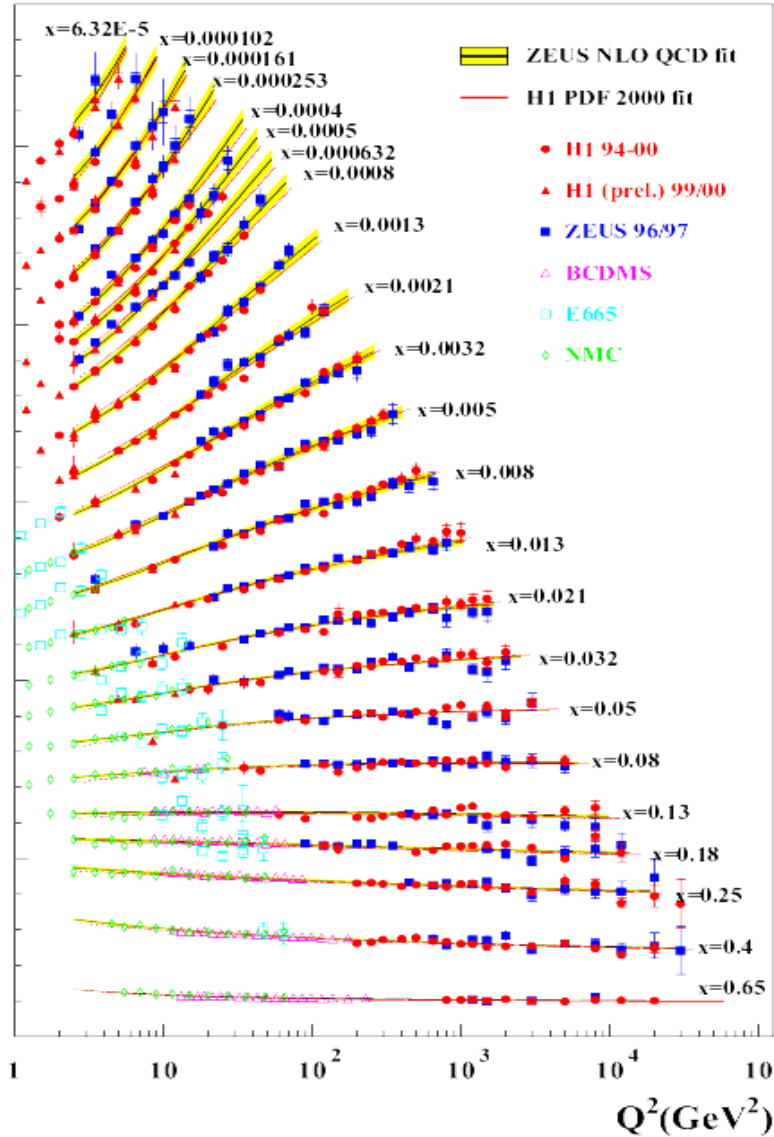
NUMBER DENSITY

	N/q	U	L	T
nucleon polarisation	U	f_1  <i>Number Density</i>		h_1^\perp  -  <i>Boer-Mulders</i>
	L		g_1  -  <i>Helicity</i>	h_{1L}^\perp  -  <i>Worm-gear</i>
	T	f_{1T}^\perp  -  <i>Sivers</i>	g_{1T}^\perp  -  <i>Worm-gear</i>	h_1  -  <i>Transversity</i> h_{1T}^\perp  -  <i>Pretzelosity</i>

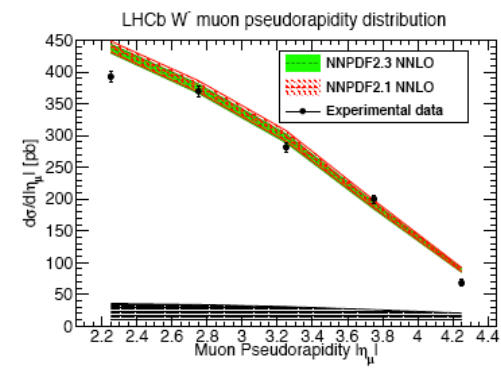
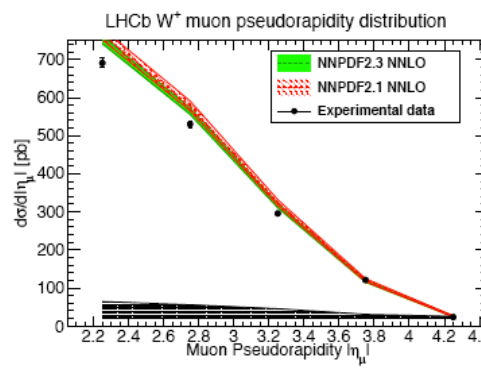
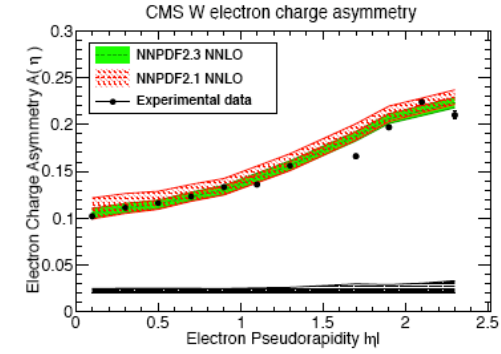
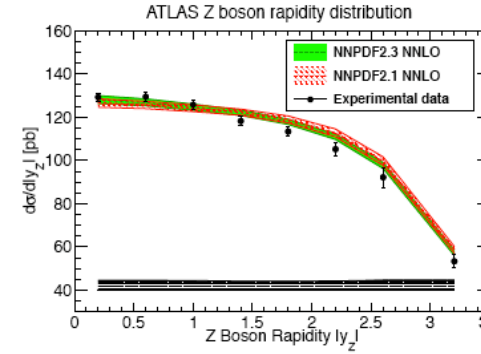
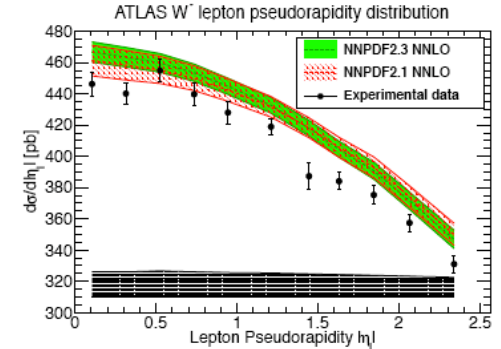
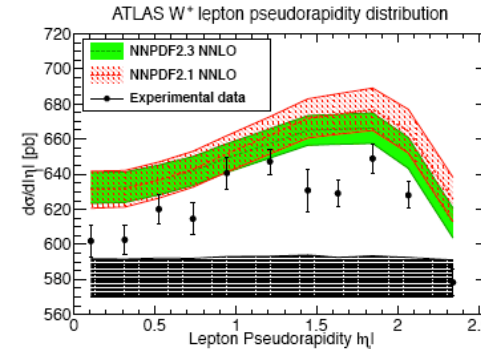
(THE BASELINE)

Parton Number Density

HERA F_2

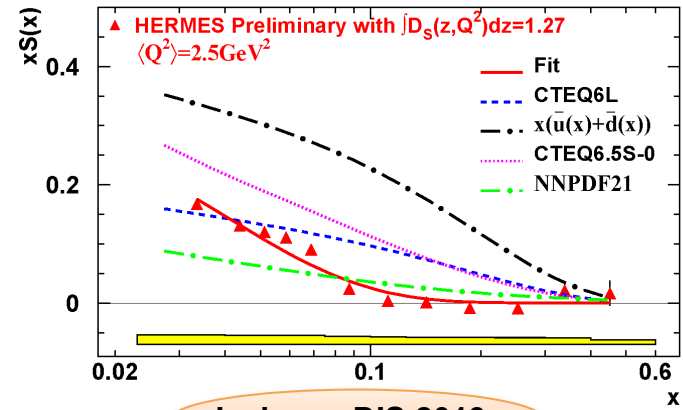
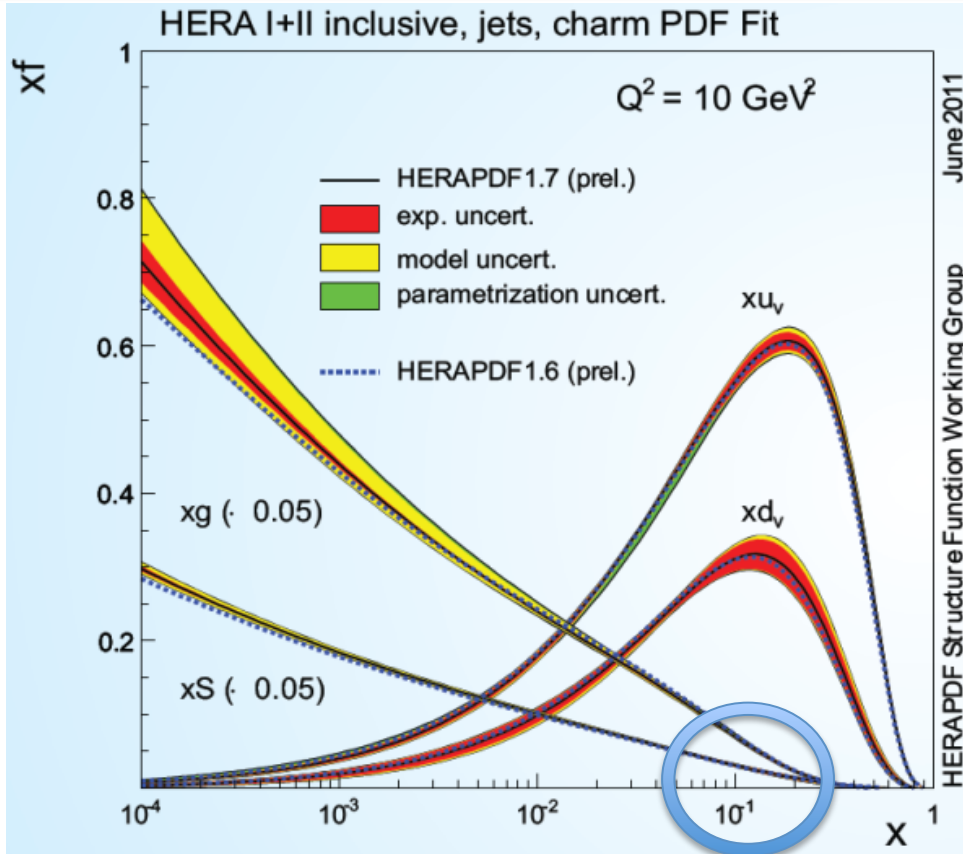


LHC gauge boson production

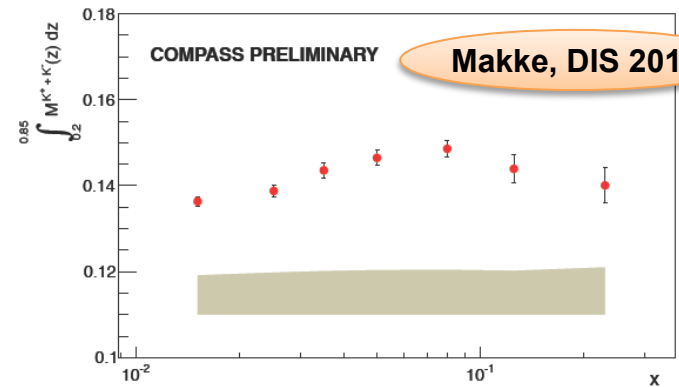


NNPDF: arXiv:1207.1303

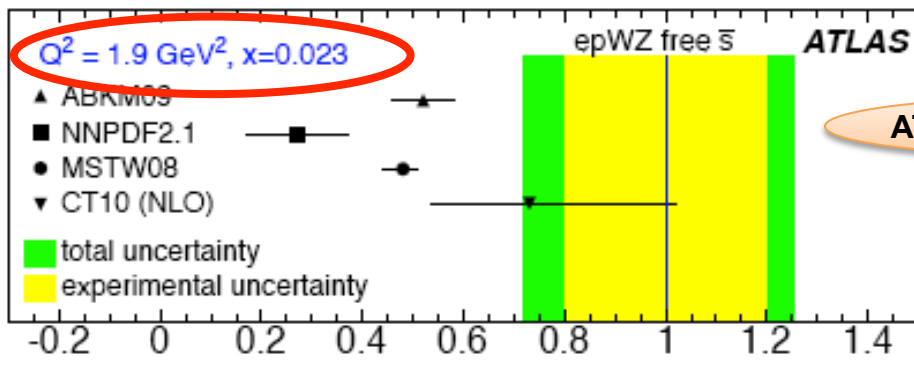
Parton Number Density



Jackson, DIS 2013

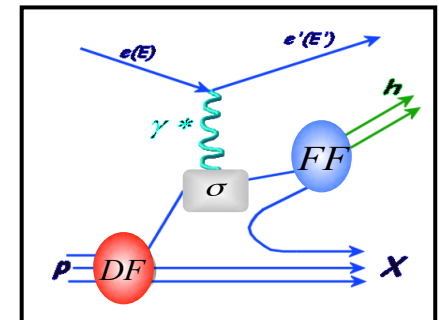


Makke, DIS 2013

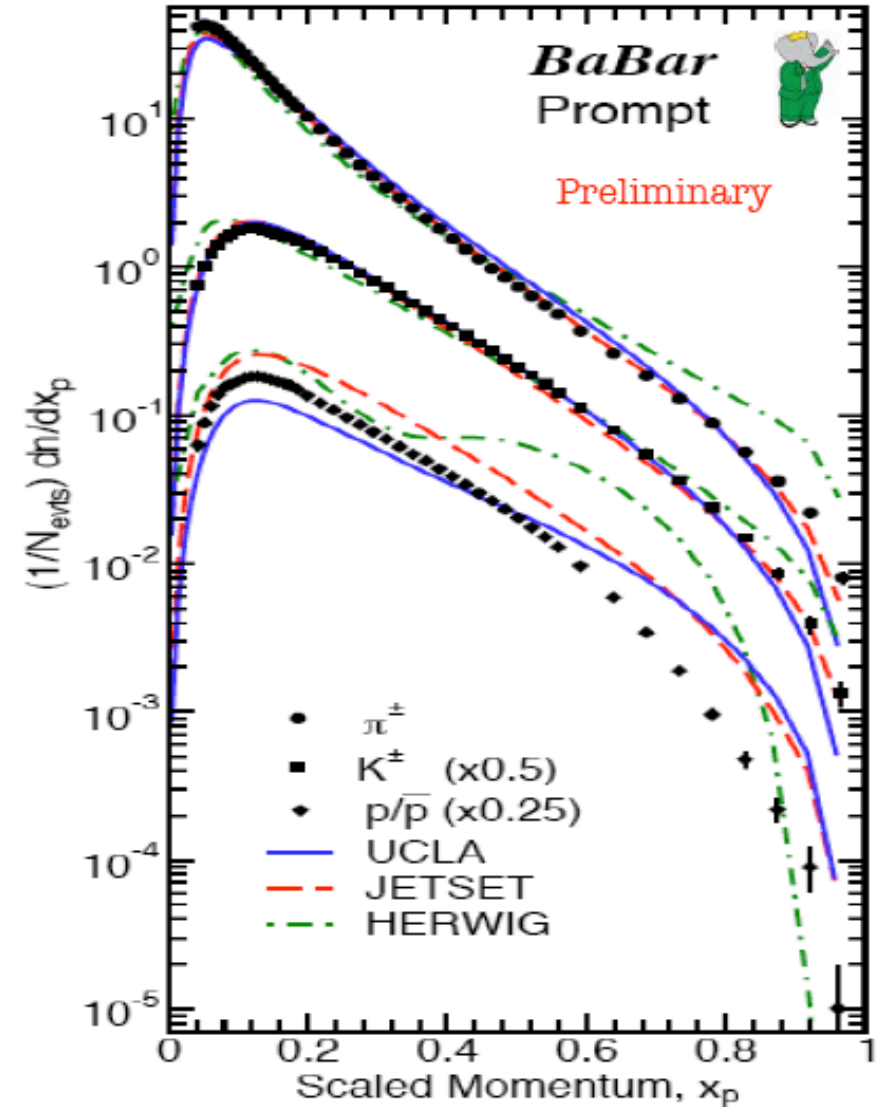
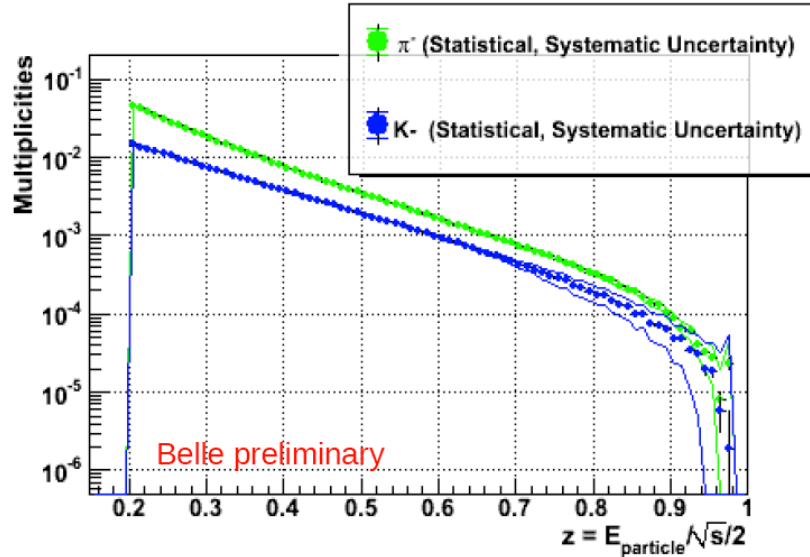


ATLAS: arXiv:1206.4051

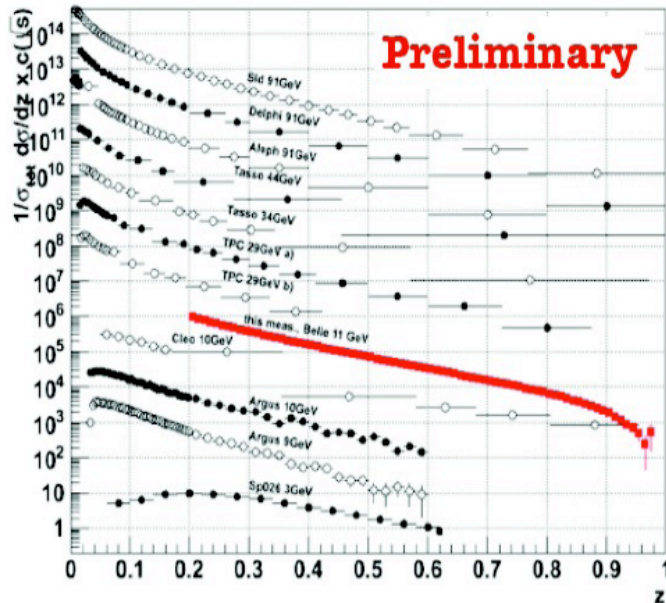
$$r_s = 0.5(s + \bar{s})/\bar{d}$$



Fragmentation Functions @ B-factories



world data (sel.) for $e^+e^- \rightarrow \pi^\pm + X$ production



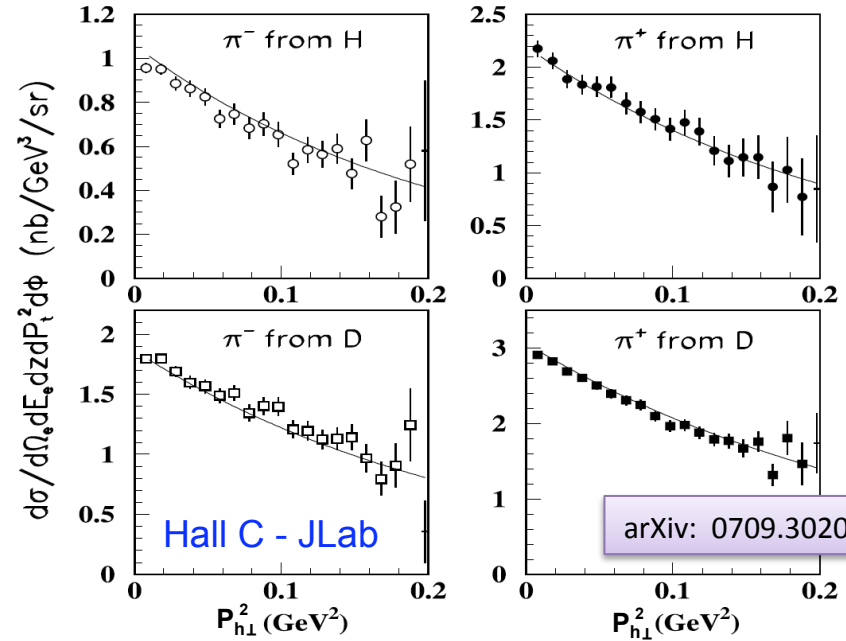
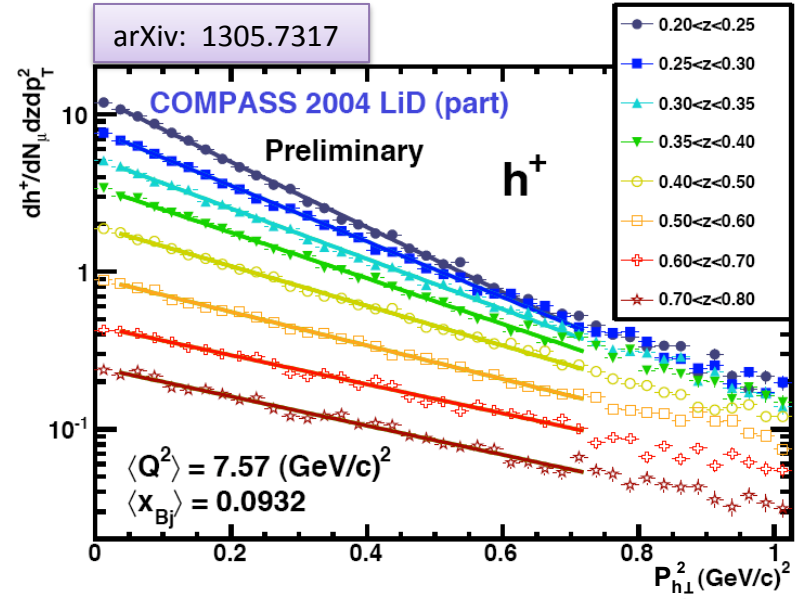
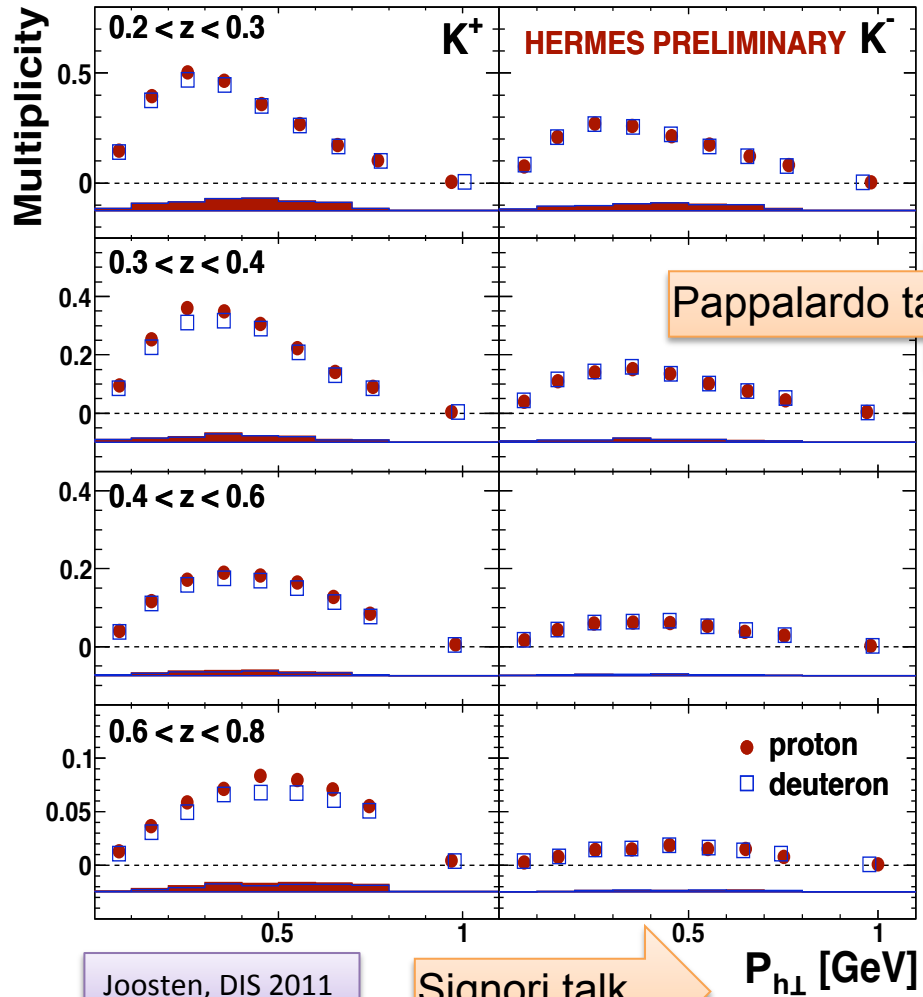
Vossen talk

The $P_{h\perp}$ -unintegrated multiplicities

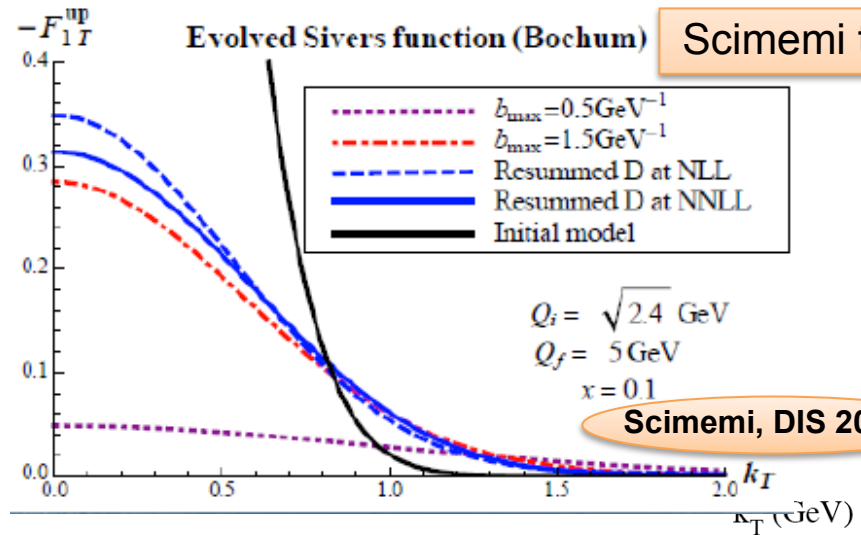
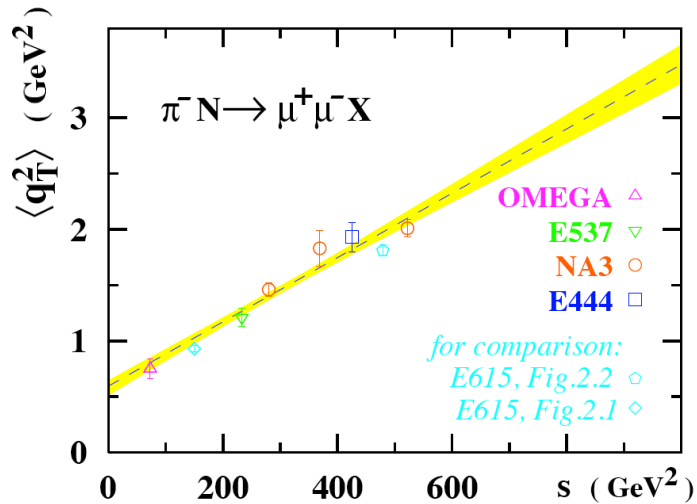
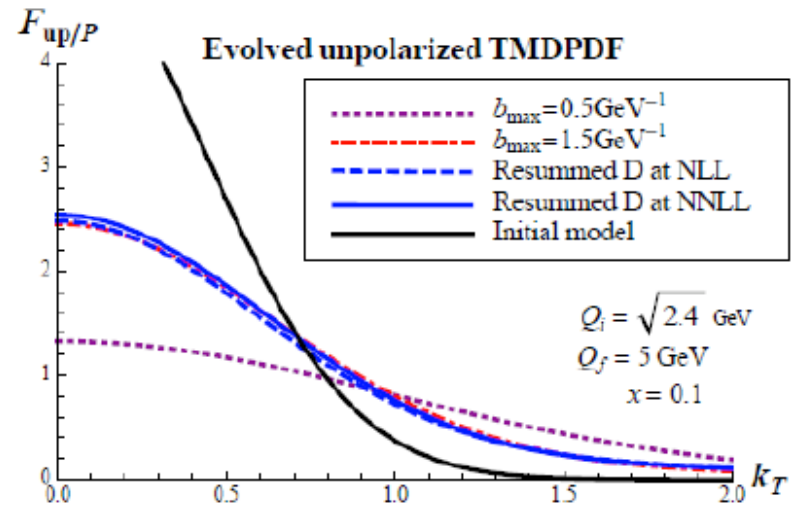
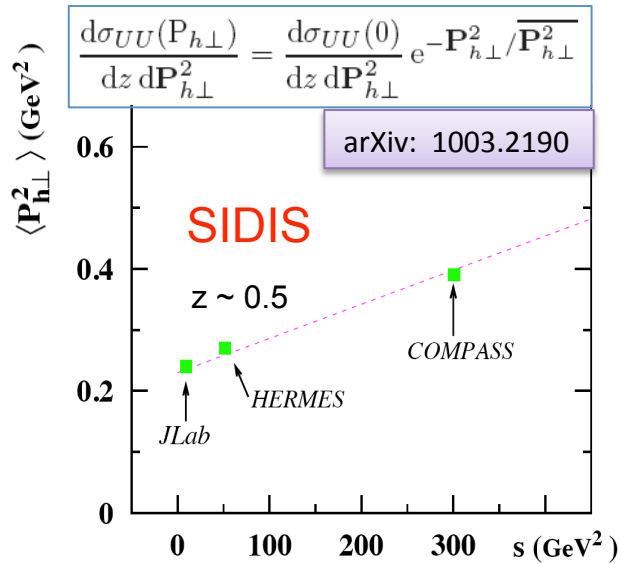
$$f_1 \otimes D_1$$

