



Istituto Nazionale di Fisica Nucleare



European  
Commission



Korea Institute of  
Science and Technology Information

# TRILLION

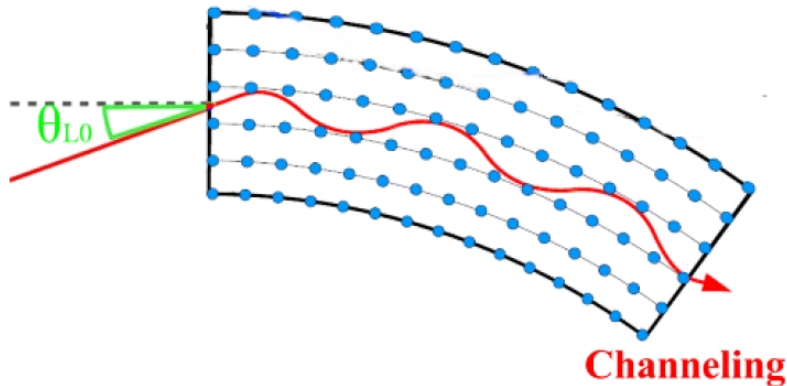
**Project TRILLION:  
Implementation of steering and radiation effects in  
oriented crystals and their applications into Geant4**

**Dr. Alexei Sytov**

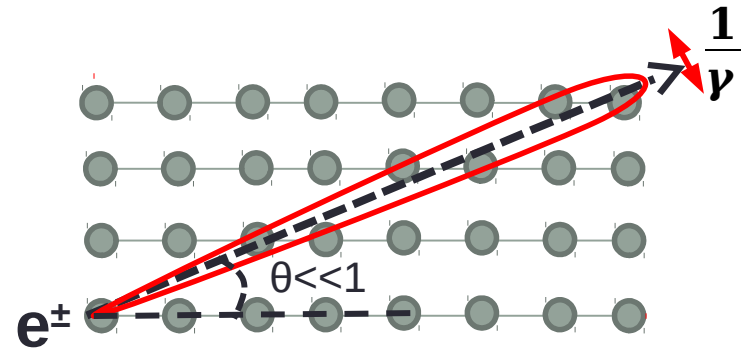
**KPS 70th Anniversary and 2022 Fall Meeting  
Busan, 2022/10/19**

# Coherent effects in a crystal

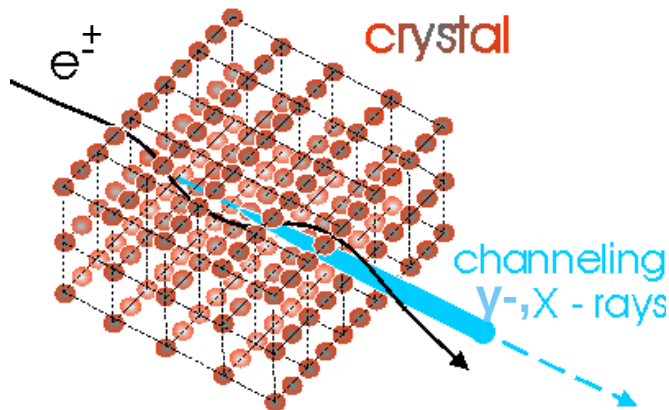
## Channeling\*



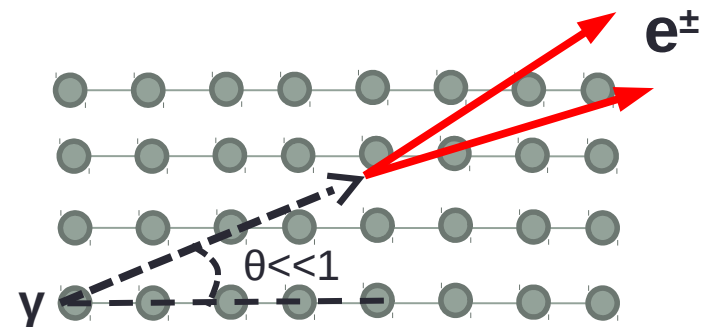
## Coherent bremsstrahlung\*\*\*



## Channeling radiation\*\*



## Coherent pair production\*\*\*\*



\*J. Stark, Zs. Phys. 13, 973–977 (1912); J. A. Davies, J. Friesen, J. D. McIntyre, Can J. Chem. 38, 1526–1534 (1960)

\*\*M.A. Kumakhov, Phys. Lett. A 57(1), 17–18 (1976)

\*\*\*B. Ferretti, Nuovo Cimento 7, 118 (1950); M. Ter-Mikaelian, Sov. Phys. JETP 25, 296 (1953).

\*\*\*\* H. Überall, Phys. Rev. 103, 1055 (1956).

# Marie Skłodowska-Curie Action Global Individual Fellowships by A. Sytov in 2021-2024, Project TRILLION GA n. 101032975

**Main goal:** The **implementation** of both physics of **electromagnetic processes in oriented crystals** and the design of specific applications of crystalline effects into **Geant4** simulation toolkit as Extended Examples to bring them to a large scientific and industrial community and under a free Geant4 license.