Disentanglement of z and $P_{h\perp}$: access to the transverse intrinsic quark k_T and fragmentation p_T ,

i.e. from gaussian ansatz $\langle P_{h\perp}^2 \rangle = z^2 \langle k_T^2 \rangle + \langle p_T^2 \rangle$



Indication of a k_T and p_T broadening with c.m. energy:
TMD Q^2 evolution


















Scimemi talk

Scimemi, DIS 2013

Parton Polarization

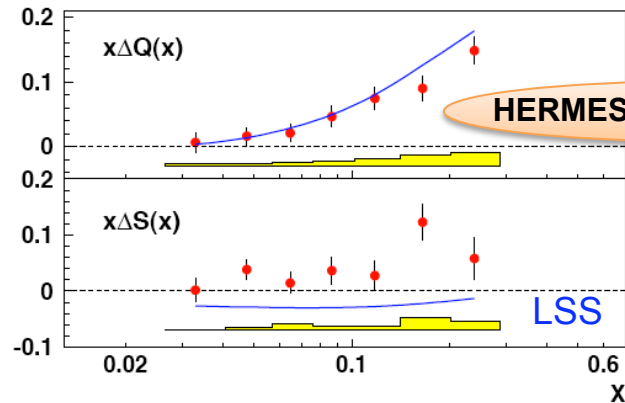
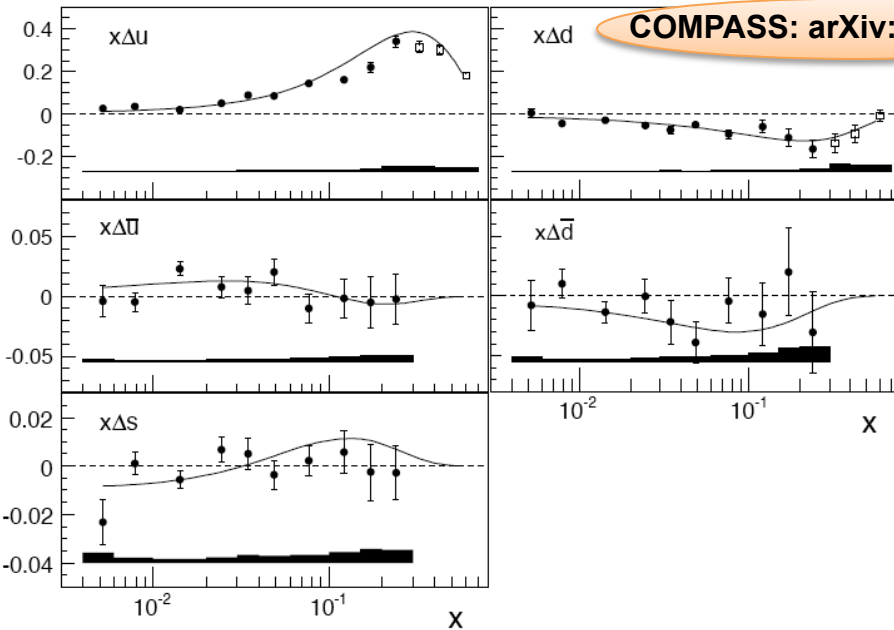


HELICITY

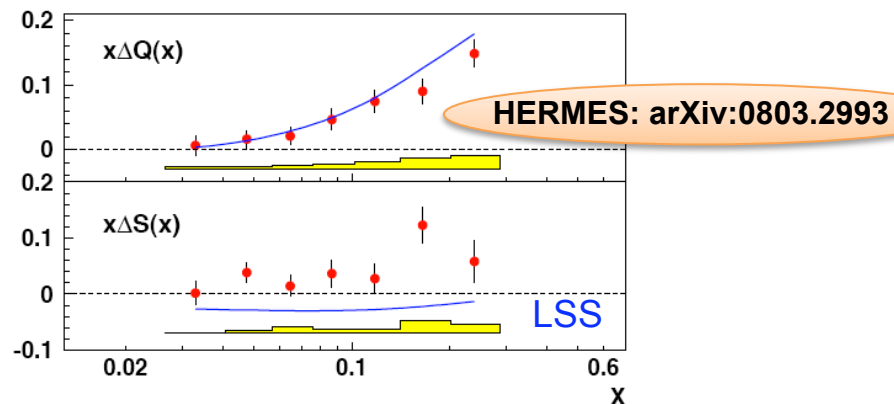
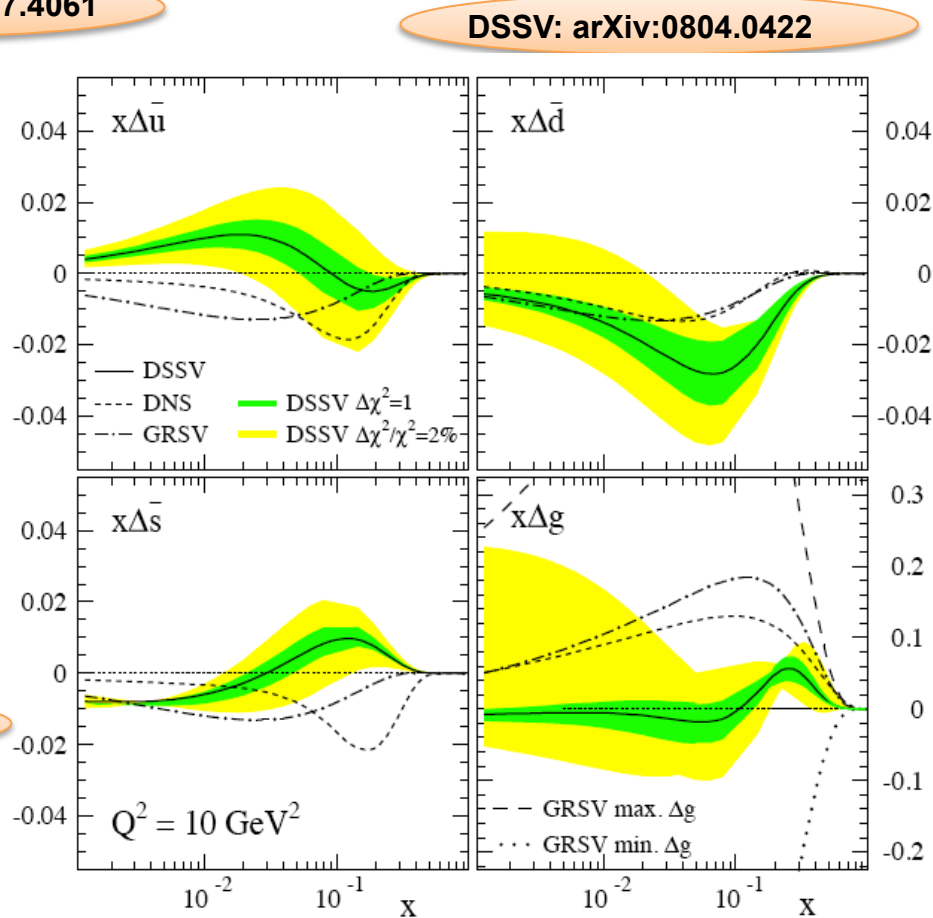
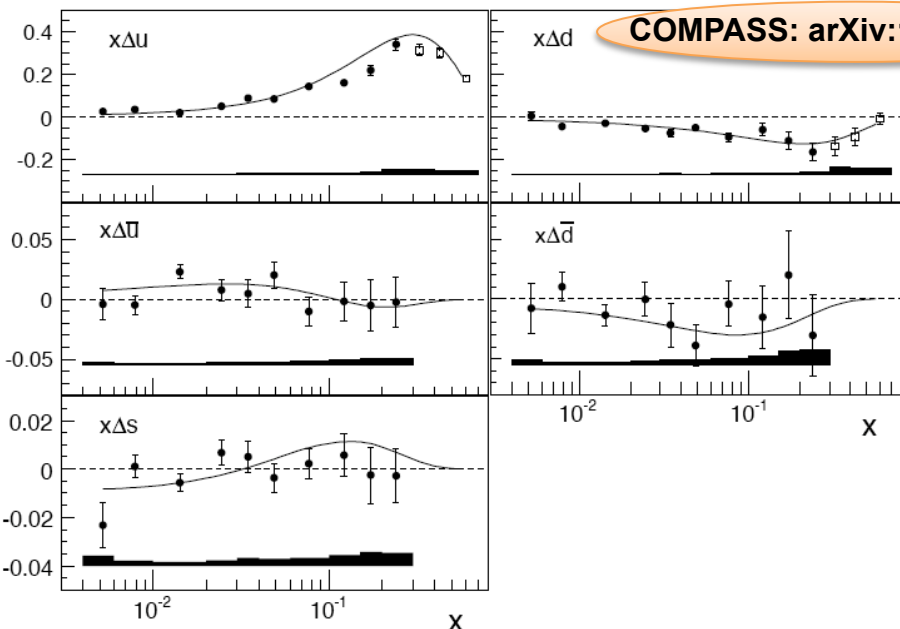
	N/q	U	L	T
nucleon polarisation	U	f_1  <i>Number Density</i>		h_1^\perp  -  <i>Boer-Mulders</i>
	L		g_1  -  <i>Helicity</i>	h_{1L}^\perp  -  <i>Worm-gear</i>
	T	f_{1T}^\perp  -  <i>Sivers</i>	g_{1T}^\perp  -  <i>Worm-gear</i>	h_1  -  <i>Transversity</i> h_{1T}^\perp  -  <i>Pretzelosity</i>

(THE FIRST PUZZLE)

Parton Helicity from SIDIS



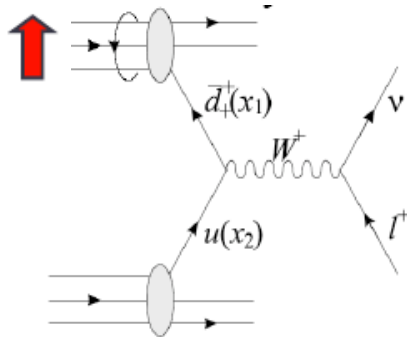
Parton Helicity from SIDIS



NNPDF: arXiv:1206.0201

	NNPDFpol1.0	DSSV08 [5]	BB10 [2]	LSS10 [4]	AAC08 [3]
$\Delta\Sigma(Q^2)$	0.31 ± 0.10	0.25 ± 0.02	0.19 ± 0.08	0.21 ± 0.03	0.24 ± 0.07
$\Delta g(Q^2)$	-0.2 ± 1.4	-0.10 ± 0.16	0.46 ± 0.43	0.32 ± 0.19	0.63 ± 0.81

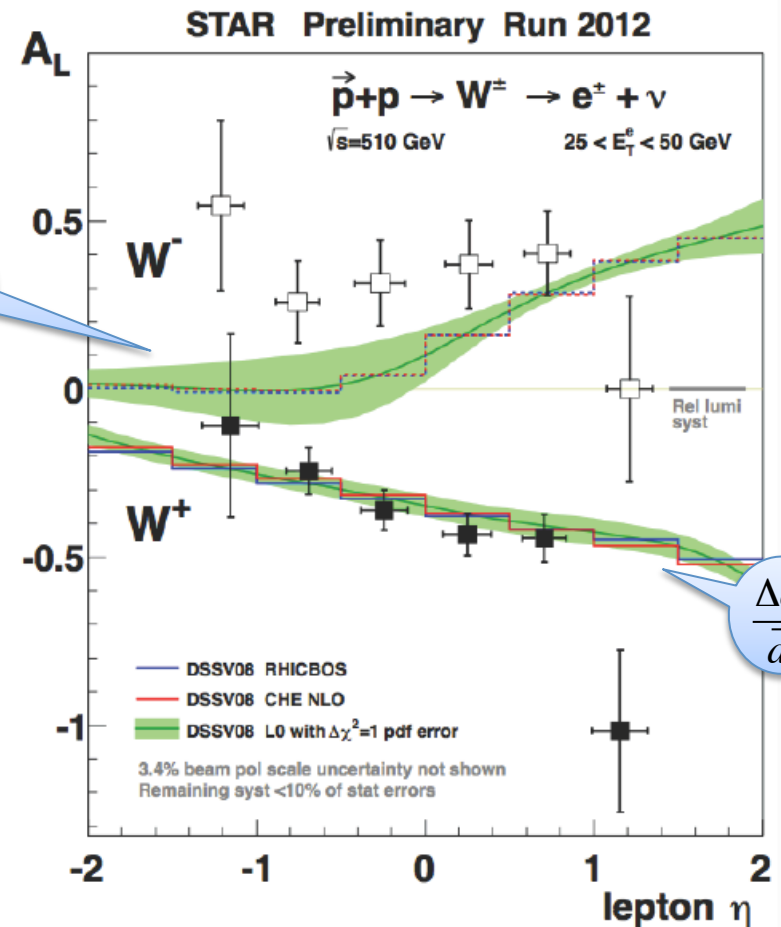
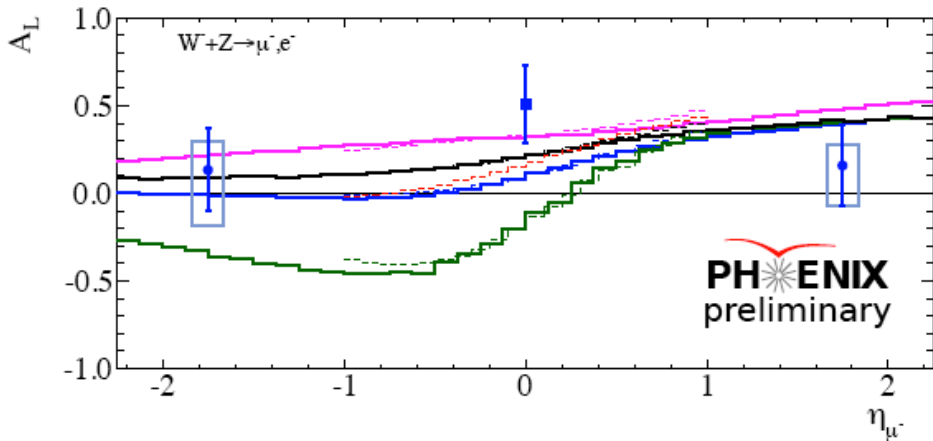
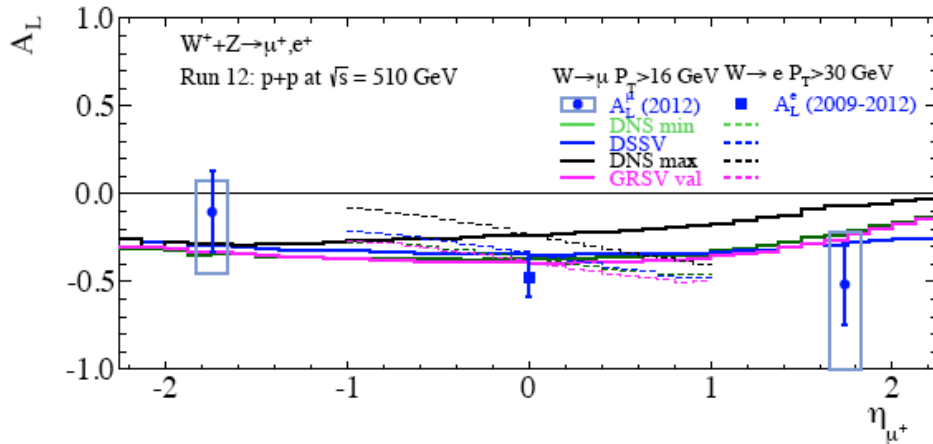
Parton Helicity from W



Charge + Rapidity



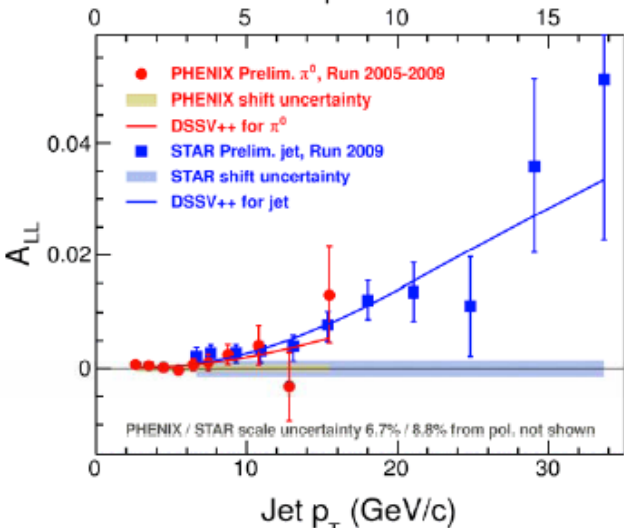
Flavor



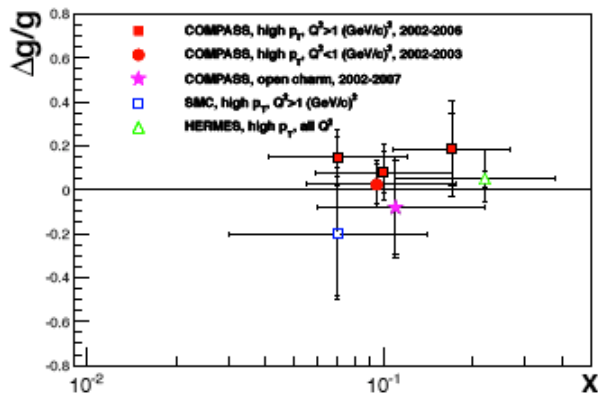
Gluon Helicity

pp inclusive hadron

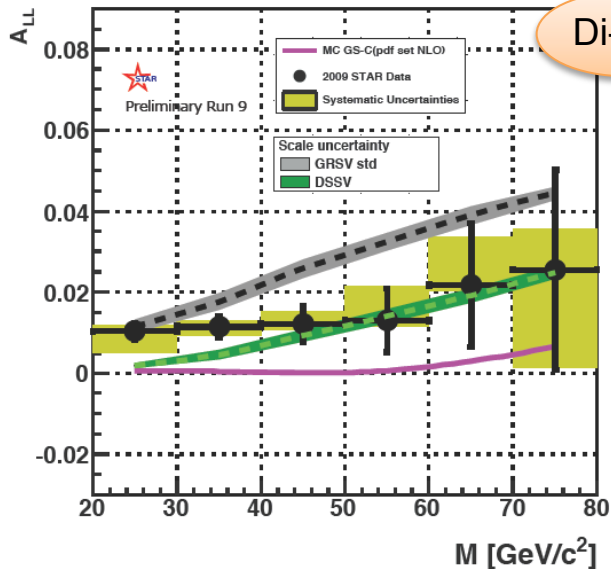
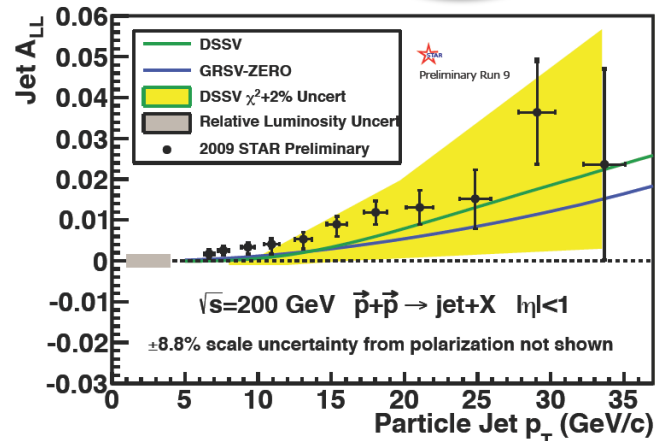
$$x \sim \frac{2p_T}{\sqrt{s}}$$



SIDIS high- p_T & open charm



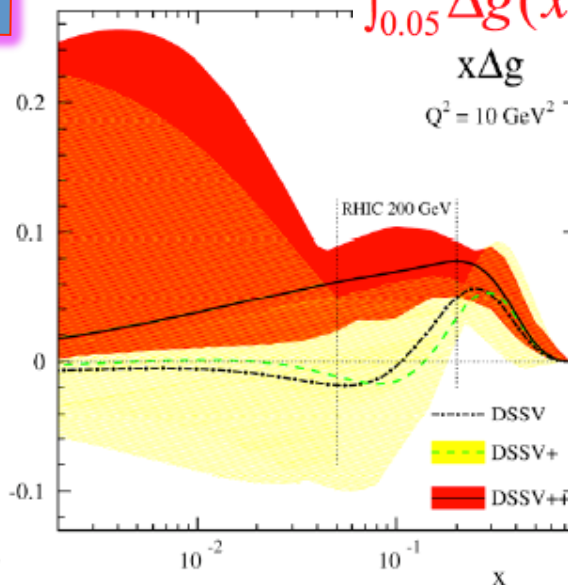
Inclusive Jet in pp



Di-Jet



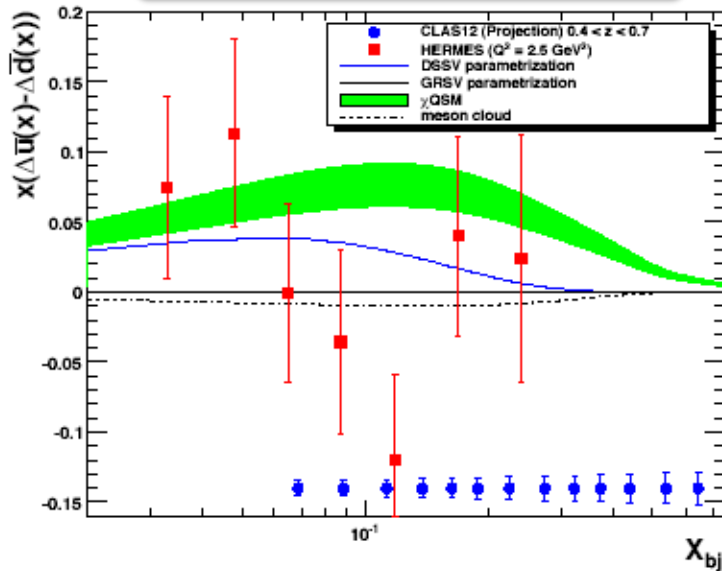
$$\int_{0.05}^{0.2} \Delta g(x) dx = 0.1 \pm_{0.07}^{0.06}$$



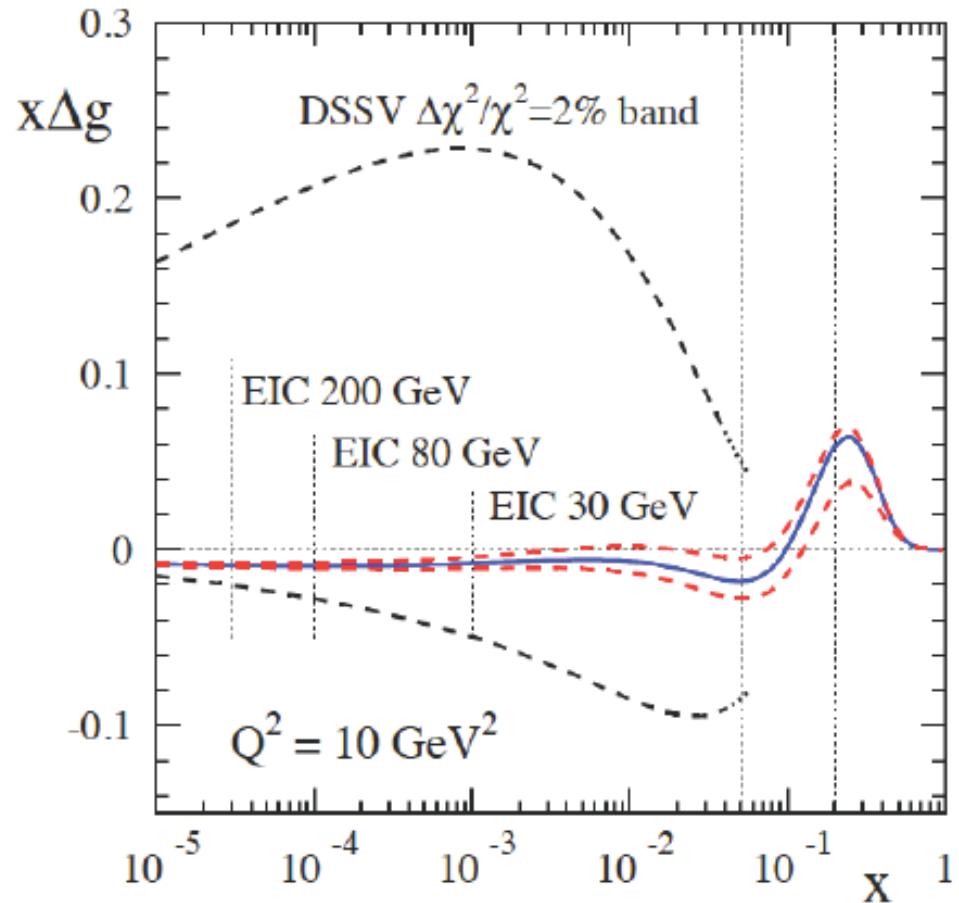
Zhang talk

Parton Helicity

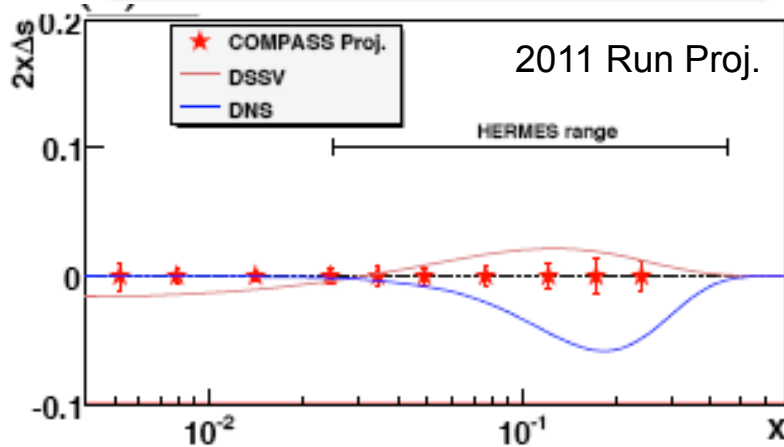
Valence Δq @ CLAS12



Sea Δq and ΔG @ EIC



Middle-sea Δq @ COMPASS

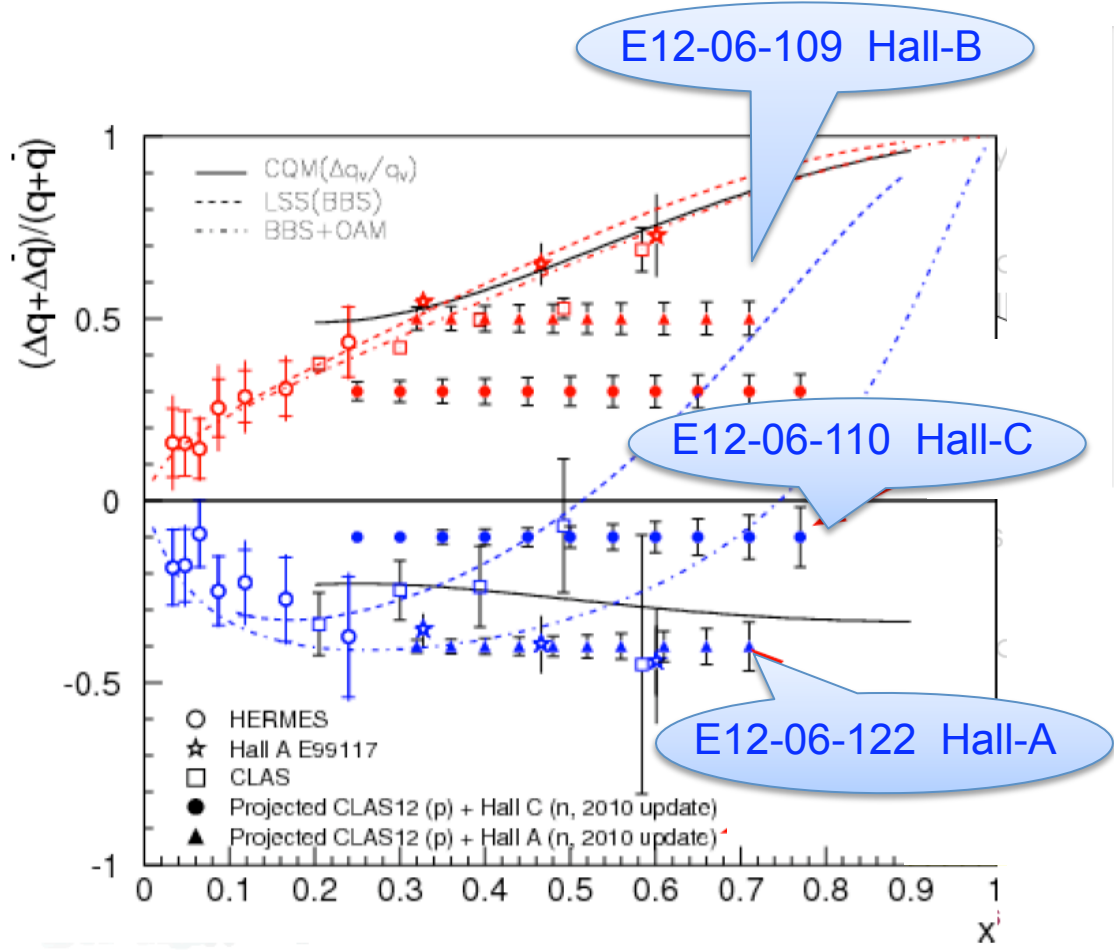


Quark Helicity

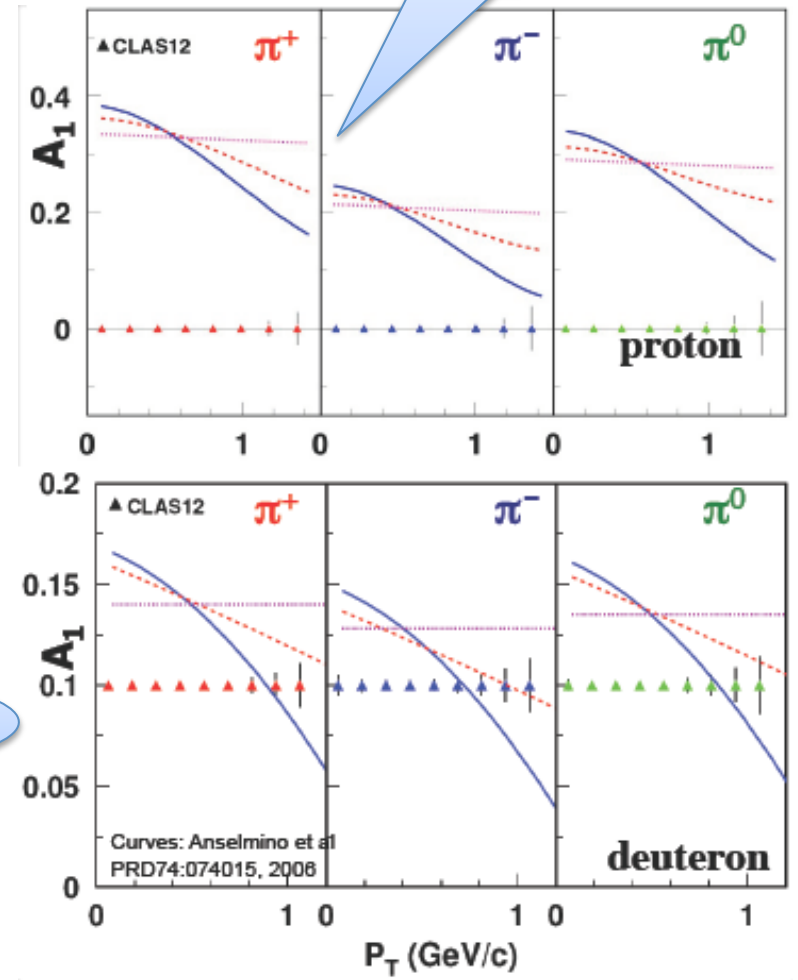
Quark helicity at high-x is sensitive to orbital angular momentum.

Cisbani talk

Transverse momentum dependence of quark helicity vs number density


















E12-07-104 Hall-B

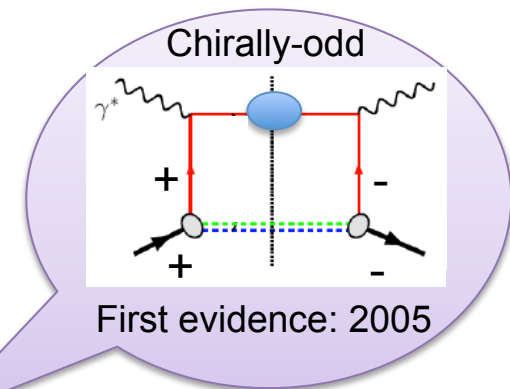


Point Transverse



TRANSVERSITY

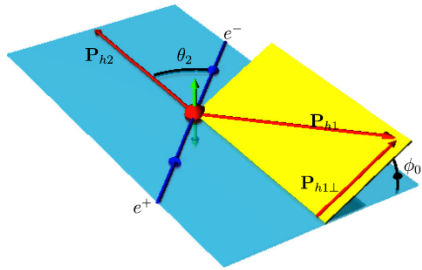
	N/q	U	L	T
nucleon polarisation	U	f_1  Number Density		h_1^\perp  -  Boer-Mulders
	L		g_1  -  Helicity	h_{1L}^\perp  -  Worm-gear
	T	f_{1T}^\perp  -  Sivers	g_{1T}^\perp  -  Worm-gear	h_1^\perp  -  Transversity h_{1T}^\perp  -  Pretzelosity



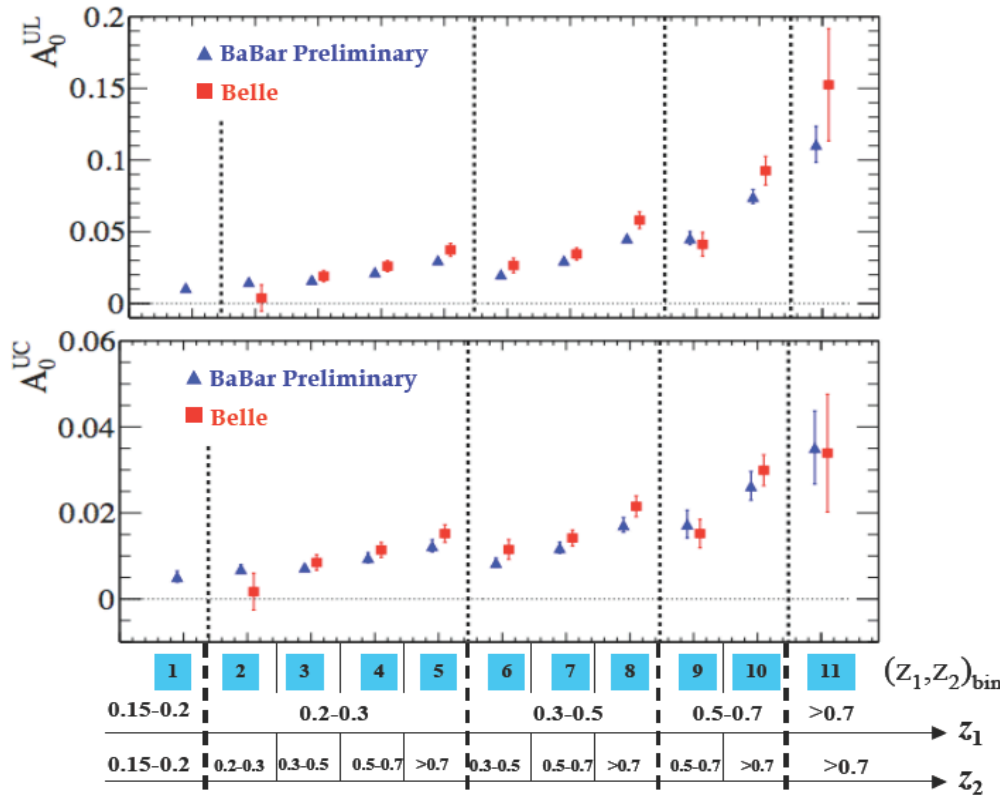
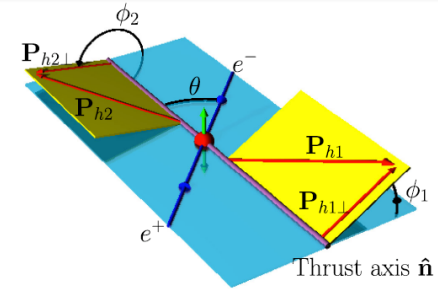
(THE COLLINEAR MISSING PIECE)

Fragmentation @ e+e- Colliders

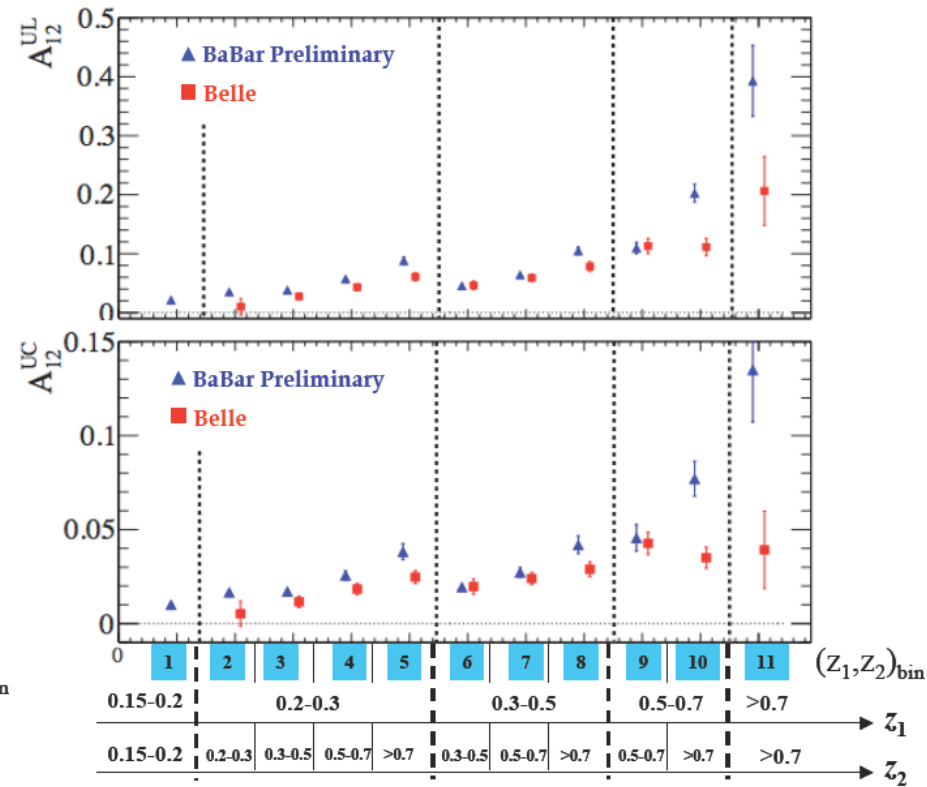
$$H_1^\perp \otimes H_1^\perp$$



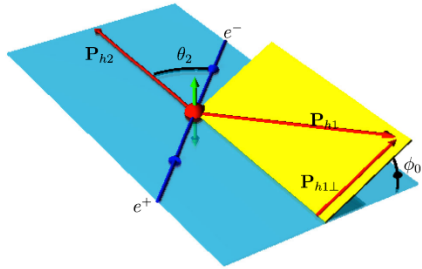
COLLINS SIGNALS



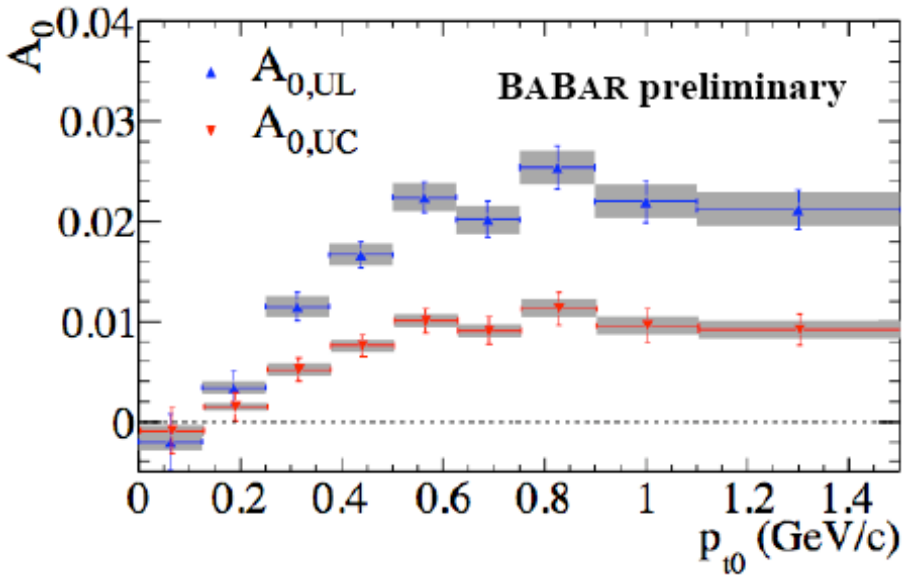
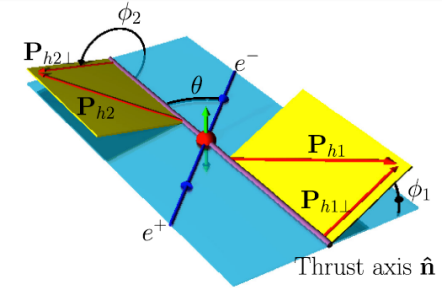
Garzia, DIS 2013



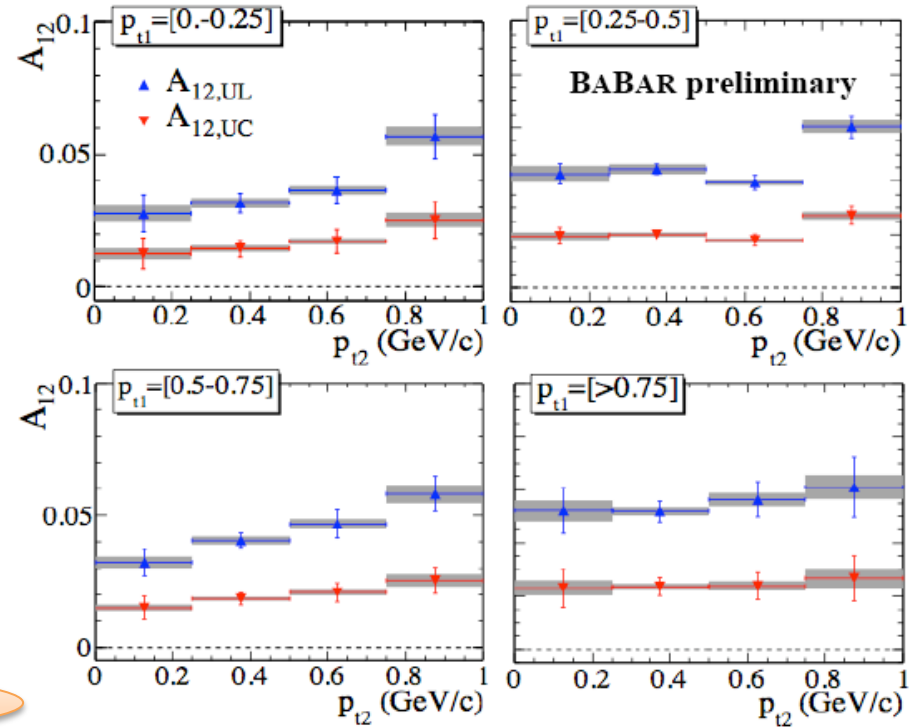
BELLE, PRD 86 (2012) 039905(E)



COLLINS SIGNALS



Garzia, DIS 2013



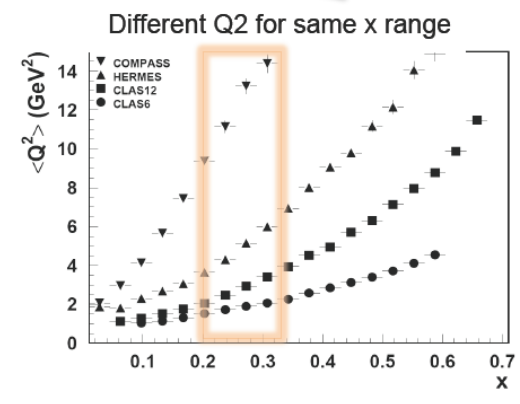
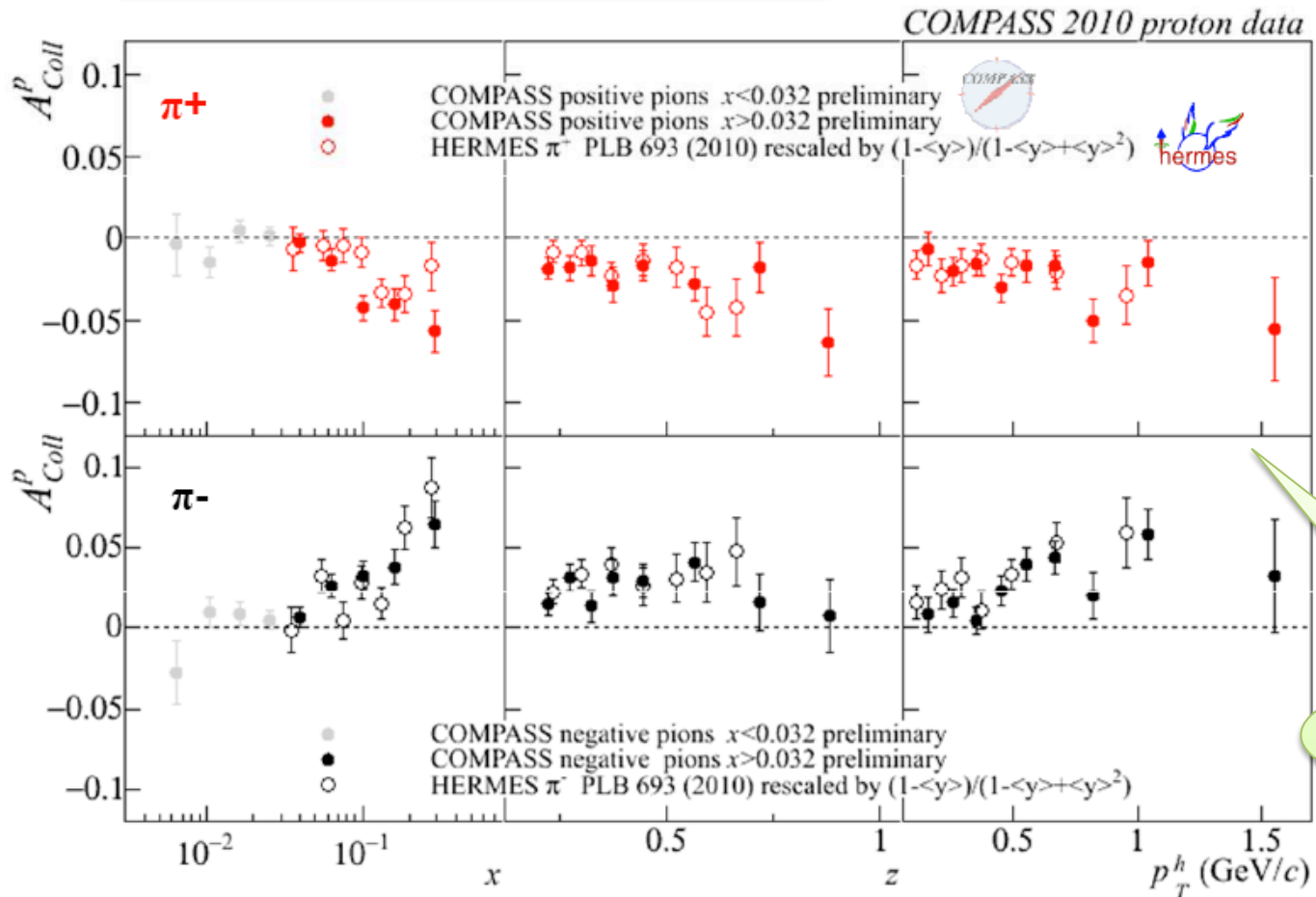
The Collins SIDIS amplitude

$$h_1 \otimes H_1^\perp$$

CLEAR NON ZERO SIGNALS !

$$A_{UT}^{\sin(\phi + \phi_S)} \propto \frac{\sum_q e_q^2 h_1^q(x, p_T^2) \otimes_\omega H_1^{q,\perp}(z, k_T^2)}{\sum_q e_q^2 f_1^q(x, p_T^2) \otimes D_1^q(z, k_T^2)}$$

Consistent results at different Q^2
 → No higher twists
 → No strong evolution



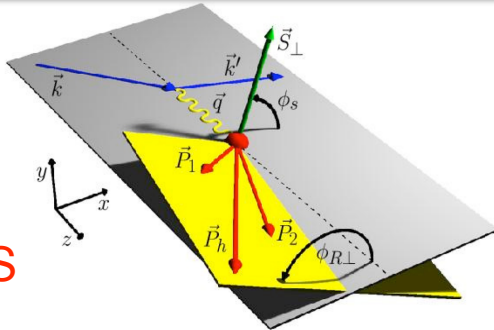
Bressan talk →

Opposite sign for pions reveals Collins features

Two hadron asymmetries

$$h_1 \otimes H_1^\Delta$$

SIDIS



COMPASS, arXiv: 1202.6150

HERMES, arXiv: 0803.2367

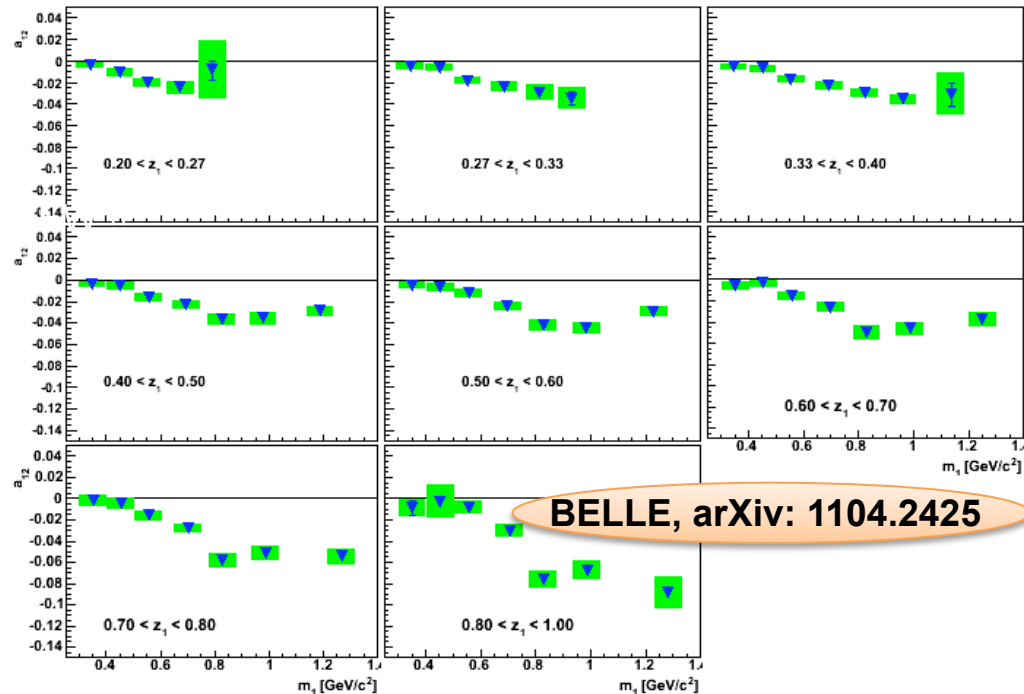
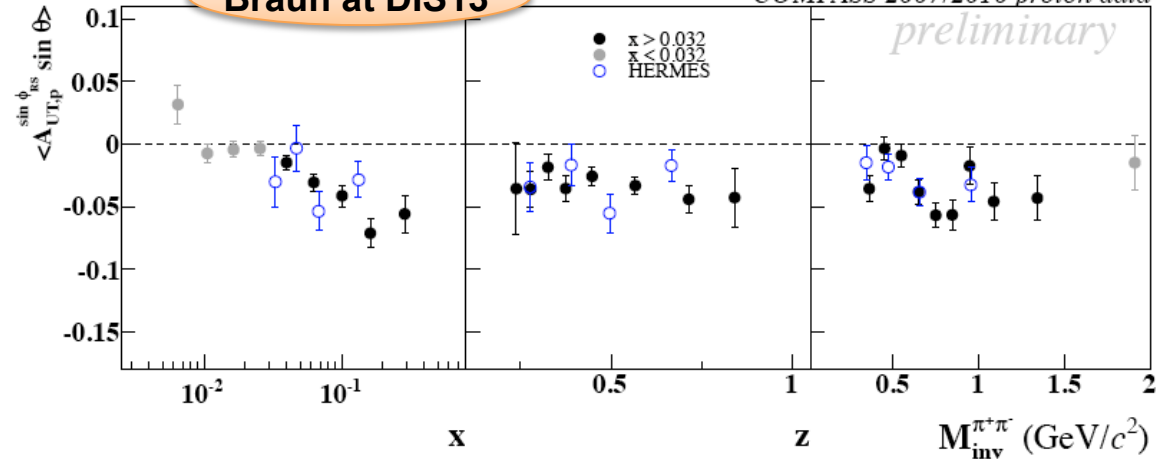
$$A_{UT}^{\sin(\phi_R + \phi_S) \sin \theta} \propto \frac{\sum_q e_q^2 h_1(x, Q^2) H_1^\Delta(z, M_h^2, Q^2)}{\sum_q e_q^2 f_1(x, Q^2) D_1^\Delta(z, M_h^2, Q^2)}$$

- Survives P_h integration
- Collinear factorization (simple product)
- DGLAP volution
- Universality
- Issue: unknown pp-terms in PW expansion

Belle

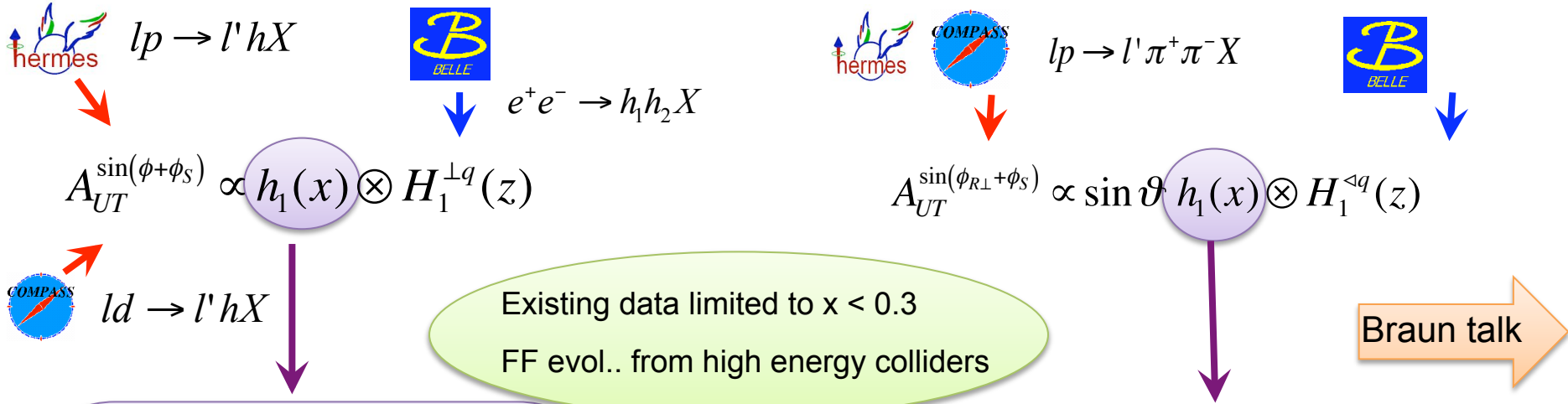
Braun at DIS13

COMPASS 2007/2010 proton data

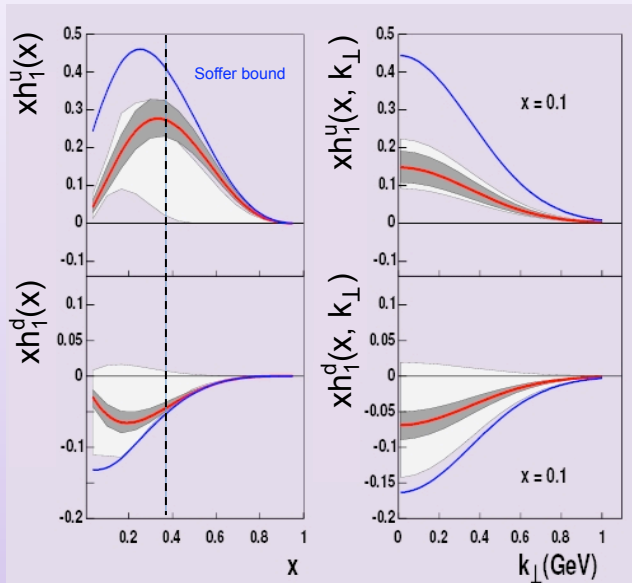


BELLE, arXiv: 1104.2425

Transversality Signals

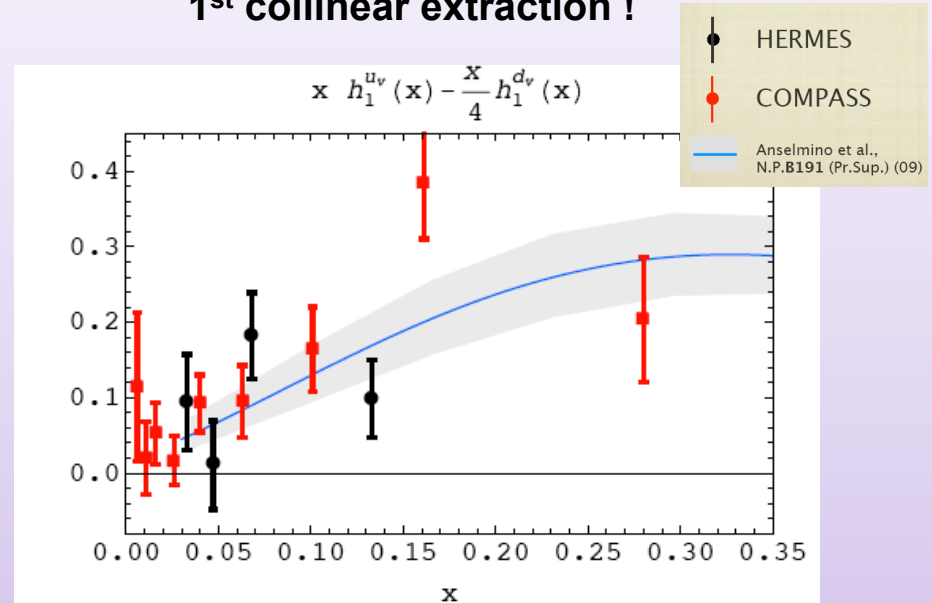


1st extraction of Transversity!



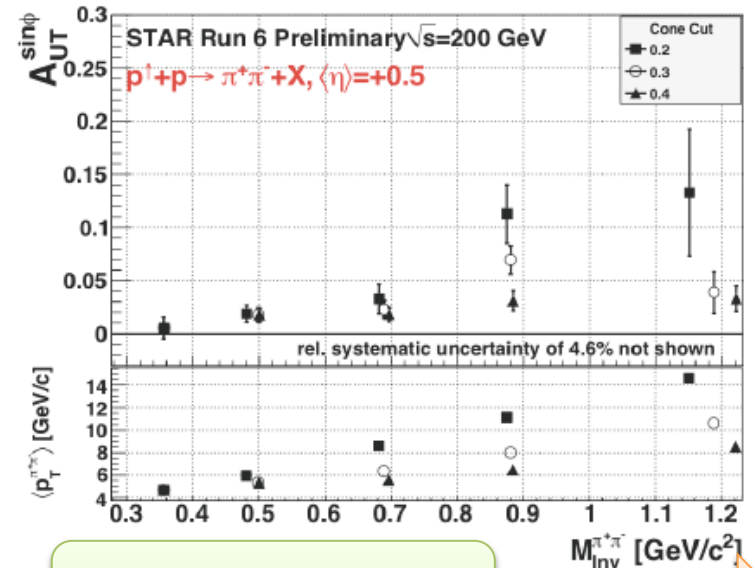
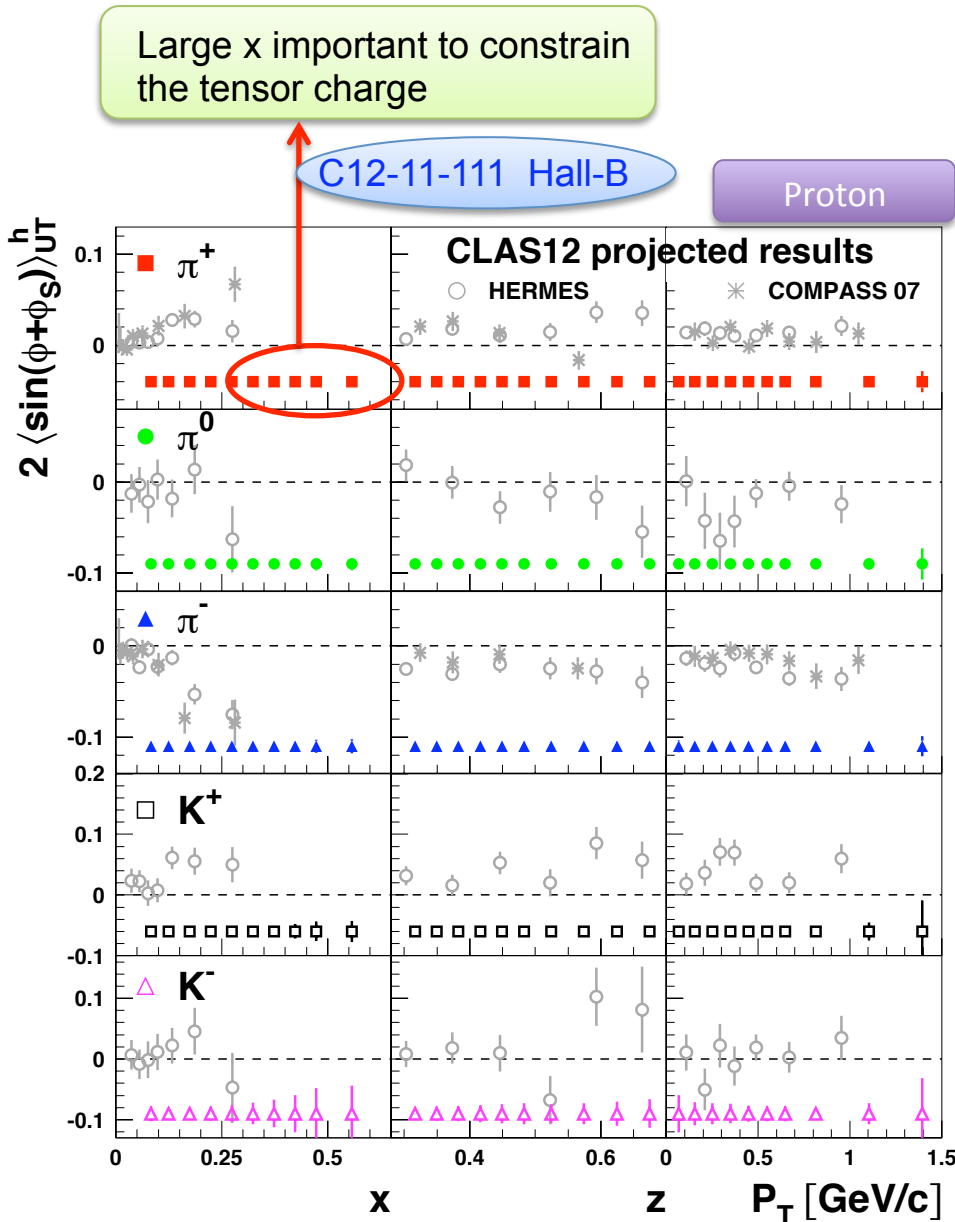
Anselmino ++ arXiv: 0701006

1st collinear extraction !



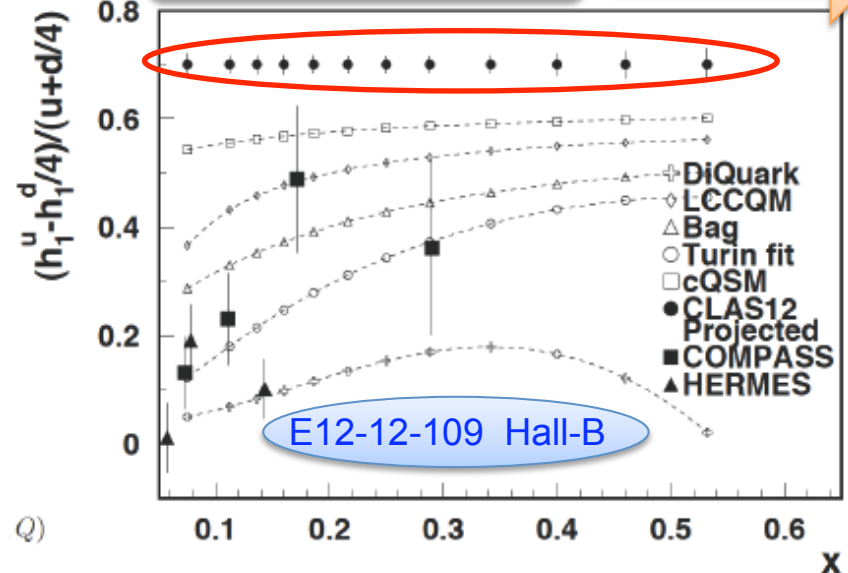
Bacchetta ++ arXiv: 1104.3855

Transversity @ JLab12 2014+



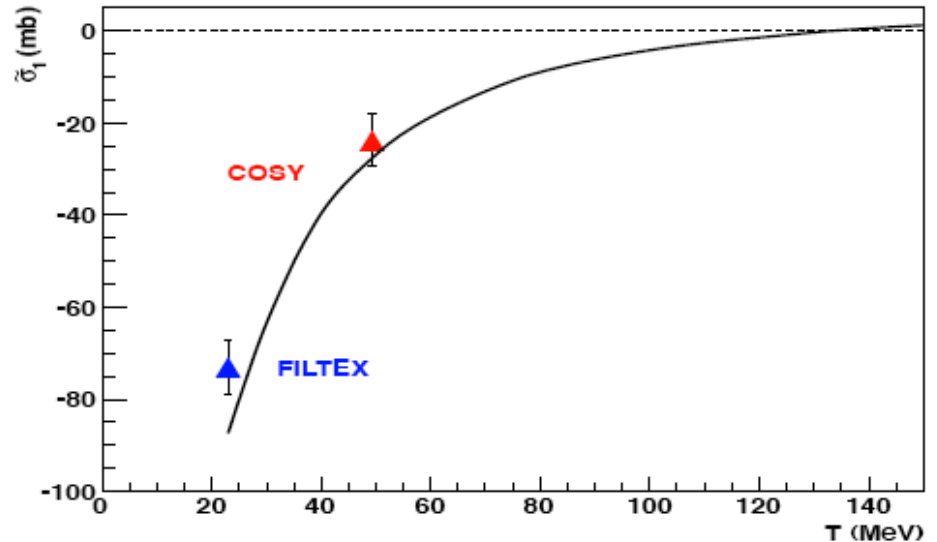
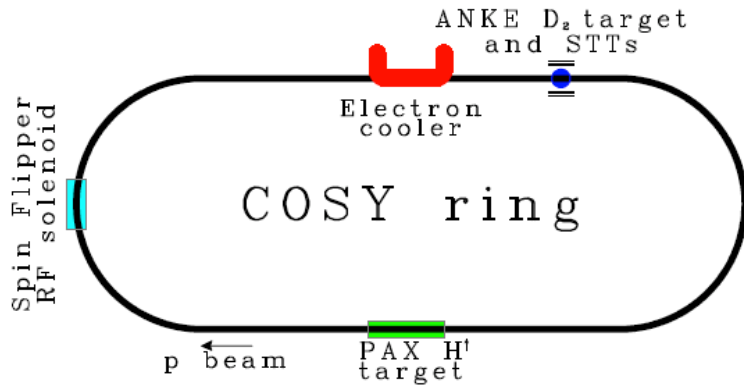
Di-hadron channel for h_1
Test of TMDs extraction

Pereira talk



Polarized Drell-Yan 2018+

Spin-filtering with protons:



Anti-proton beam @ FAIR

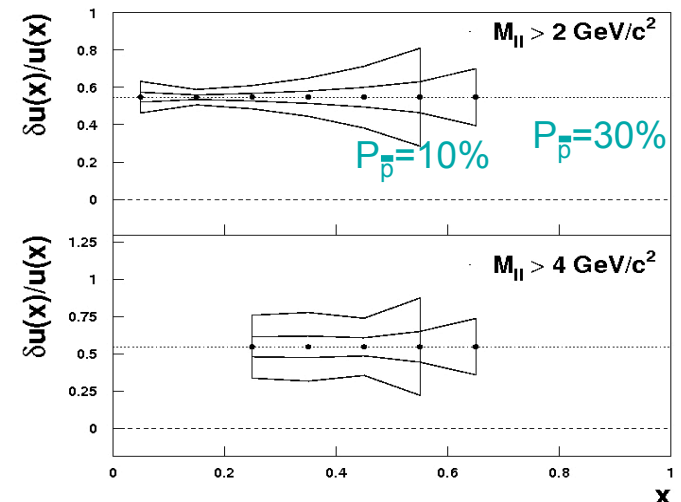
PANDA: unpolarized target ($s=30 \text{ GeV}^2$)

PAX: polarized collider ($s=200 \text{ GeV}^2$)

$$A_{TT} = \frac{d\sigma^{\uparrow\uparrow} - d\sigma^{\uparrow\downarrow}}{d\sigma^{\uparrow\uparrow} + d\sigma^{\uparrow\downarrow}} \approx \hat{a}_{TT} \frac{h_{1u}(x_1) h_{1u}(x_2)}{u(x_1) u(x_2)}$$

- u-dominance
- $|h_{1u}| > |h_{1d}|$
















1year run: 10 % precision on the $h_{1u}(x)$ in the valence region



Angular-Momentum Effects



PRETZELOSITY

N/q	U	L	T
U	f_1  Number Density		h_1^\perp  -  Boer-Mulders
L		g_1  -  Helicity	h_{1L}^\perp  -  Worm-gear
T	f_{1T}^\perp  -  Sivers	g_{1T}^\perp  -  Worm-gear	h_1  -  Transversity h_{1T}^\perp  -  Pretzelosity

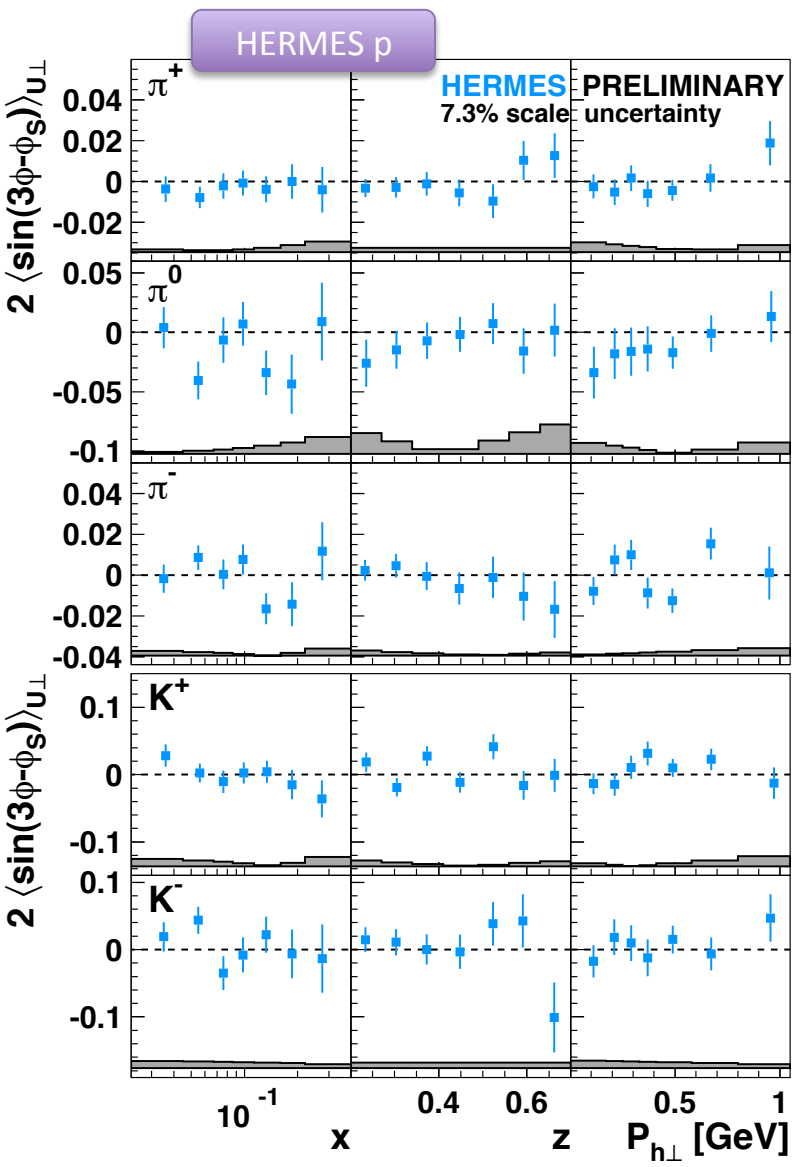
nucleon polarisation

Sensitive to the D-wave component and the non spherical shape of the nucleon

(THE D-WAVE)

The Pretzelosity

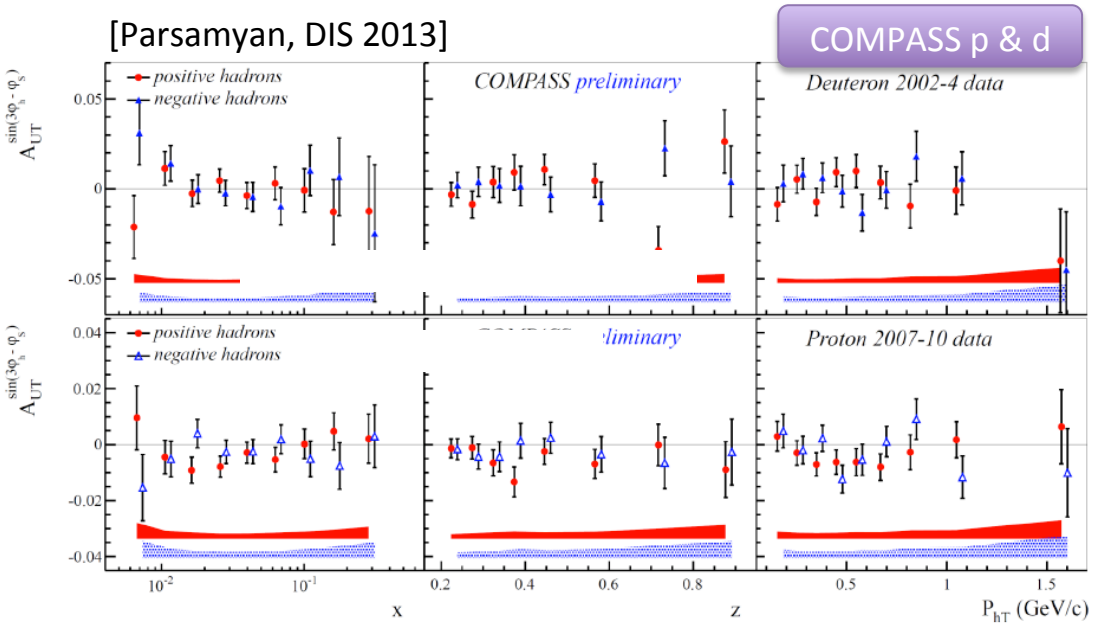
$$h_{1T}^\perp \otimes H_1^\perp$$



$$h_{1T}^{\perp(1)q}(x) = g_1^q(x) - h_1^q(x) \quad \text{no-gluon models}$$

$$\left| h_{1T}^{\perp(1)q}(x) \right| + \left| h_1^q(x) \right| \leq f_1^q(x) \quad \text{positivity bound}$$

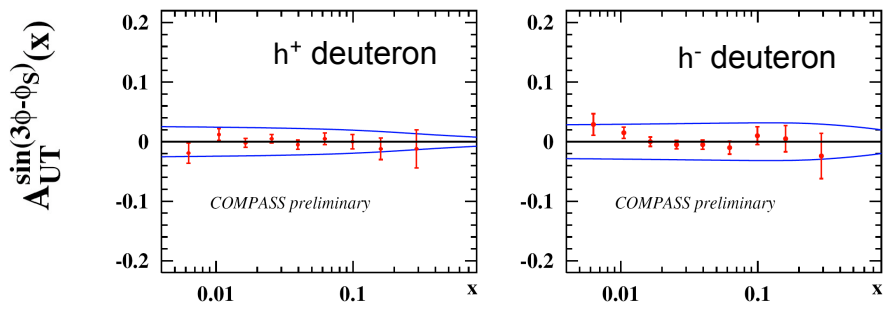
Asymmetry suppressed vs Collins by a factor $\sim \left| P_{h\perp}^2 \right|$



The Pretzelosity

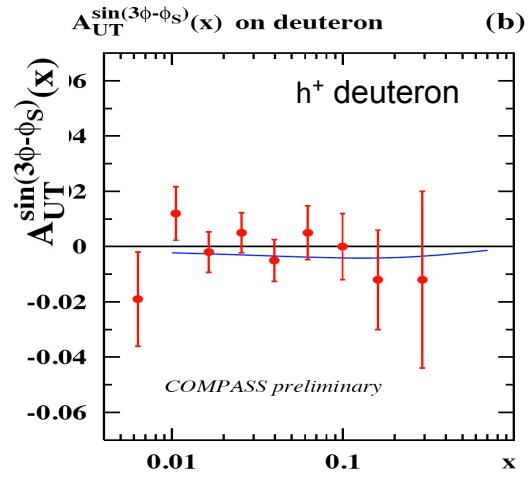
$$h_{1T}^\perp \otimes H_1^\perp$$

Statistical power of existing data is not enough to observe significant signals



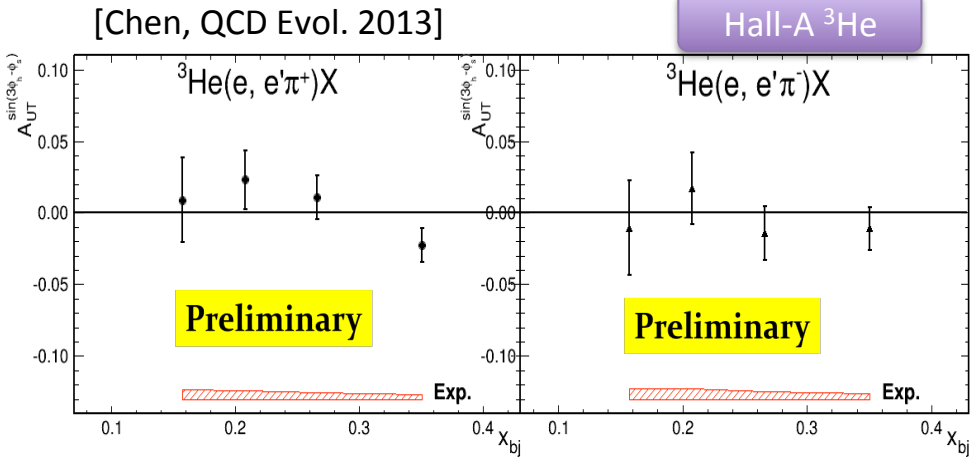
Positivity bound

Avakian, PRD78

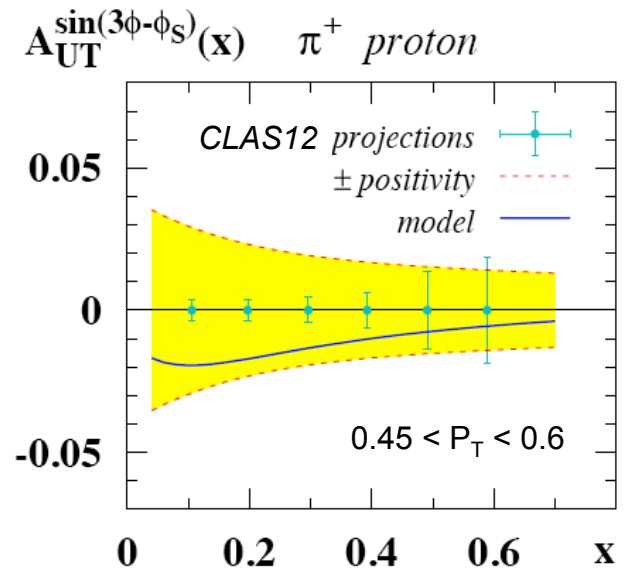


Covariant model
arXiv: 0812.3246

Parsamyan talk



Hall-A ³He



WORM GEAR

N/q	U	L	T
U	f_1 Number Density		h_1^\perp Boer-Mulders
L		g_1 Helicity	h_{1L}^\perp Worm-gear
T	f_{1T}^\perp Sivers	g_{1T}^\perp Worm-gear	h_1^\perp Transversity h_{1T}^\perp Pretzelosity

nucleon polarisation

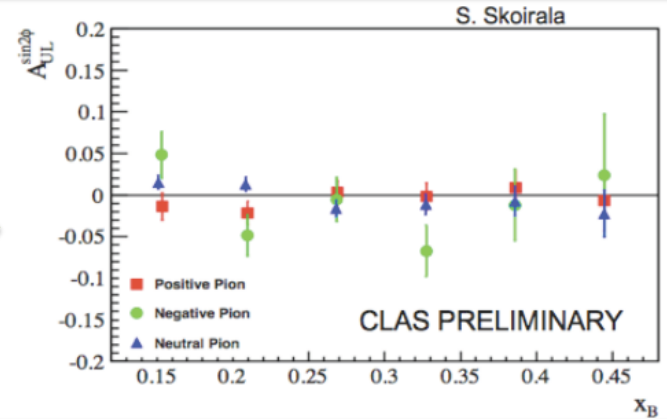
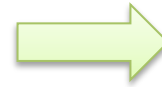
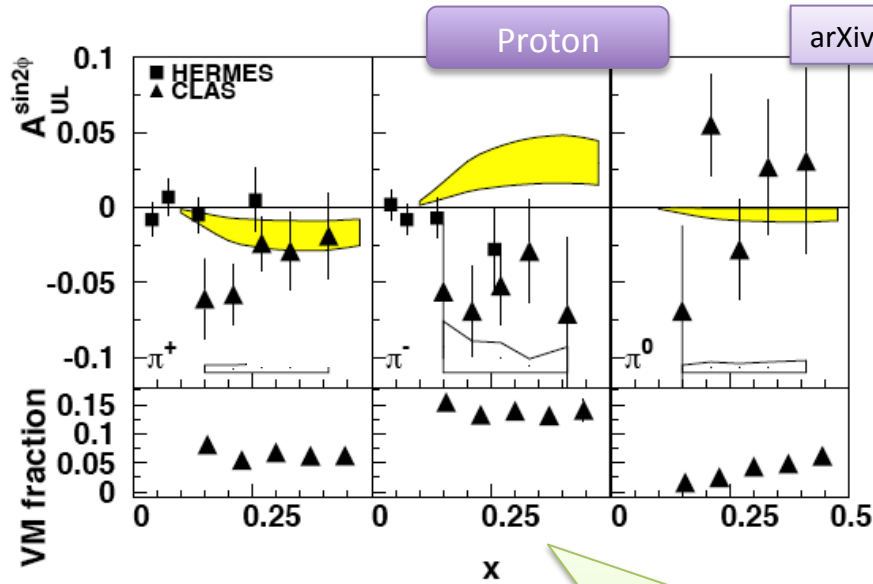
Proton wave-components with different OAM

The only T-even and chirally-even off-diagonal TMD

(THE STANDARD OAM EFFECT)

The $A_{UL}^{\sin 2\phi}$ Asymmetry

$$h_{1L}^{\perp} \otimes H_1^{\perp}$$



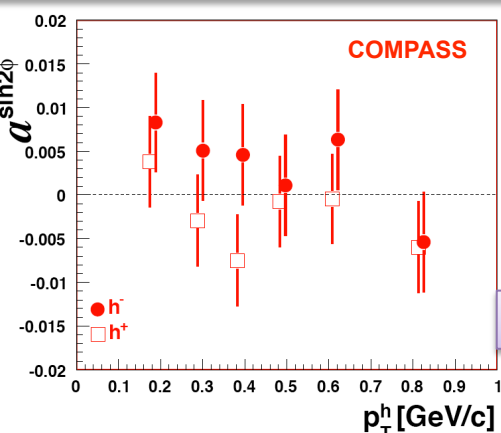
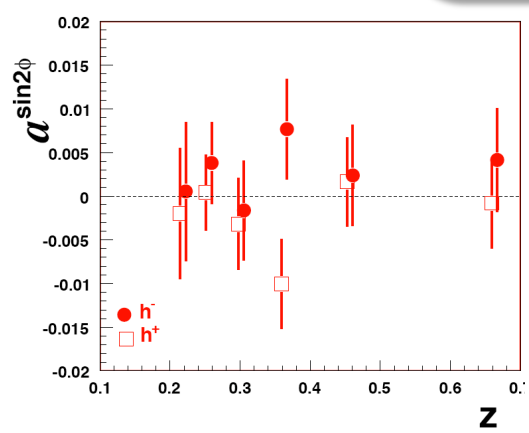
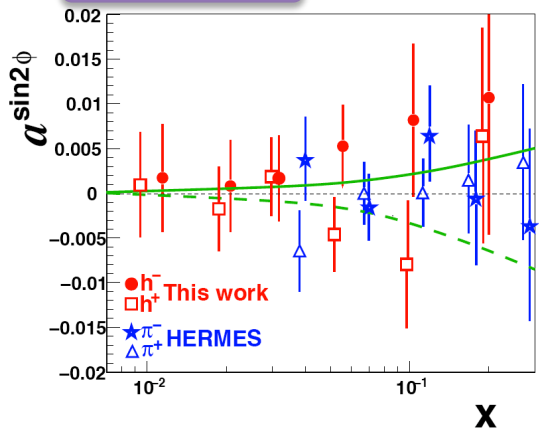
Unexpected pattern needs more statistics to be verified

Statistics not enough to investigate relations supported by many theoretical models:

$$g_{1T}^q = -h_{1L}^{\perp q} \quad (\text{model-dependent relation})$$

$$h_{1L}^{q(1)}(x) \approx -x^2 \int_x^1 \frac{dy}{y} h_1^q(y) \quad (\text{Wandura-Wilczek type approximation})$$

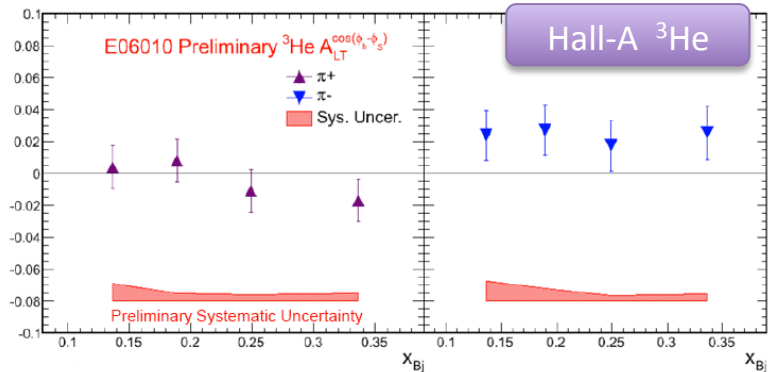
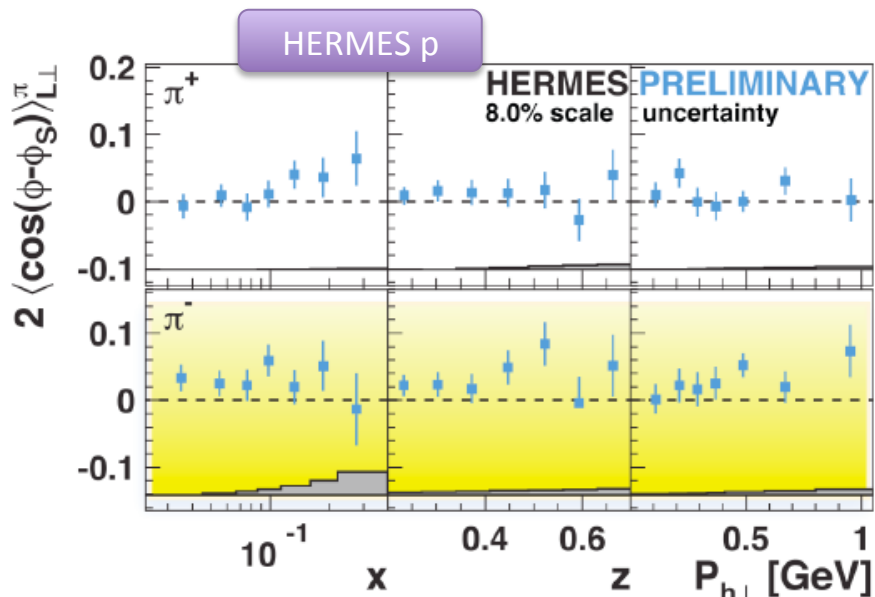
Deuteron



arXiv: 1007.1562

The $A_{LT}^{\cos(\phi-\phi_S)}$ Asymmetry

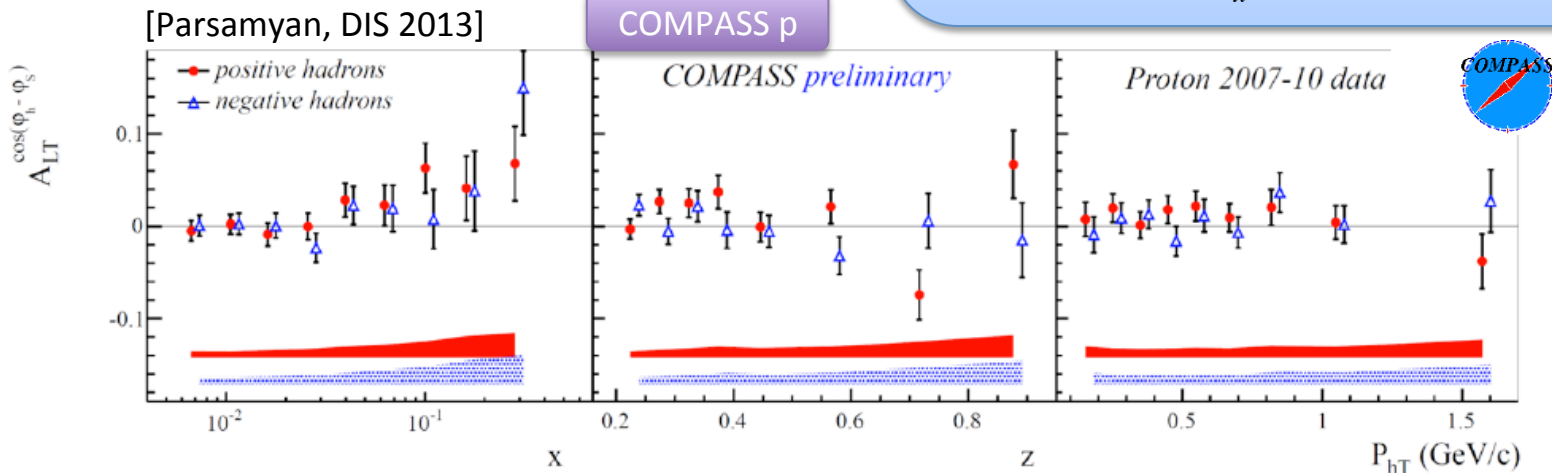
$$g_{1T}^{\perp} \otimes D_1$$



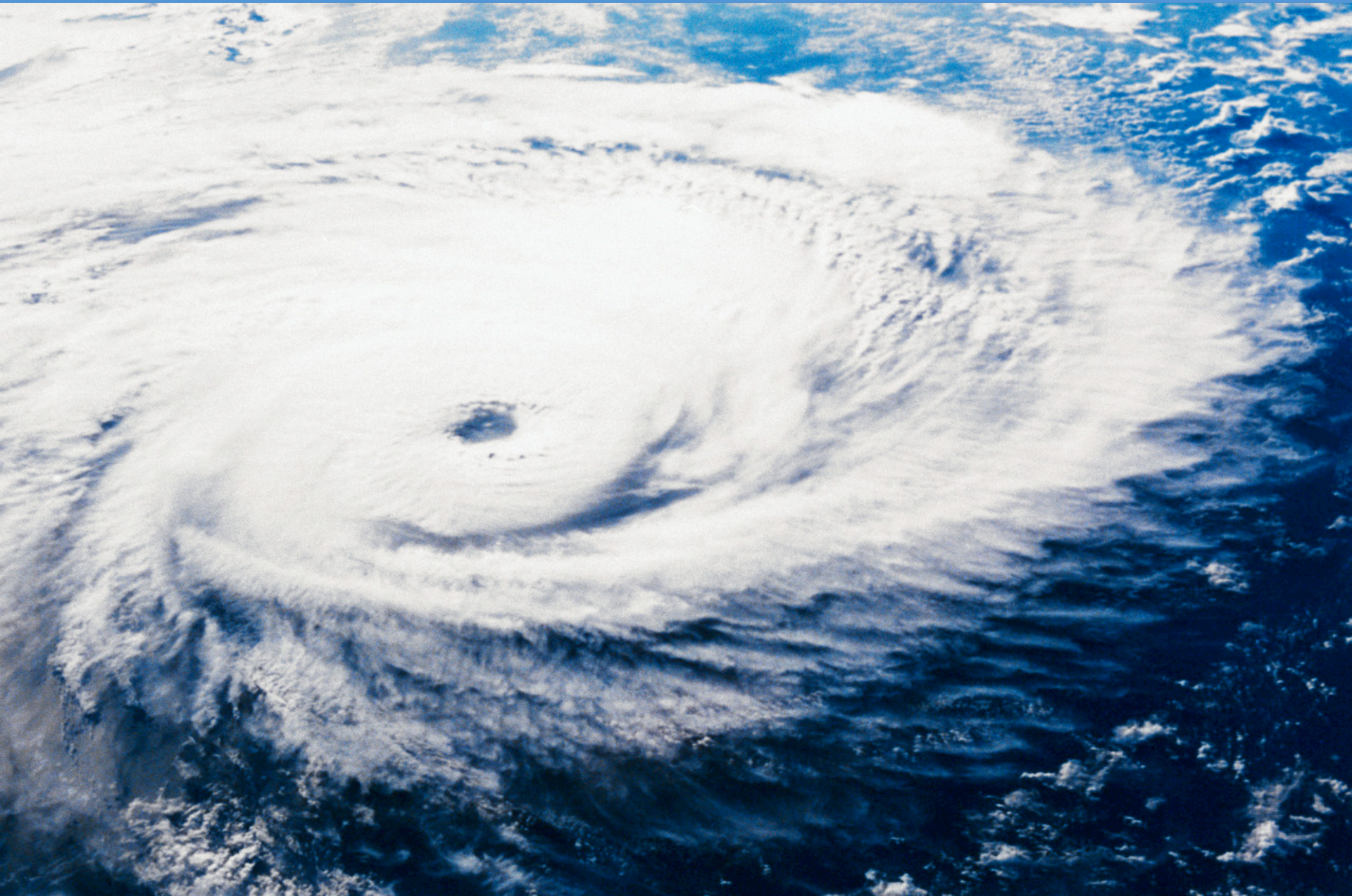
First evidences found by the experiments
 Statistics not enough to investigate relations
 supported by many theoretical models:

$$g_{1T}^q = -h_{1L}^{\perp q} \quad (\text{model-dependent relation})$$

$$g_{1T}^{q(1)}(x) \approx x \int_x^1 \frac{dy}{y} g_1^q(y) \quad (\text{Wandura-Wilczek type approximation})$$

















Spin-Orbit Effects

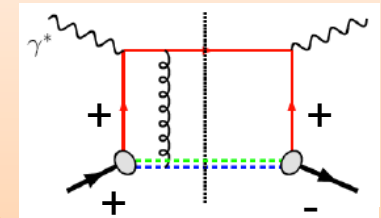


SIVERS

nucleon polarisation

N/q	U	L	T
U	f_1  <i>Number Density</i>		h_1^\perp  -  <i>Boer-Mulders</i>
L		g_1  -  <i>Helicity</i>	h_{1T}  <i>Worm-gear</i>
T	f_{1T}^\perp  -  <i>Sivers</i>	g_{1T}^\perp  -  <i>Worm-gear</i>	h_1  -  <i>Transversity</i> h_{1T}^\perp  -  <i>Pretzelosity</i>

Naïve-T-odd
Non-trivial gauge link



Process dependence

(THE TMD CHALLENGE)

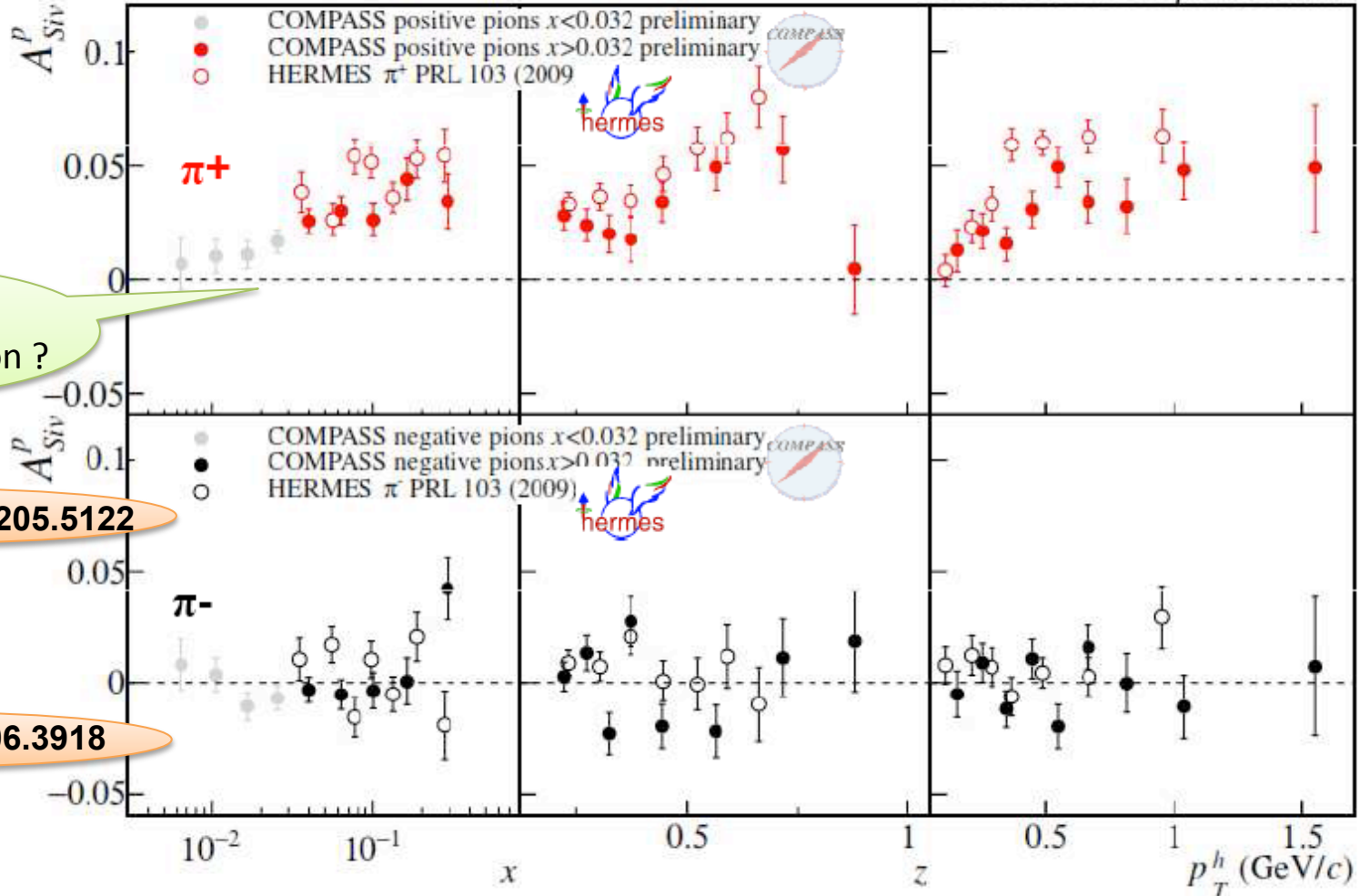
The Sivers signals

$$f_{1T}^\perp \otimes D_1$$

$$A_{UT}^{\sin(\phi - \phi_S)} \propto \frac{\sum_q e_q^2 f_{1T}^{\perp,q}(x, p_T^2) \otimes_\omega D_1^q(z, k_T^2)}{\sum_q e_q^2 f_1^q(x, p_T^2) \otimes D_1^q(z, k_T^2)}$$

CLEAR NON ZERO SIGNALS !

COMPASS 2010 proton data



Systematic shift:
Sivers Q^2 evolution ?

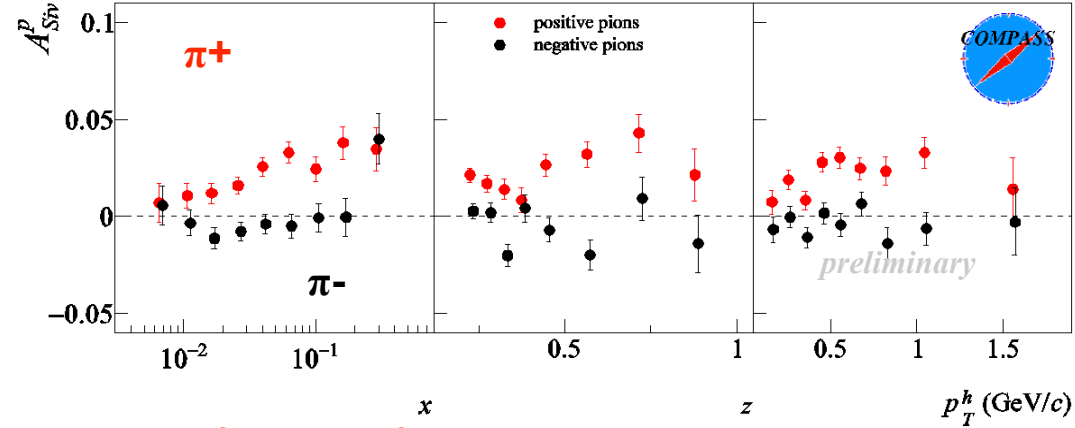
COMPASS, arXiv: 1205.5122

HERMES, arXiv: 0906.3918

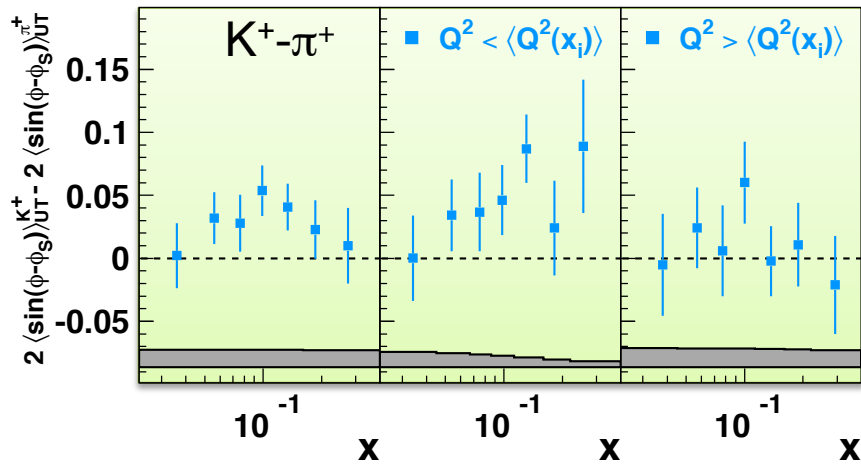
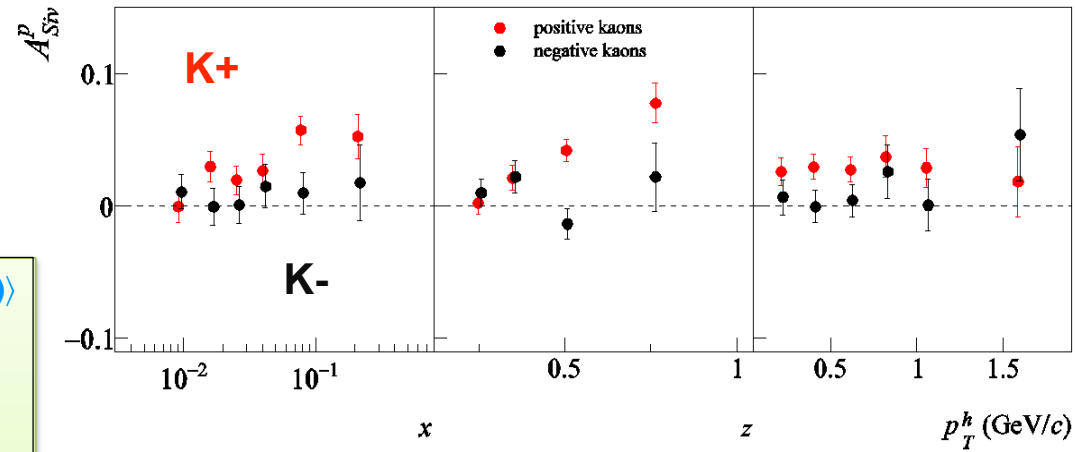
The Kaon Sivers signals

$$f_{1T}^\perp \otimes D_1$$

combined 2007 – 2010 results

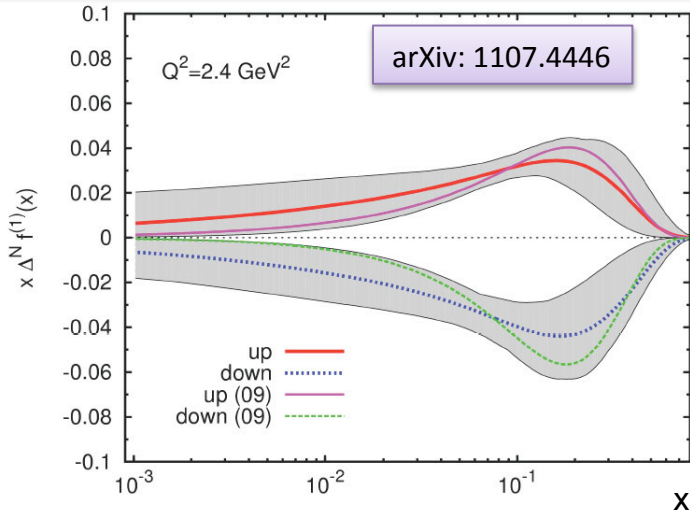


larger for K+ than for π^+



The Sivers challenges - I

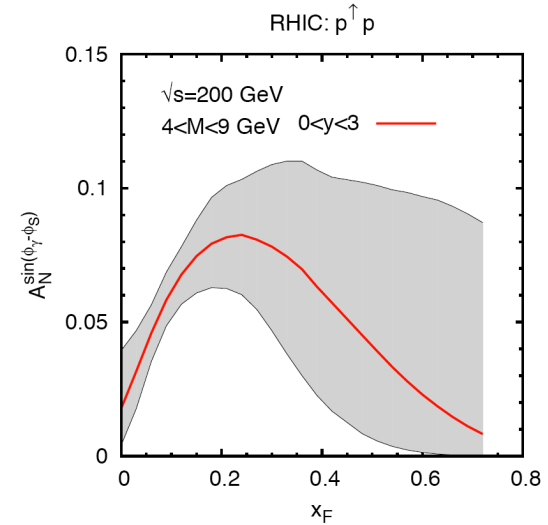
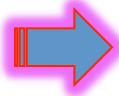
$$f_{1T}^{\perp} \otimes D_1$$



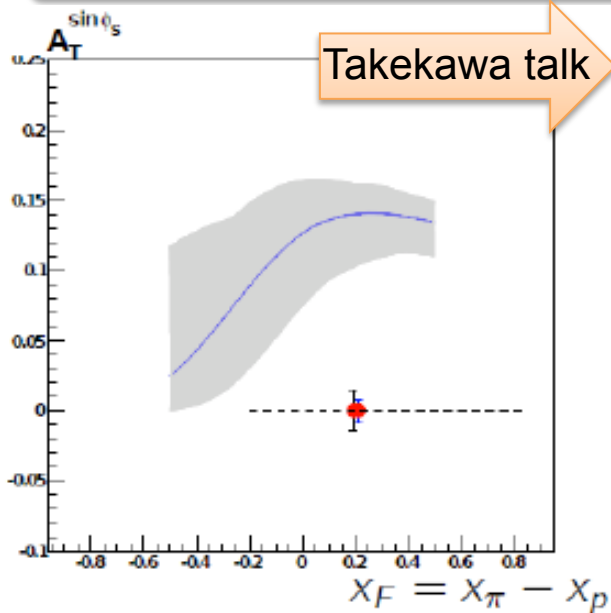
From SIDIS to Drell-Yan:

Sign change as a crucial test of TMDs factorization

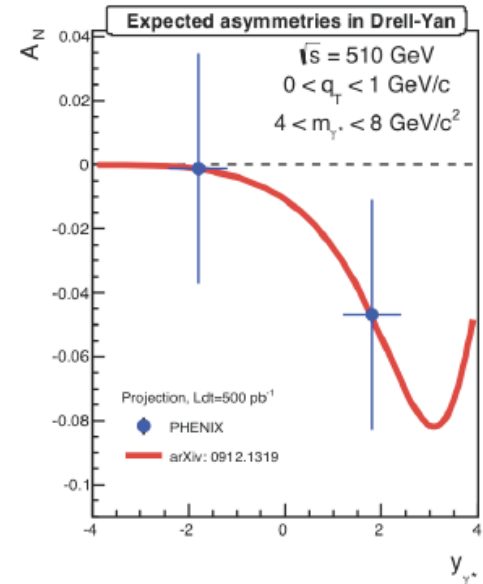
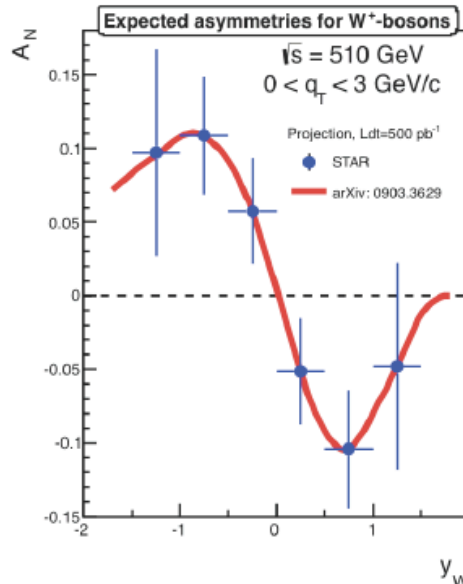
arXiv: 0901.3078



πH^{\uparrow} @ CERN

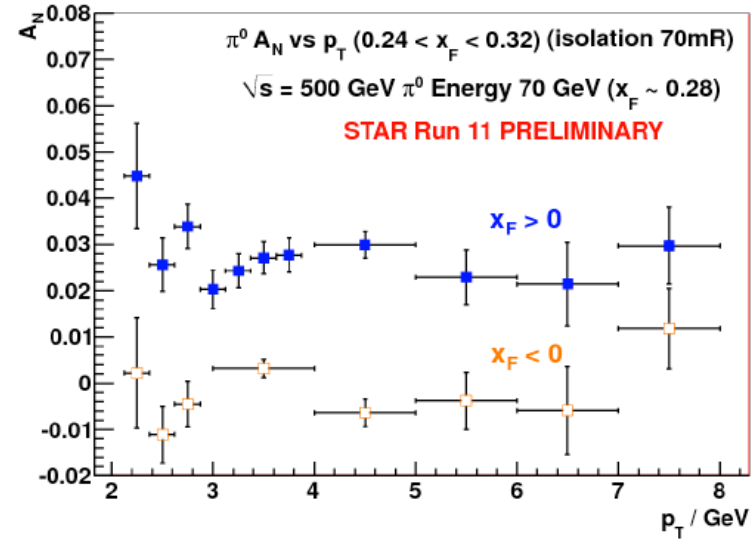
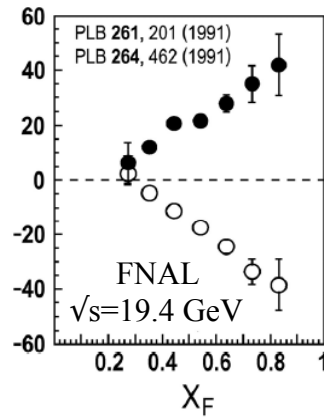
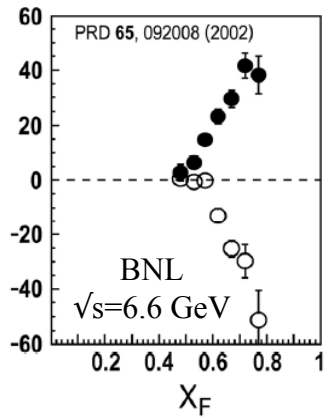
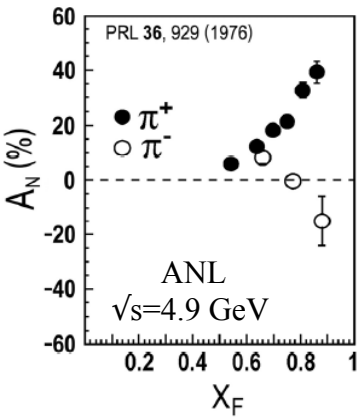


$p^{\uparrow} p$ @ Brookhaven



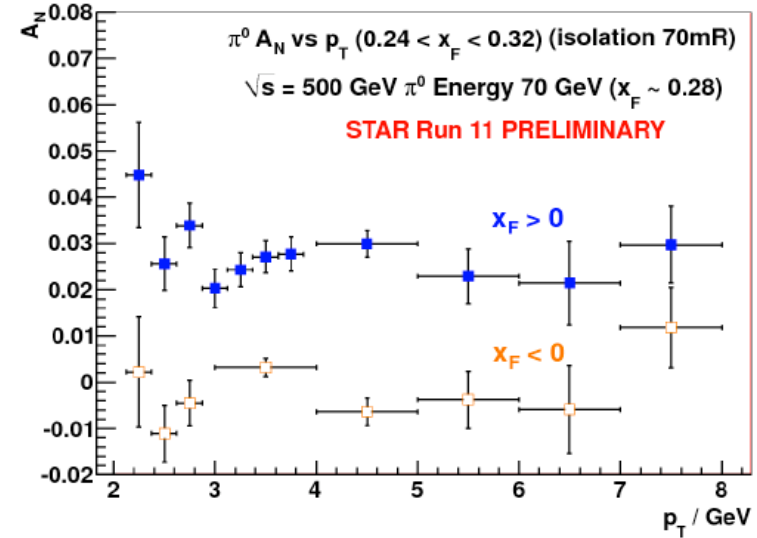
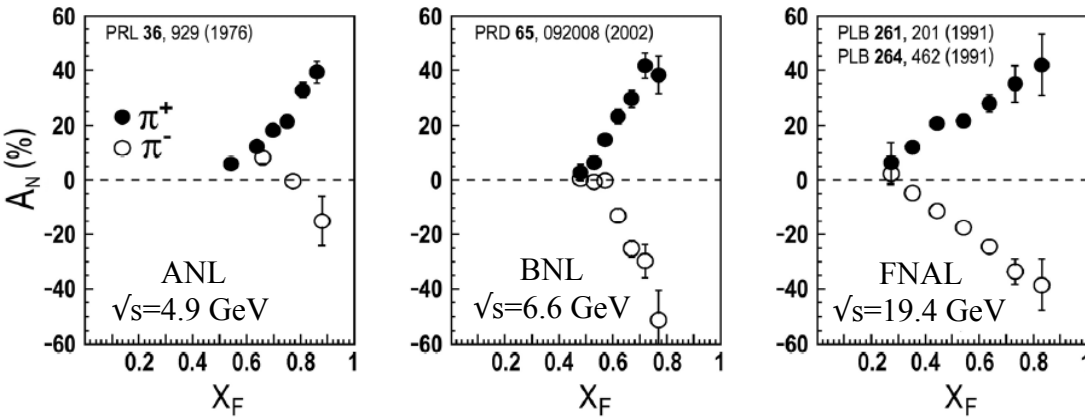
The Sivers challenges - II

$$f_{1T}^{\perp} \otimes D_1$$



The Sivers challenges - II

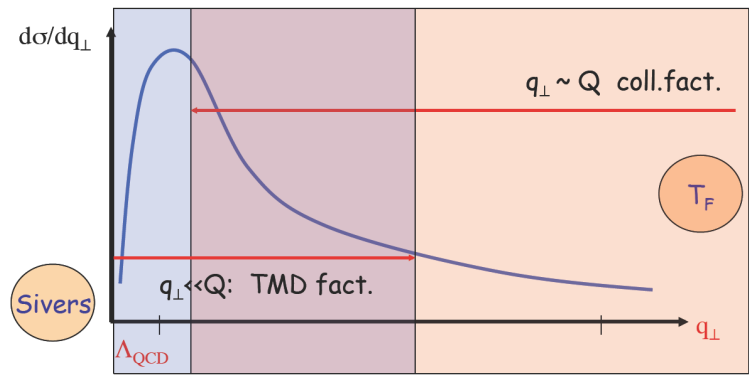
$$f_{1T}^\perp \otimes D_1$$



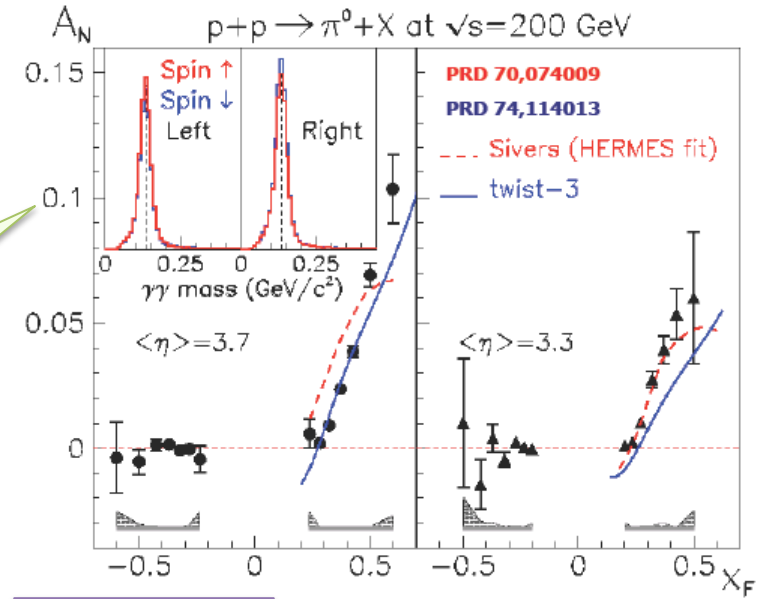
From SIDIS to pp: A possible candidate to explain SSA

Coverage at large p_T and relation with twist-3 collinear approach

$$gT_{q,F}(x, x) = - \int d^2 k_\perp \frac{|k_\perp|^2}{M} f_{1T}^{\perp q}(x, k_\perp^2) |_{\text{SIDIS}}$$



After 1st promising results a sign mismatch was found



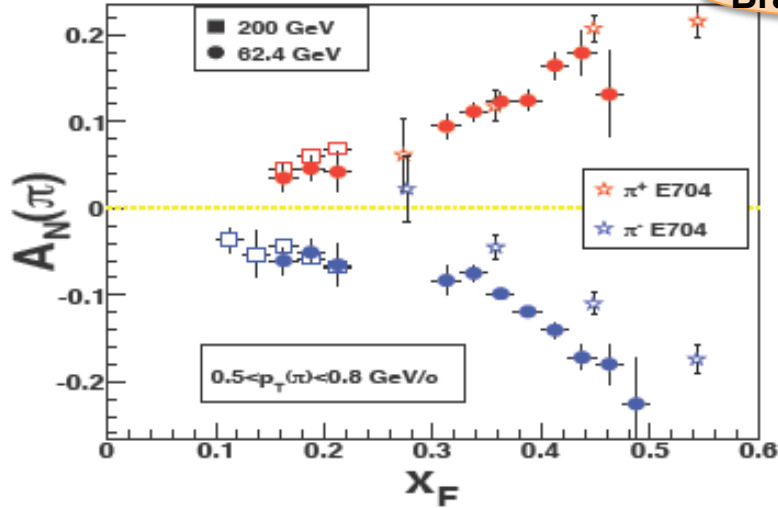
arXiv: 0801.2990

$\Lambda_{\text{QCD}} \ll q_\perp \ll Q$ same physics

The Sivers challenges - II

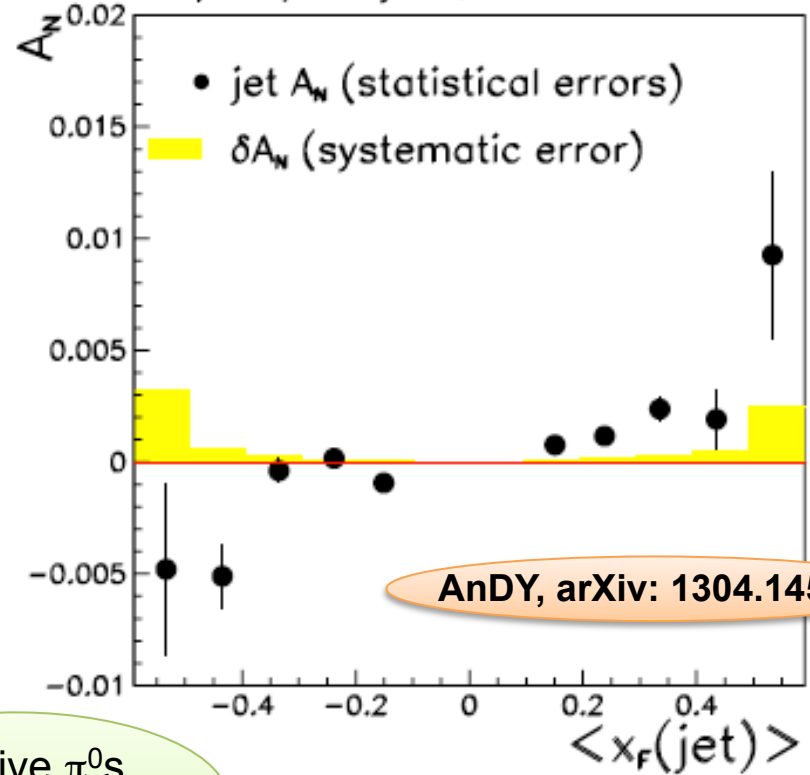
$$f_{1T}^\perp \otimes D_1$$

Brahms, PRL 101 (2008) 042001

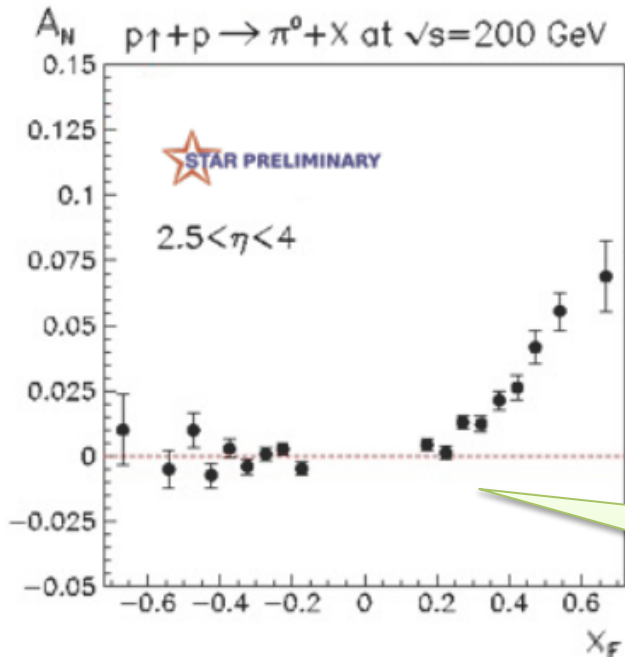


Inclusive Jets,
No FF involved

$p^\uparrow + p \rightarrow \text{jets}, \sqrt{s}=500 \text{ GeV}$



AnDY, arXiv: 1304.1454

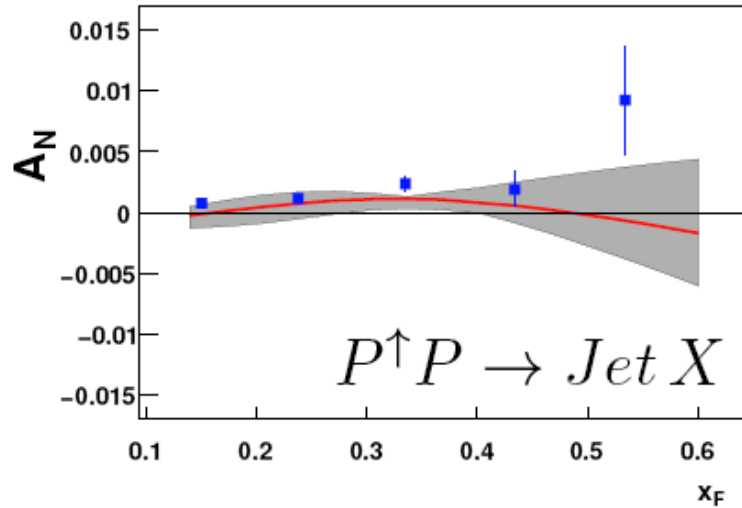


Inclusive π^0 s,
Collins FF cancels ?

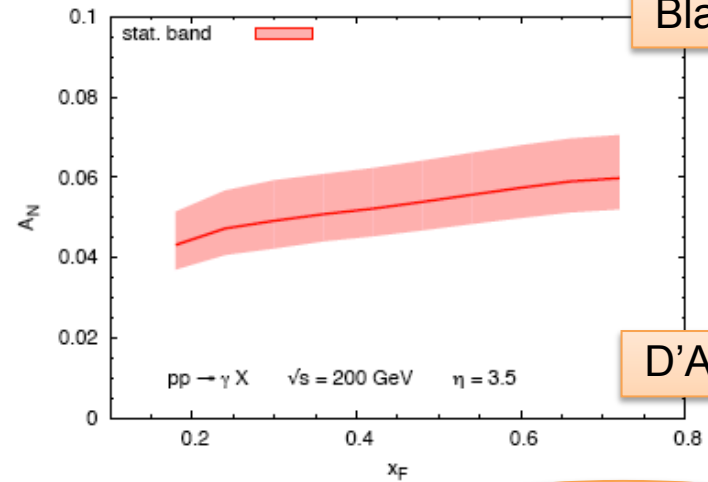
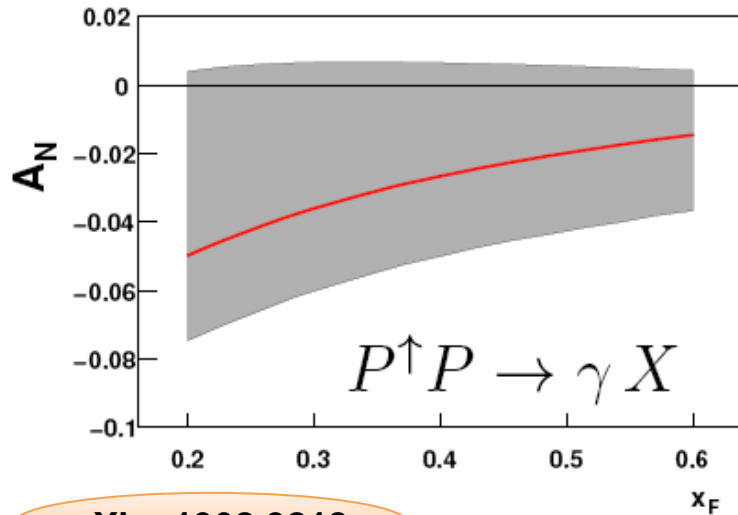
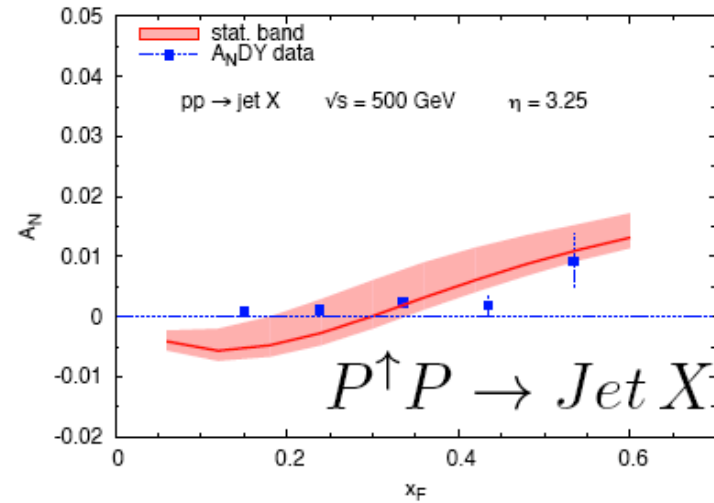
The Sivers challenges - II

$$f_{1T}^\perp \otimes D_1$$

w/ color factors



w/o color factors



Bland talk

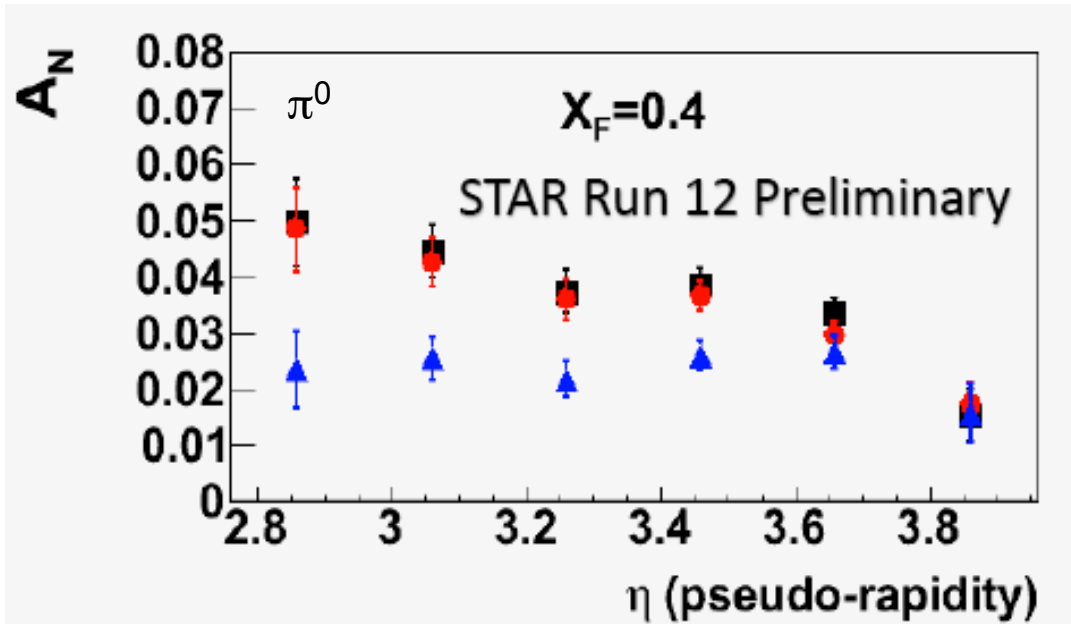
D'Alesio talk

arXiv: 1302.3218

arXiv: 1304.7691

The Sivers challenges - II

$$f_{1T}^\perp \otimes D_1$$



(Least Jet like) 

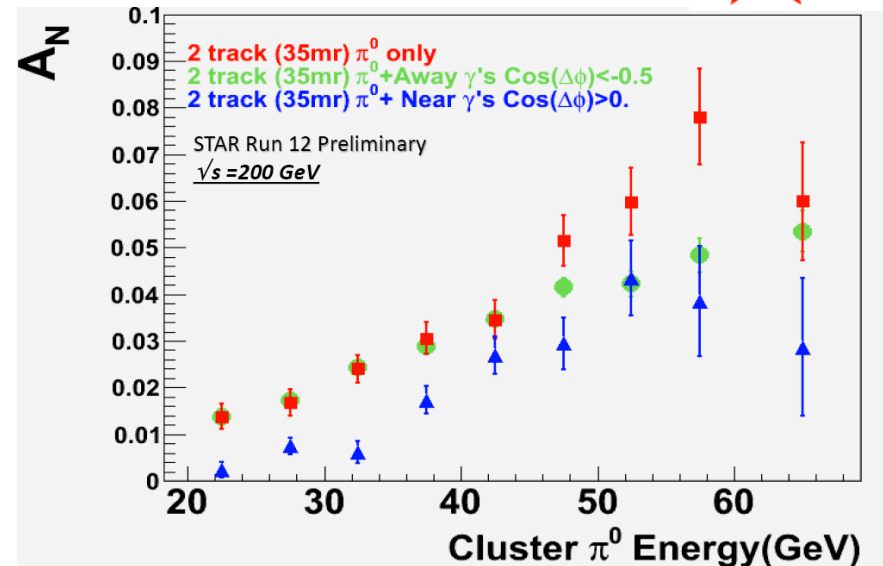
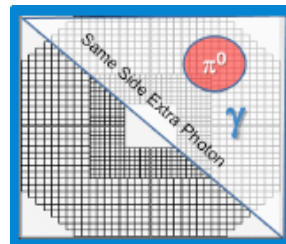
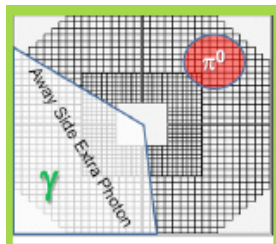
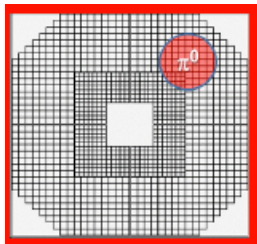
(More Jet like) 

(Most Jet like) 



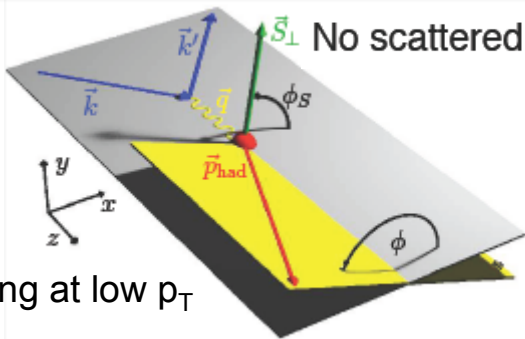
Heppelmann, DIS 2013

Asymmetry depends on isolation criteria (jet-like fragmentation)



Inclusive hadron SSA in SIDIS

$$f_{1T}^\perp \otimes D_1$$



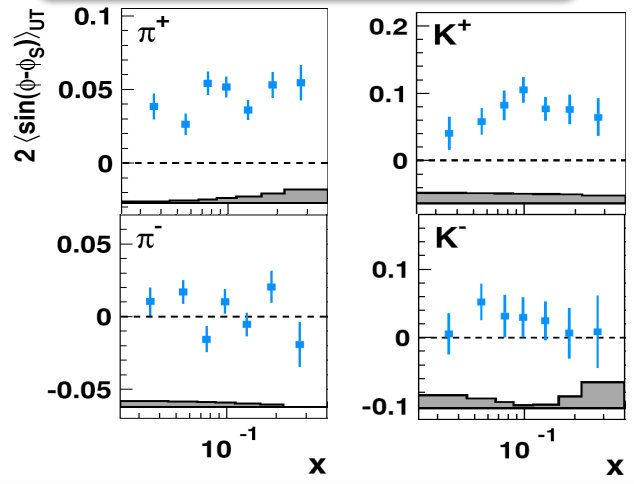
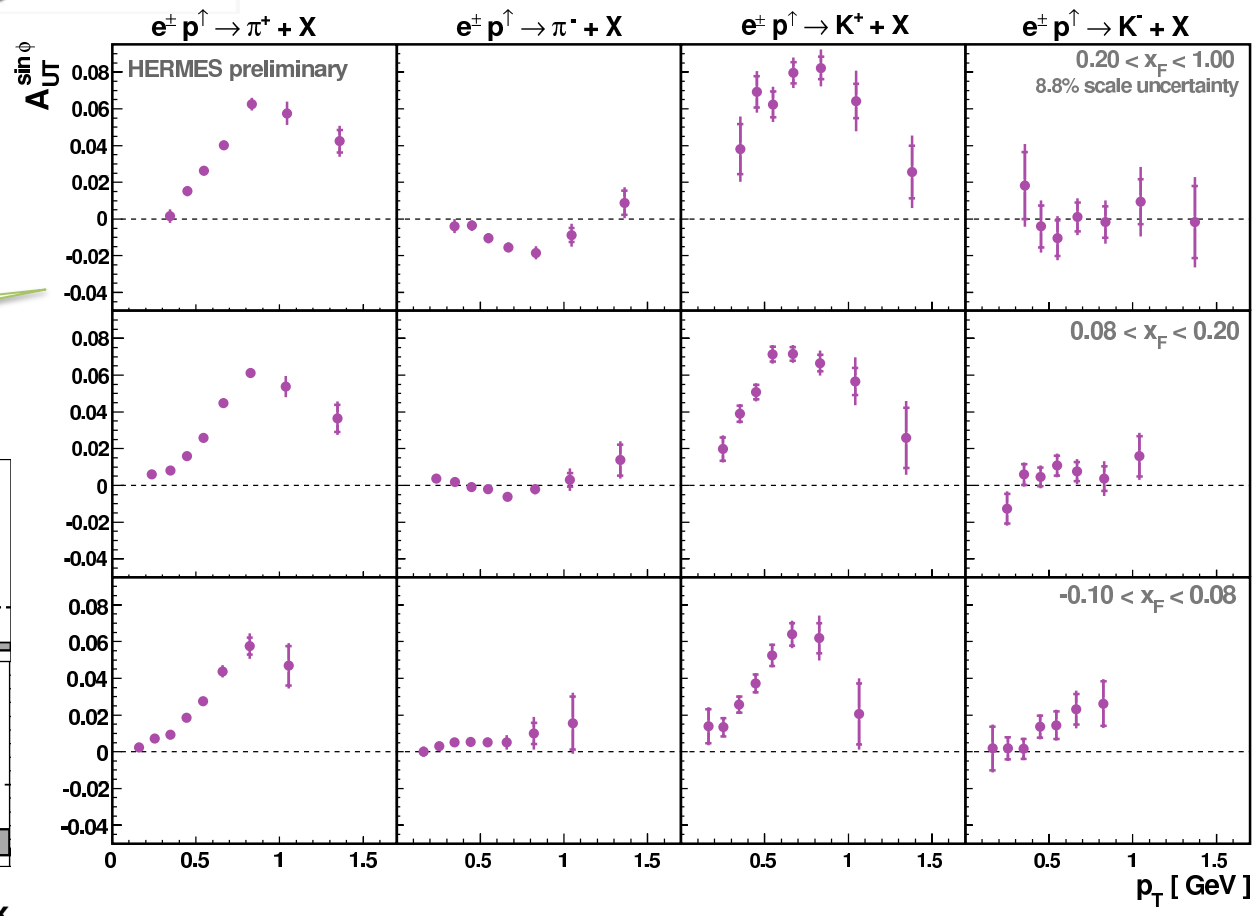
No scattered beam detected \rightarrow $\mathbf{p}_T, \mathbf{x}_F$ with respect to \mathbf{e} beam (not \mathbf{q} -vector)

Sivers modulation $\sin(\phi - \phi_S)$ can survive as $\sin(\phi)$

$$A(x_F, p_T, \phi) = \frac{\sigma_{UT}(x_F, p_T, \phi)}{\sigma_{UU}(x_F, p_T)} = [A_{UT} \sin\phi(x_F, p_T)] \sin\phi$$

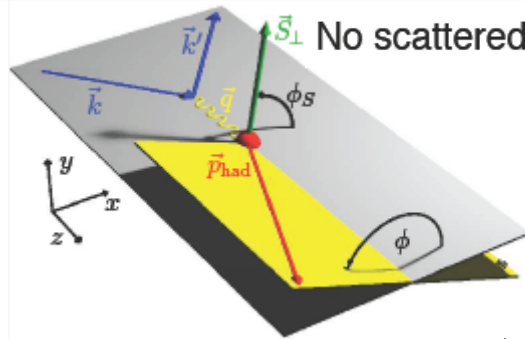
- ❖ A_{UT} is vanishing at low p_T
- ❖ Q^2 increases with p_T approaching DIS regime
- ❖ Study transition from perturbative to non-perturbative regime

Non-zero signals for positive hadrons resembling Sivers



Inclusive hadron SSA in SIDIS

$$f_{1T}^\perp \otimes D_1$$



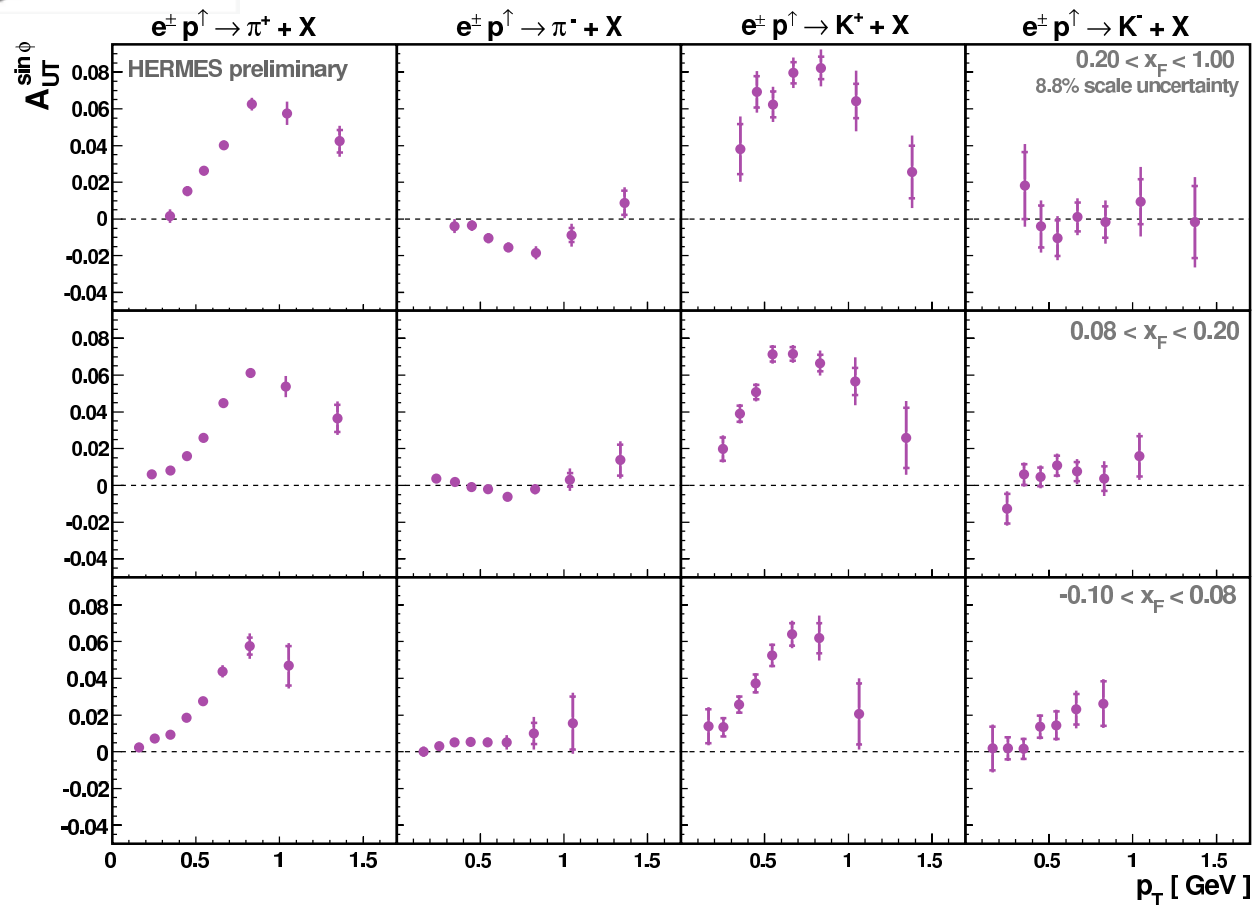
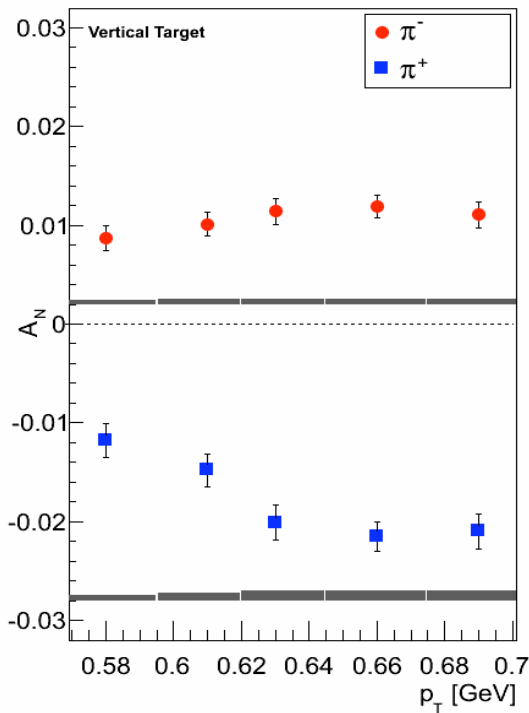
No scattered beam detected $\rightarrow \mathbf{p}_T, x_F$ with respect to \mathbf{e} beam (not \mathbf{q} -vector)

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Chen, QCD Evolution 13

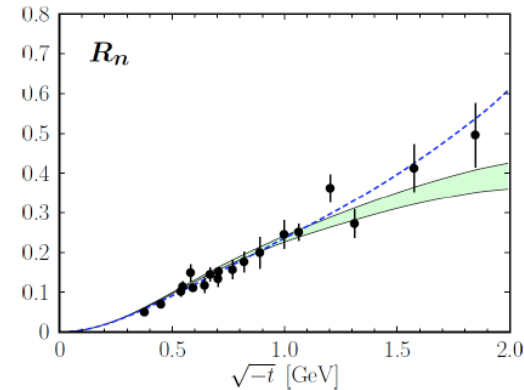
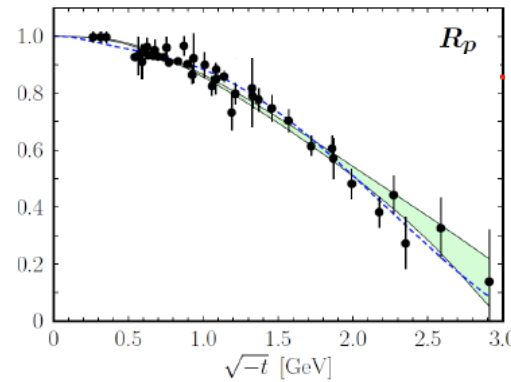
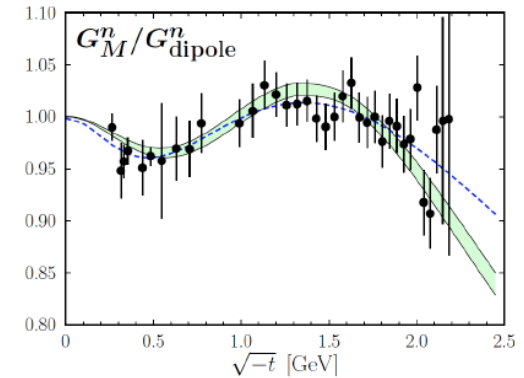
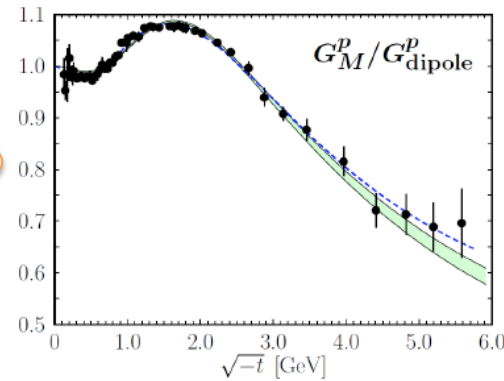
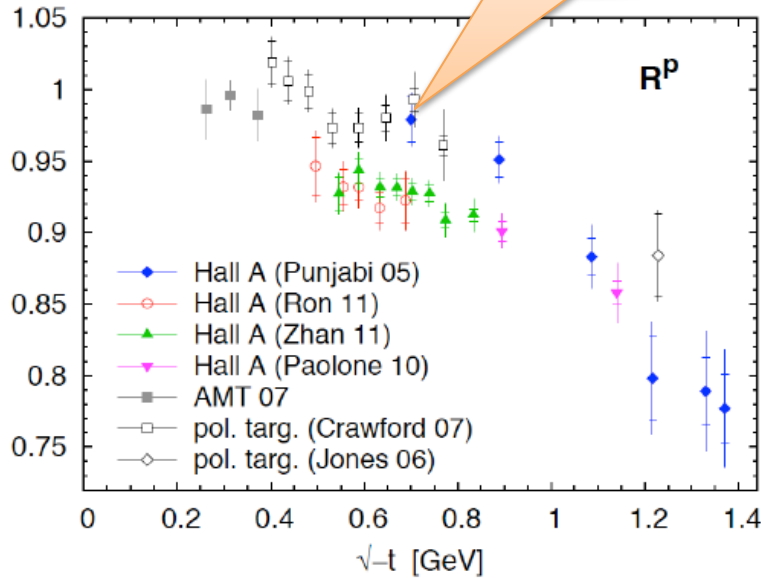
$e + {}^3\text{He}^\uparrow \rightarrow \pi^\pm + X$



OAM Glimpses

$$R^p = G_E^p / (G_M^p / \mu_p)$$

Inconsistency in DATA ?



- obtain at $\mu = 2$ GeV

$$J_v^u = 0.230^{+0.009}_{-0.024}$$

$$J_v^d = -0.004^{+0.010}_{-0.016}$$

Diehl et al. arXiv: 1302.4604

- within errors consistent with determination from Sivers distrib. and model for chromodynamic lensing:

$$J_v^u = 0.214^{+0.009}_{-0.013}$$

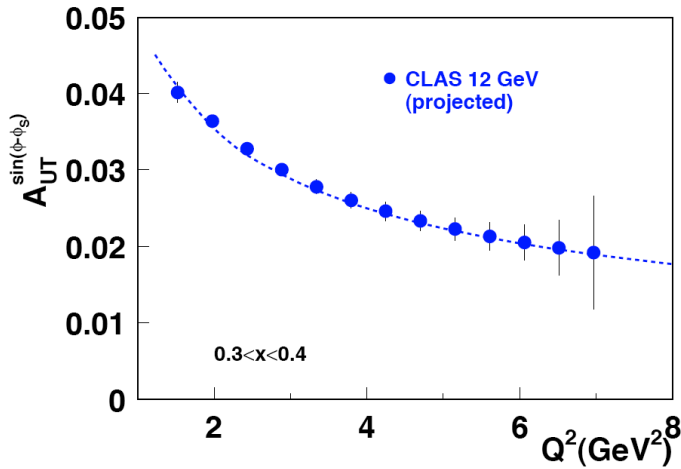
$$J_v^d = -0.029^{+0.021}_{-0.008}$$

Bacchetta et al. arXiv: 1107.5755

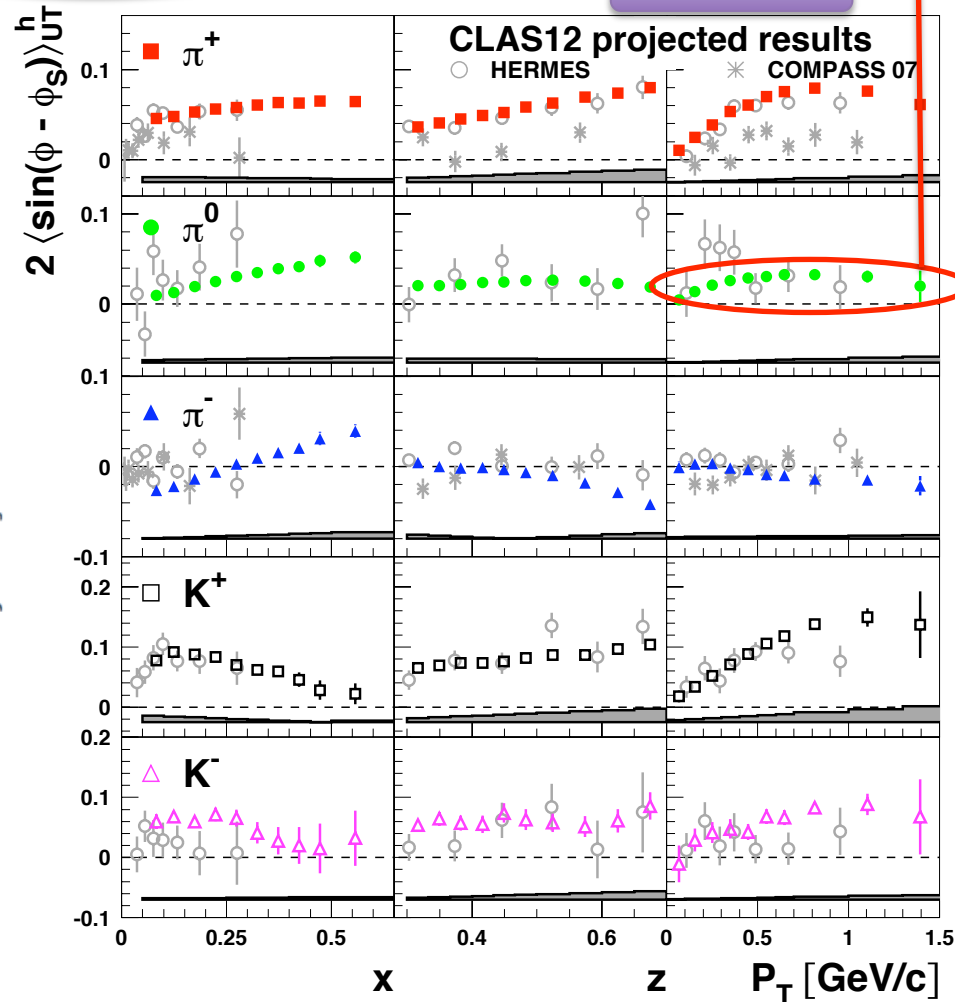
Bacchetta talk

Sivers @ JLab12 2014+

High resolution and broad range in p_T to test perturb. non-perturb. transient and for Bessel function analysis

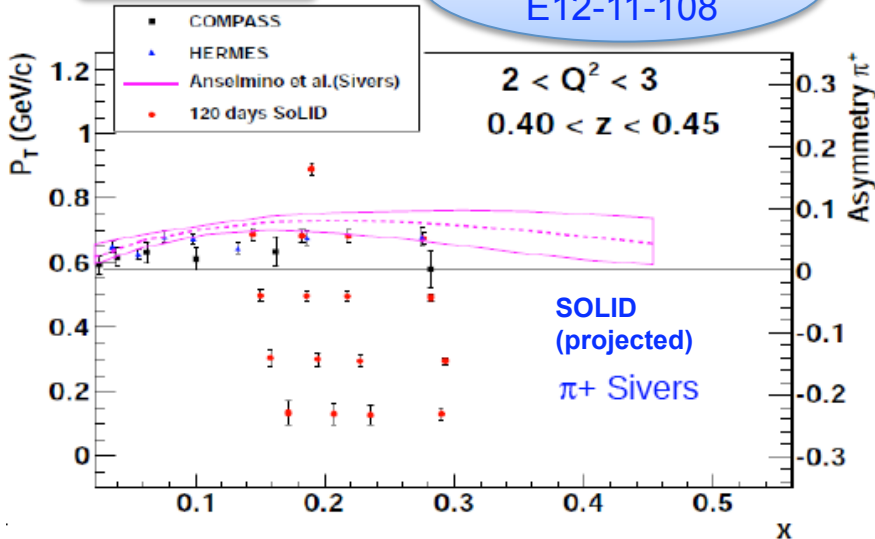


C12-11-111 Hall-B


















Proton & ^3He

E12-10-006 Hall-A
E12-11-108



CAHN & BOER-MULDERS

	N/q	U	L	T
nucleon polarisation	U	f_1  Number Density		h_1^\perp  -  Boer-Mulders
	L		g_1  -  Helicity	h_{1L}^\perp  -  Worm-gear
	T	f_{1T}^\perp  -  Sivers	g_{1T}^\perp  -  Worm-gear	h_1  -  Transversity h_{1T}^\perp  -  Pretzelosity

Naïve-T-odd
Chirally-odd
Spin effect in unpolarized
reactions

(THE NEGLECTED EFFECTS)

The azimuthal modulation

$$h_1^\perp \otimes H_1^\perp$$

$$\frac{d^5 \sigma^{ep \rightarrow e' h X}}{dx dy dz d\phi dP_{h\perp}^2} \propto \{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos(\phi) F_{UU}^{\cos(\phi)} + \varepsilon s \cos(2\phi) F_{UU}^{\cos(2\phi)} \}$$

$$(f_1 \otimes D_1) / Q$$

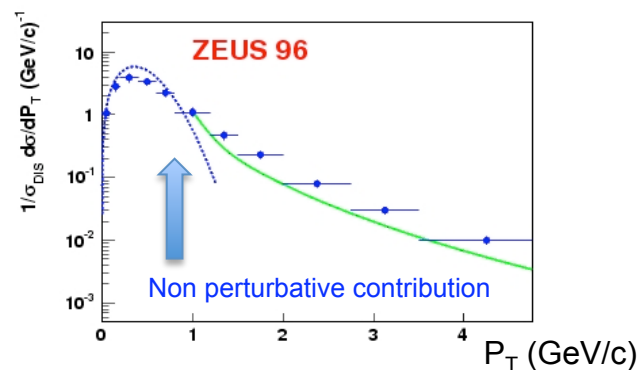
$$h_1^\perp \otimes H_1^\perp$$

Kinematical effect predicted since 1978
by Cahn due to non-zero intrinsic k_T

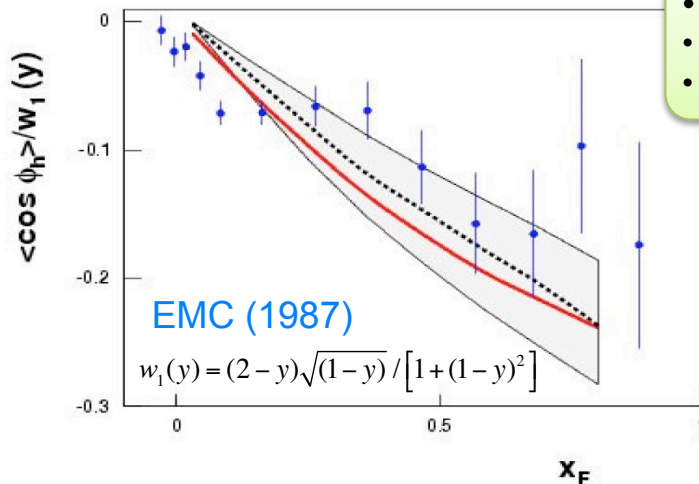
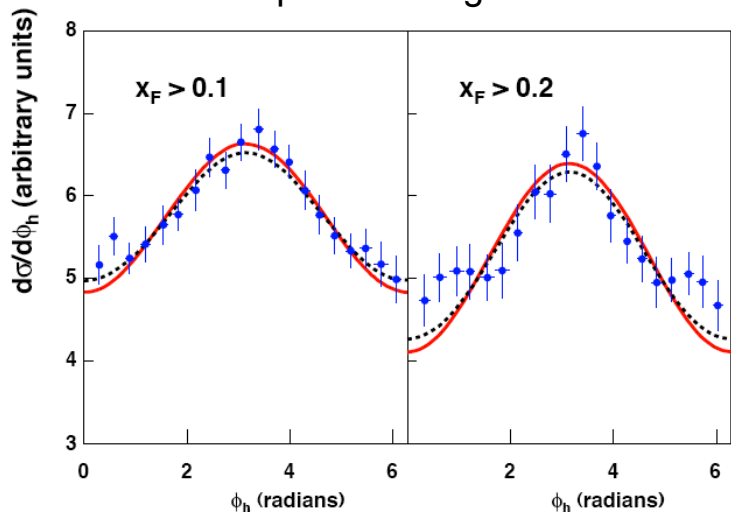
Cahn PLB 78 (1978)

Leading-twist contribution introduced
by Boer & Mulders in 1998

Boer & Mulders PRD 57 (1998)



Till 2008: qualitative agreement with Cahn expectations



- No hadron identification
- No charge separation
- Poor statistics for $\cos 2\phi$

The Lam-Tung relation

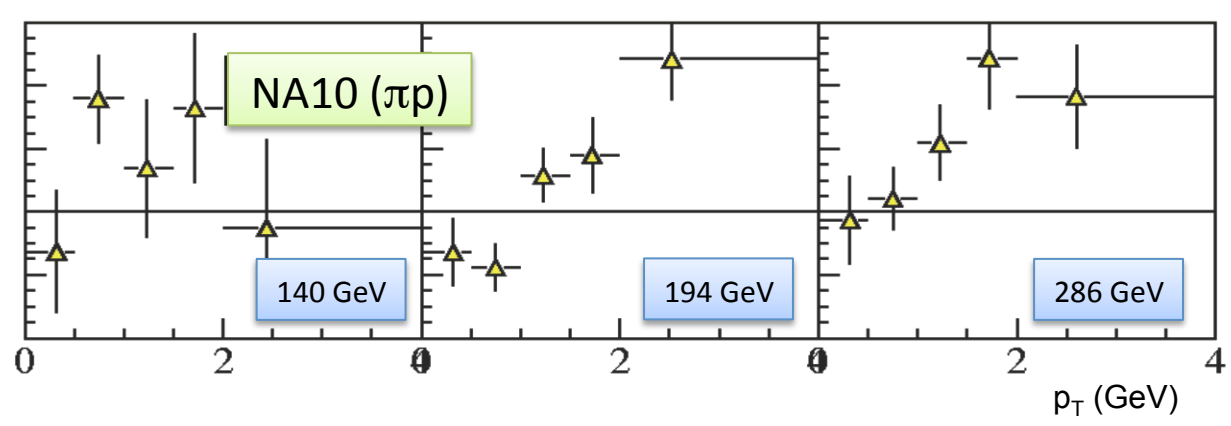
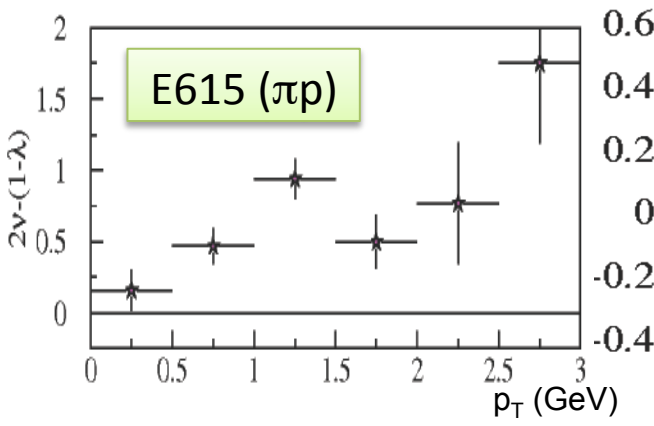
$$h_1^\perp \otimes h_1^\perp$$

$$\frac{d\sigma^{hp \rightarrow eeX}}{d\Omega} \propto 1 + \lambda \cos^2 \theta + \mu \sin 2\theta \cos \phi + \frac{\nu}{2} \sin^2 \theta \cos 2\phi$$

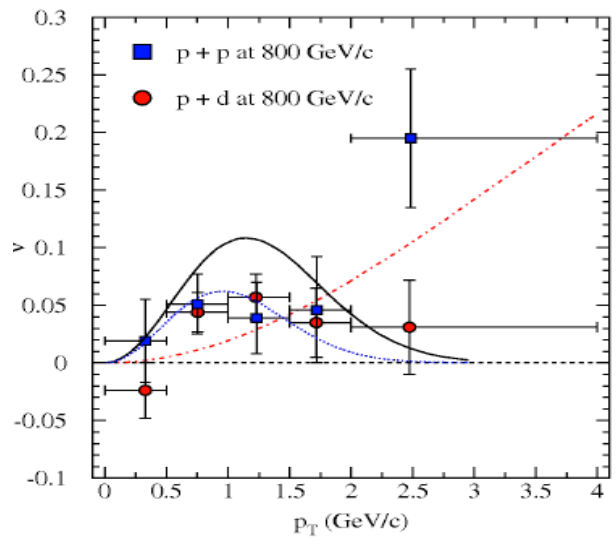
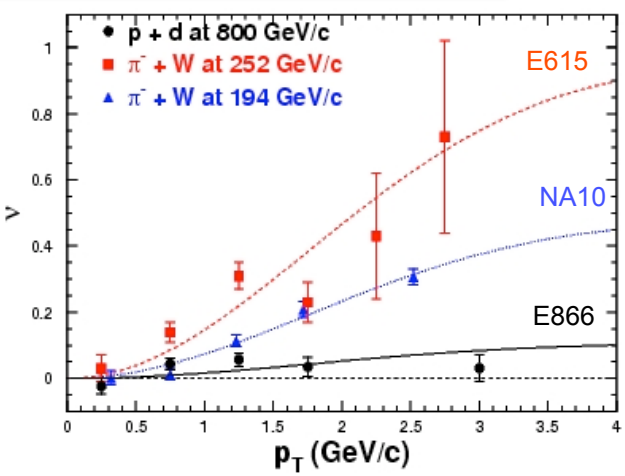
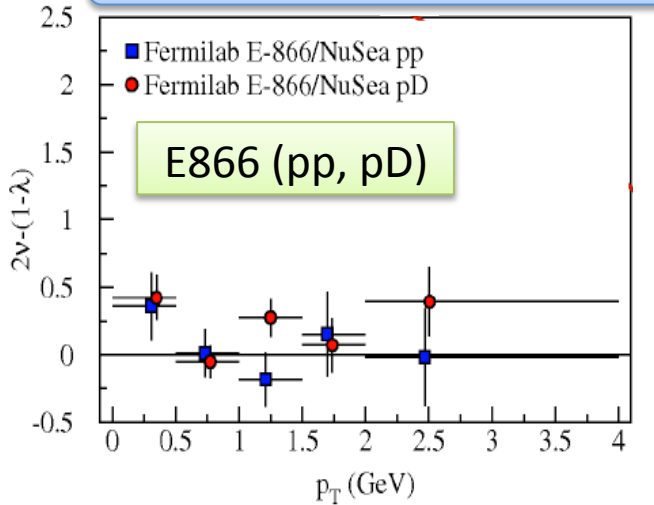
$$(1 - \lambda) = 2\nu$$

Preserved by NLO and resummation
Analogous of SIDIS Callan-Gross

$$h_1^\perp \otimes h_1^\perp$$



Boer-Mulders offers a possible explanation $\nu \approx h_{1q}^\perp \times h_{1\bar{q}}^\perp$



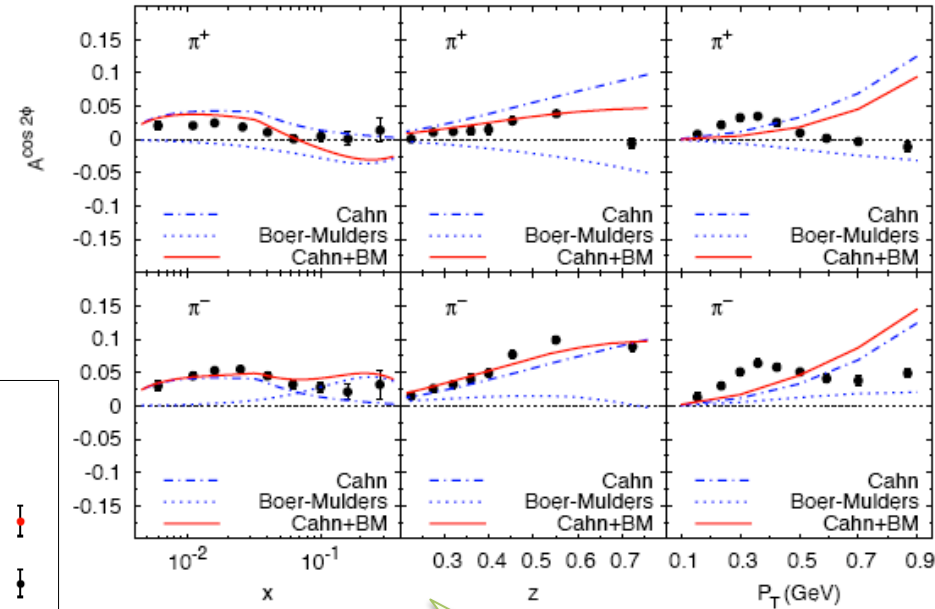
The SIDIS $\cos 2\phi$ dependence

$$h_1^\perp \otimes H_1^\perp$$

$$\sigma_{UU}^{\cos(2\phi)} \propto h_1^\perp \otimes H_1^\perp + [f_1 \otimes D_1 + \dots] / Q^2$$

Non-zero !

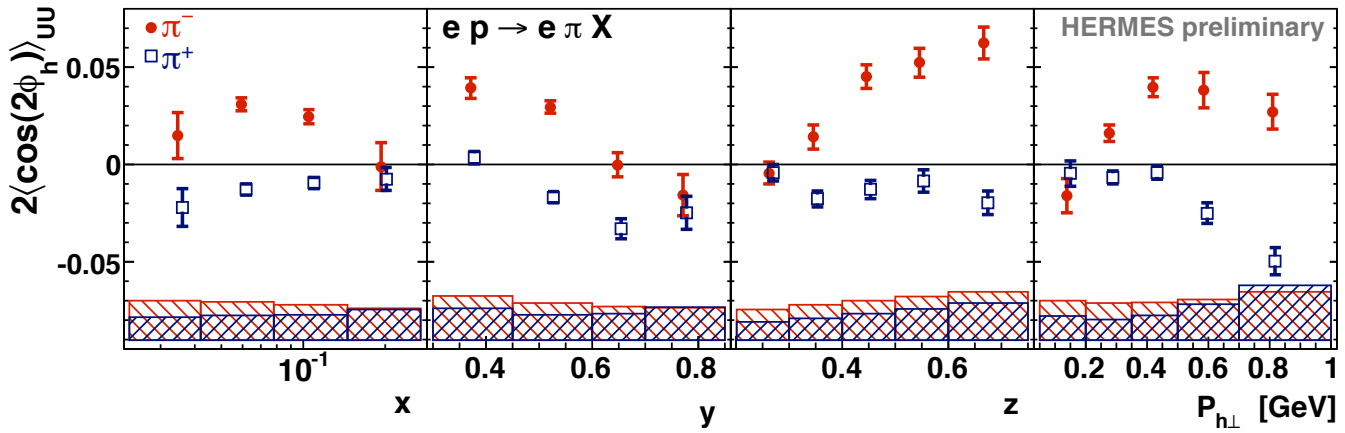
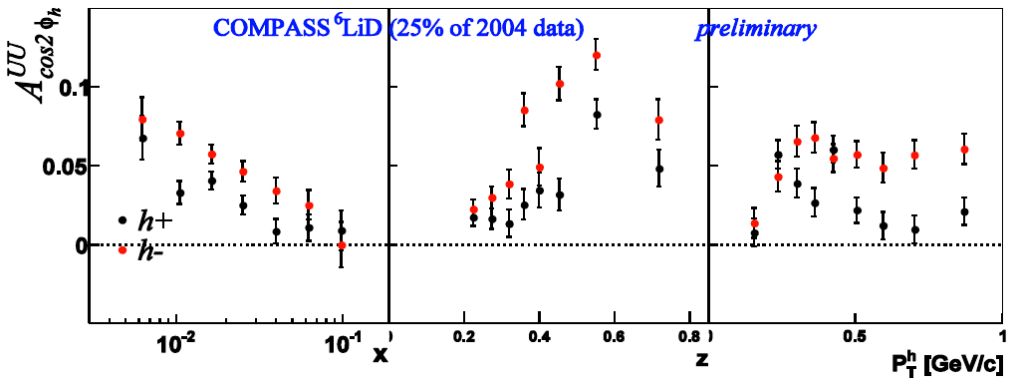
Issue on DATA consistency



arXiv: 0912.5194

Can be explained by large uncertainty on Cahn and neglected HT effects

arXiv: 1204.4161



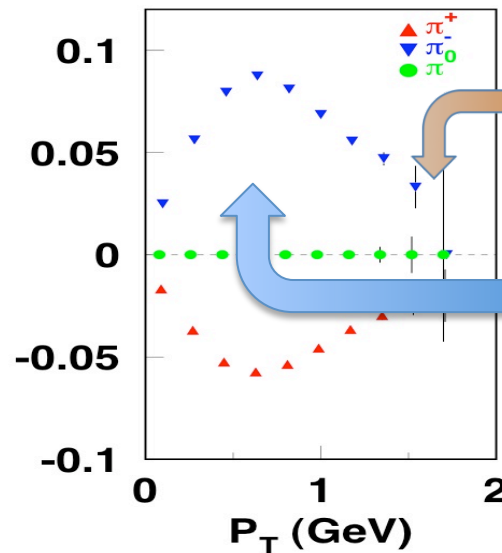
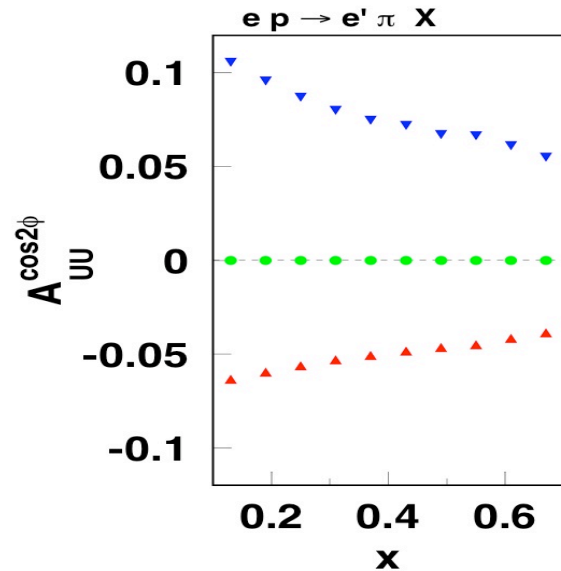
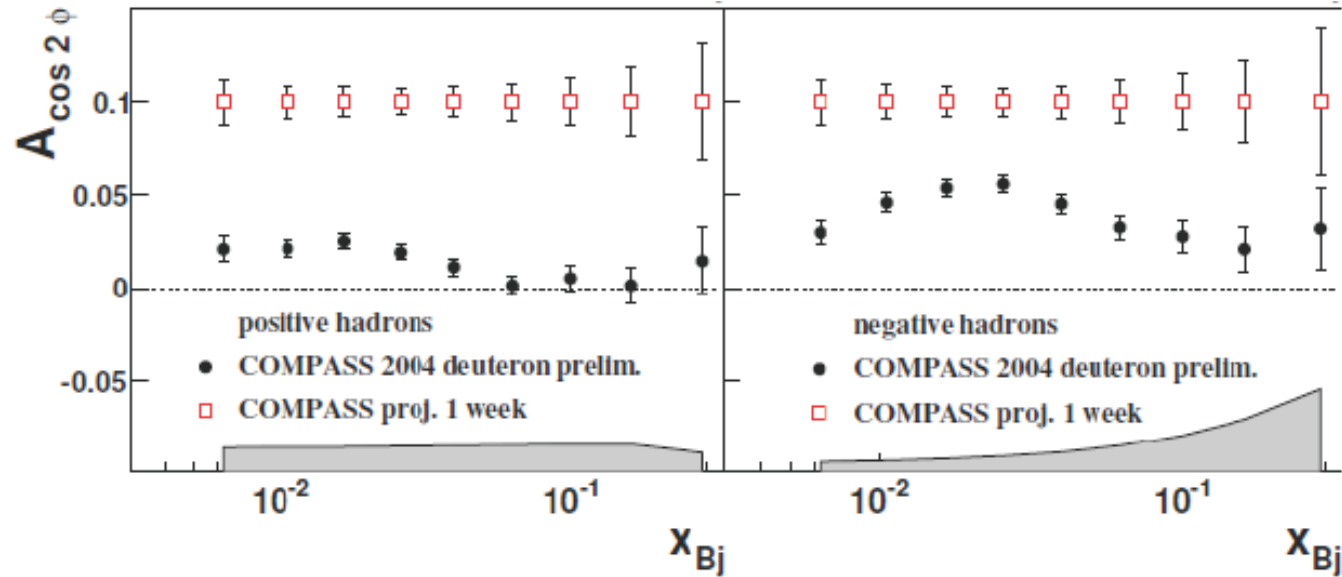
The SIDIS Landscape 2014+

COMPASS-II:

LH₂ target
160 GeV/c muons

CLAS12:

LH₂ target
12 GeV/c electrons
 $L \sim 10^{35} \text{ cm}^{-2}\text{s}^{-1}$



Perturbative region
Collinear factorization

Non-perturbative
TMD factorization

$$\Lambda_{\text{QCD}} \ll P_T \ll Q$$

The Drell-Yan Landscape 2014+

Proton beam @ Fermilab

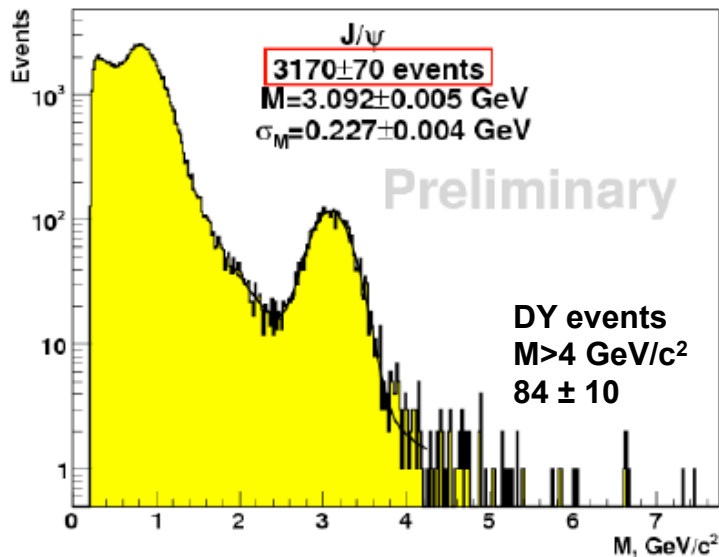
$$\left. \frac{\sigma^{pd}}{2\sigma^{pp}} \right|_{x_b \gg x_t} \approx \frac{1}{2} \left[1 + \frac{\bar{d}(x_t)}{\bar{u}(x_t)} \right]$$

E906: test run this year

Extends E866 measurements at 120 GeV
xsec scales as 1/s
background scales as s.

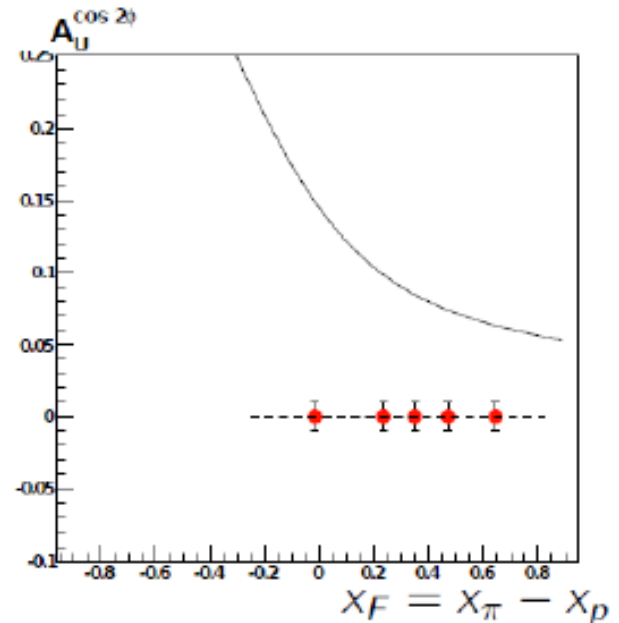
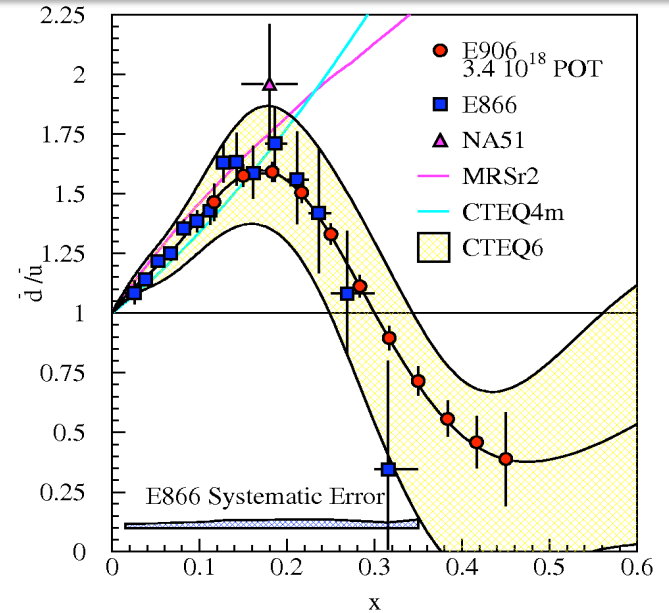
Pion beam @ CERN

2009 test



Boer-Mulders
⊗
Boer-Mulders

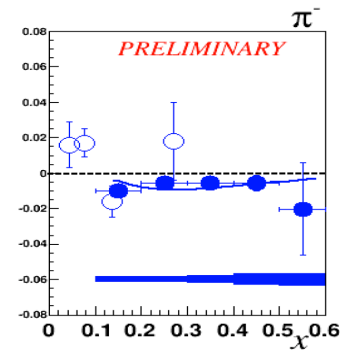
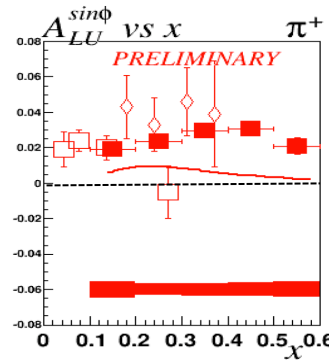
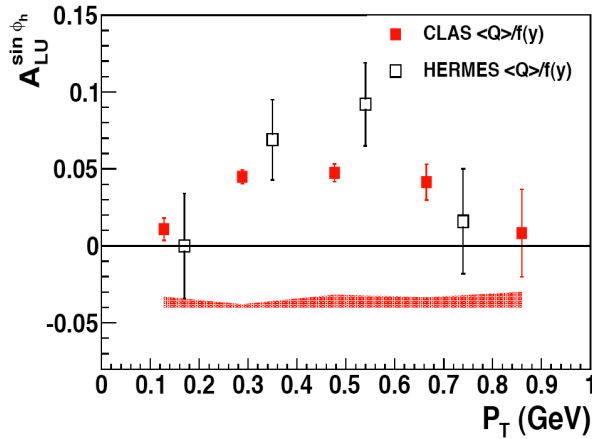
2 years
 $4 < M < 9 \text{ GeV}/c^2$



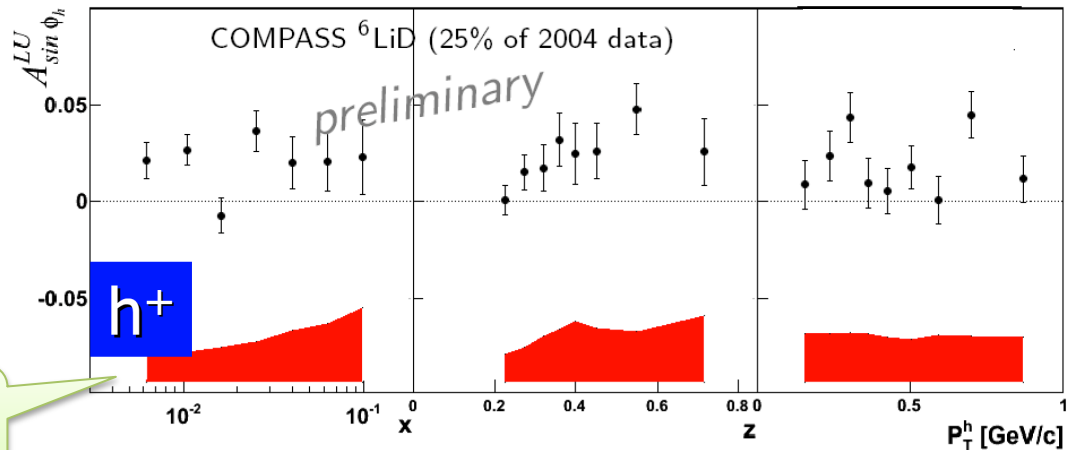
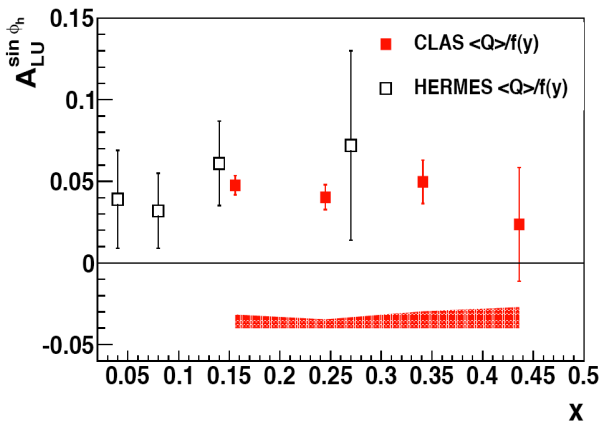
HIGHER TWISTS (THE SECOND LEVEL)

Higher-twist effects

$$\sigma_{LU}^{\sin(\phi)} \propto [e \otimes H_1^\perp + g^\perp \otimes D_1 + \dots] / Q$$



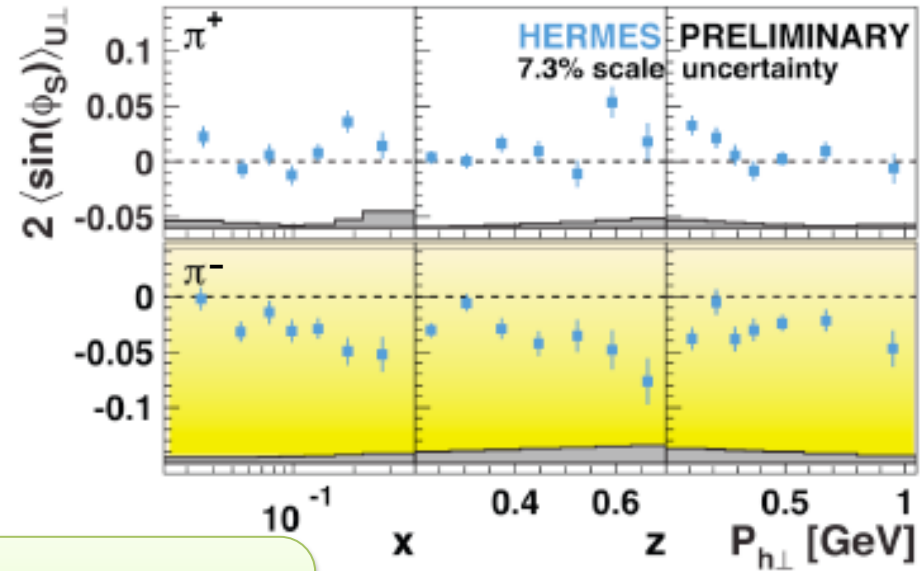
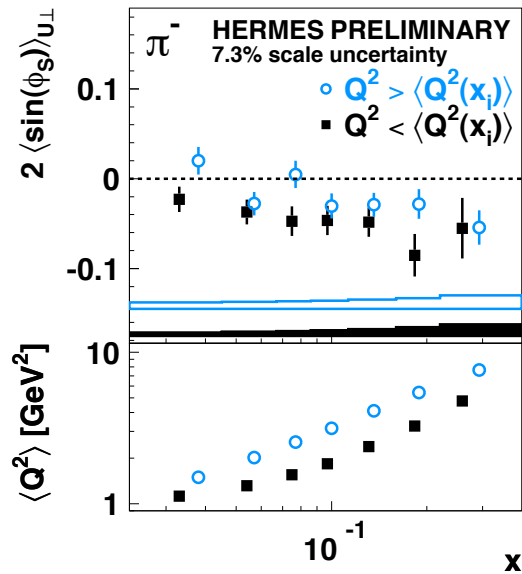
- π^- , e1f, preliminary
- π^+ , e1f, preliminary
- ◇ π^+ , CLAS e1c (2004)
- π^+ , HERMES (2007)
- ⊕ π^- , HERMES (2007)
- Model Prediction



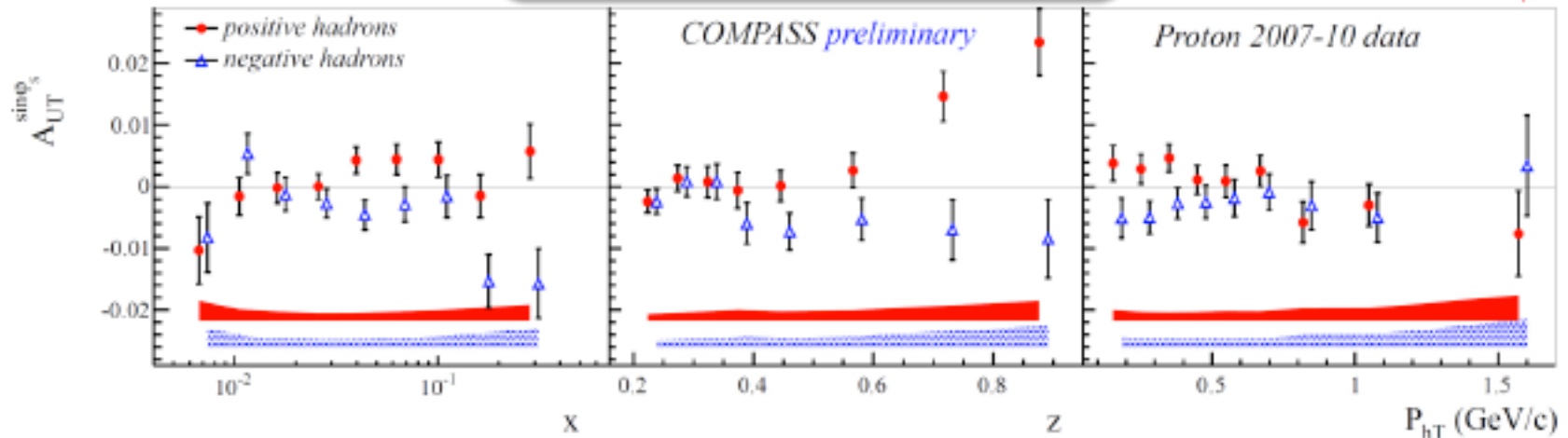
Non zero up to the COMPASS energies

Higher-twist effects

$$\sigma_{UT}^{\sin(\phi)} \propto [h_1 \otimes H_1^\perp + f_T \otimes D_1 + \dots] / Q$$



Similar pattern but different amplitude: visible effect of the different average Q^2 ?



Longitudinal Cross-section @ JLab12

$$\frac{d^5\sigma^{ep\rightarrow e'hX}}{dx dy dz d\phi dP_{h\perp}^2} \propto \{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos(\phi) F_{UU}^{\cos(\phi)} + \varepsilon s \cos(2\phi) F_{UU}^{\cos(2\phi)} \}$$

Knowledge on $R = \sigma_L/\sigma_T$
in SIDIS is non-existing!

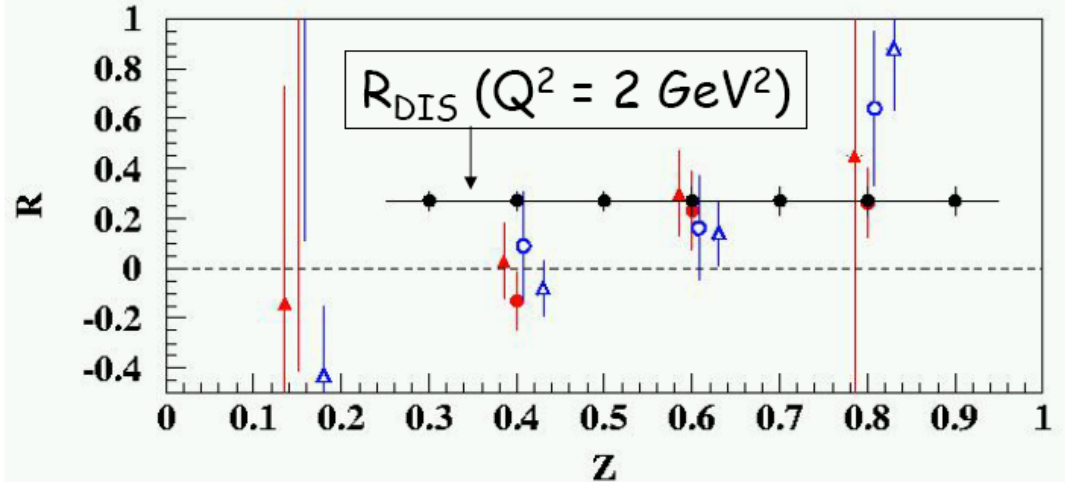
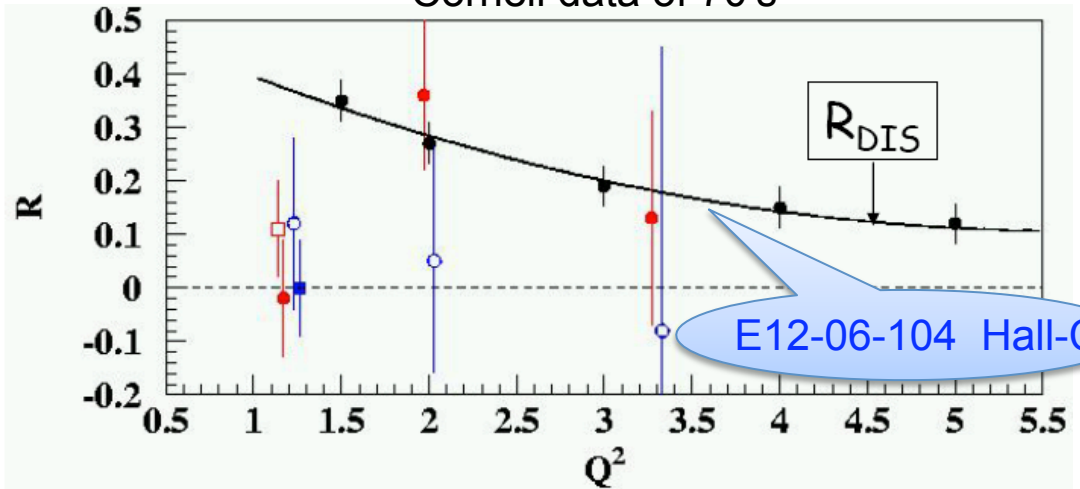
To be accounted in any TMD
asymmetry interpretation

$R_{DIS} \rightarrow 0$ at $Q^2 \rightarrow \infty$ due to
scattering off spin- $\frac{1}{2}$ quarks

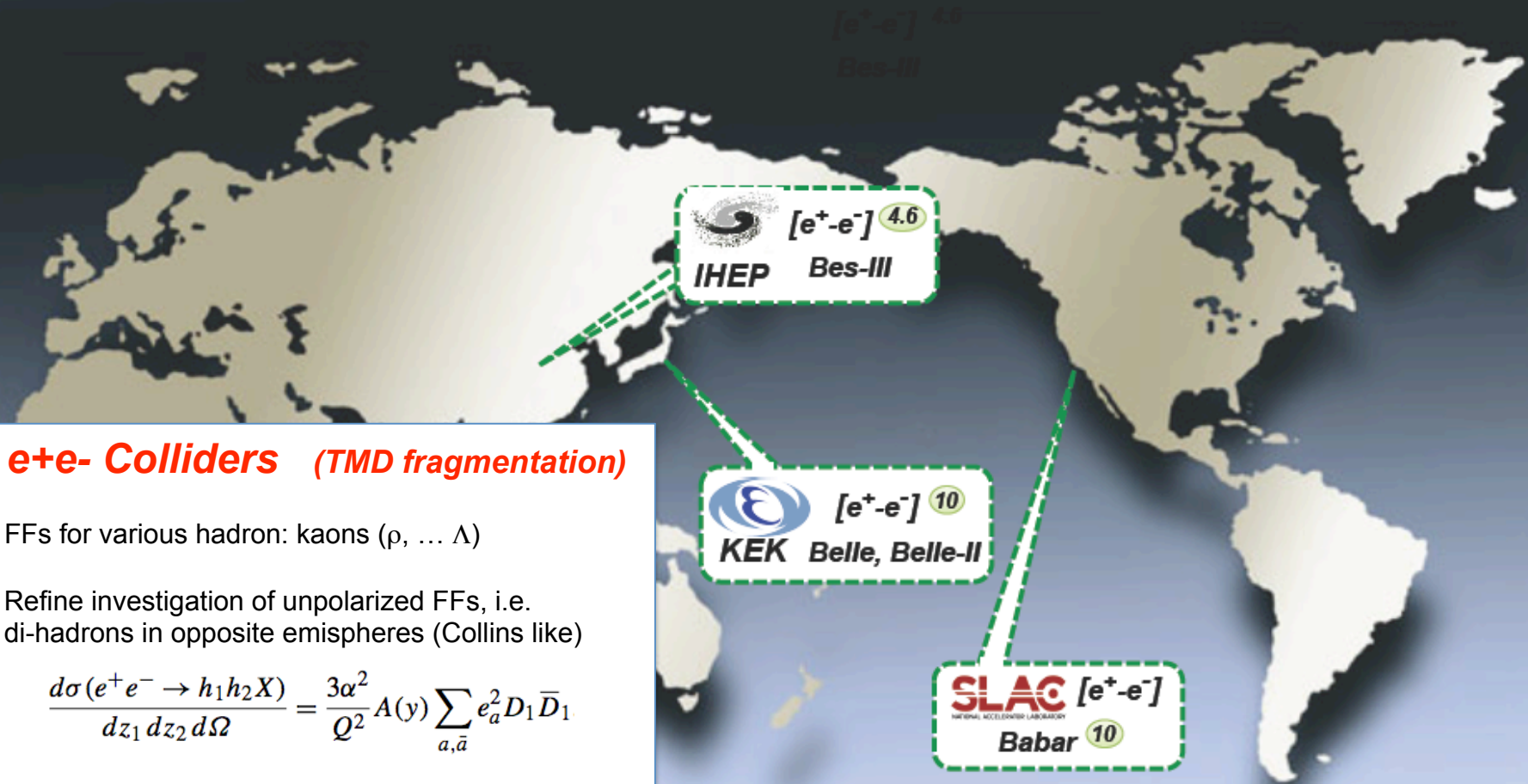
R_{DIS} sensitive to gluon and
higher-twist effects

$R_{SIDIS}(z, p_T) =$ un-integrated R_{DIS}

Cornell data of 70's



Higher-twist effects



e+e- Colliders (TMD fragmentation)

FFs for various hadron: kaons (ρ , ... Λ)

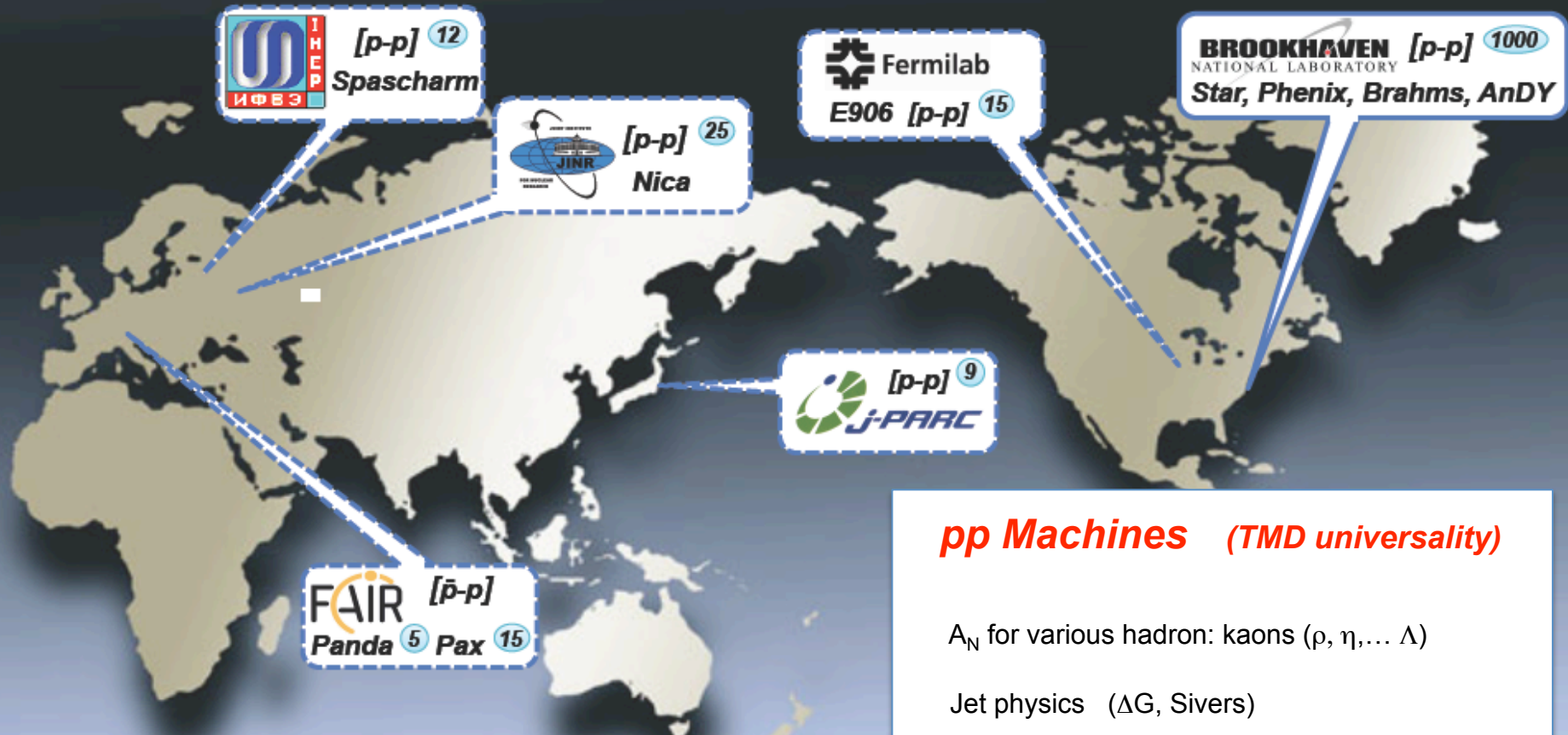
Refine investigation of unpolarized FFs, i.e. di-hadrons in opposite emispheres (Collins like)

$$\frac{d\sigma(e^+e^- \rightarrow h_1 h_2 X)}{dz_1 dz_2 d\Omega} = \frac{3\alpha^2}{Q^2} A(y) \sum_{a, \bar{a}} e_a^2 D_1 \bar{D}_1$$

Dependence on transverse momentum

Scale dependence: look for different c.m. energies (ISR, BESIII)

Higher-twist effects



pp Machines (TMD universality)

A_N for various hadron: kaons ($\rho, \eta, \dots \Lambda$)

Jet physics (ΔG , Siverts)

DY and gauge bosons (Δq , Siverts)

Di-hadron (Transversity)

Scale dependence

Higher-twist effects



DIS Experiments (TMD disentanglement)

Multidimensional analysis

Flavor separation: various hadron types and different targets

TMD formalism: di-hadron vs single-hadron h_1 extraction, inclusive SSA measurements

Scale dependence & Higher twists

A World-wide Challenge