## Group:

- **A. Sytov** – project coordinator
- **L. Bandiera** – INFN supervisor
- **K. Cho** – KISTI supervisor
- **G. Kube** – DESY supervisor
- **I. Chaikovska** – IJCLab Orsay supervisor

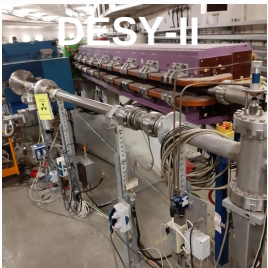
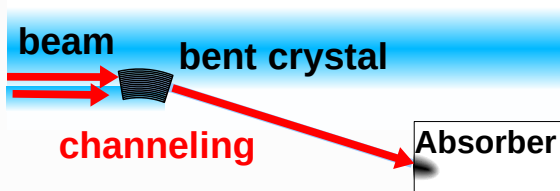


## Location:

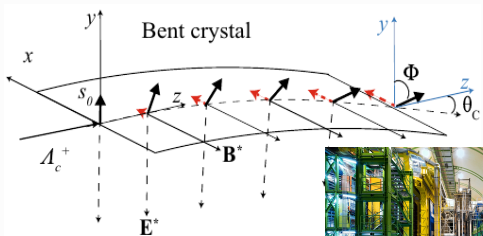
- 2 years at **KISTI** (partner organization)
- 1 year at **INFN Section of Ferrara** (host organization)
- 1 month of secondment at **DESY** (partner organization)
- 1 month of secondment at **IJCLab Orsay** (partner organization)

# Applications\*

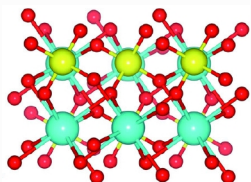
Crystal-based collimation  
or beam extraction from an  
accelerator



Measurement of dipole  
magnetic and electric  
moments of exotic particles



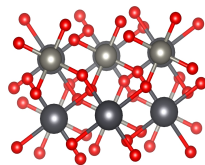
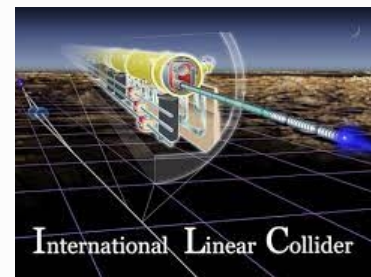
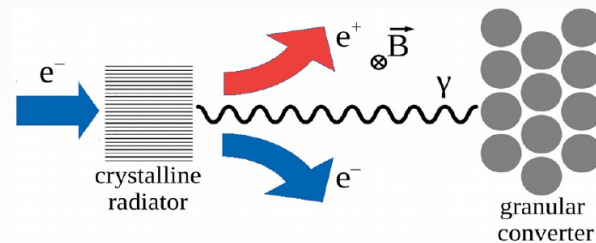
Ultrashort  
crystalline  
calorimeter



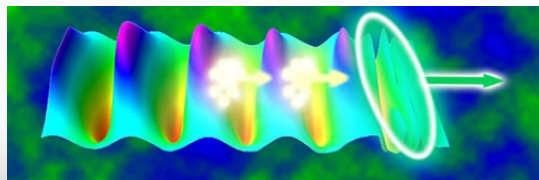
Gamma-ray  
Space Telescope



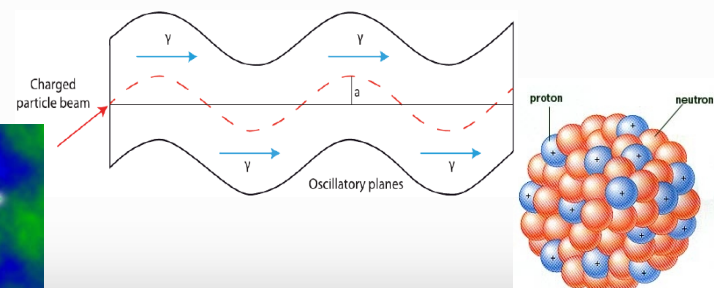
Positron source for future  
 $e^+/e^-$  and muon colliders



Plasma acceleration



X and  $\gamma$ -ray source for  
nuclear and medical physics



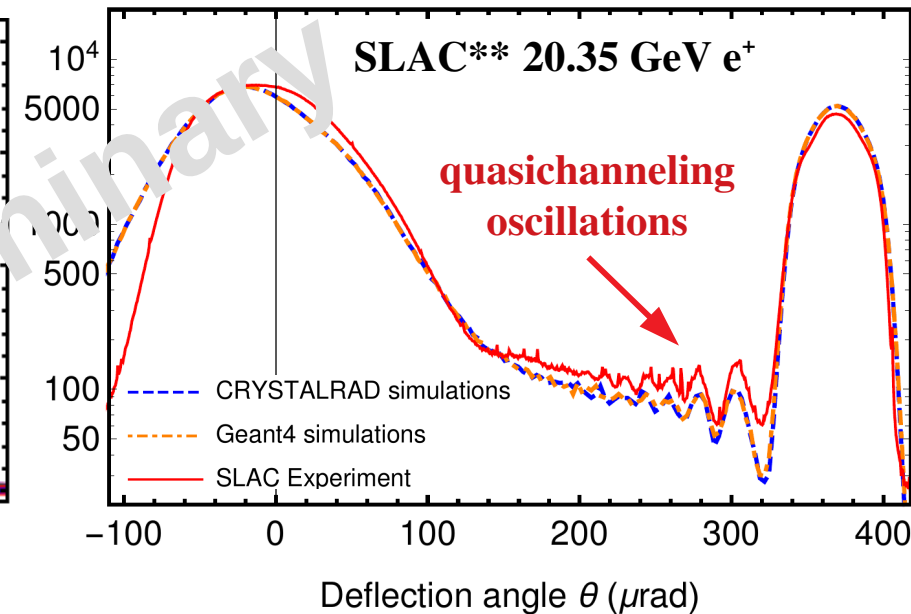
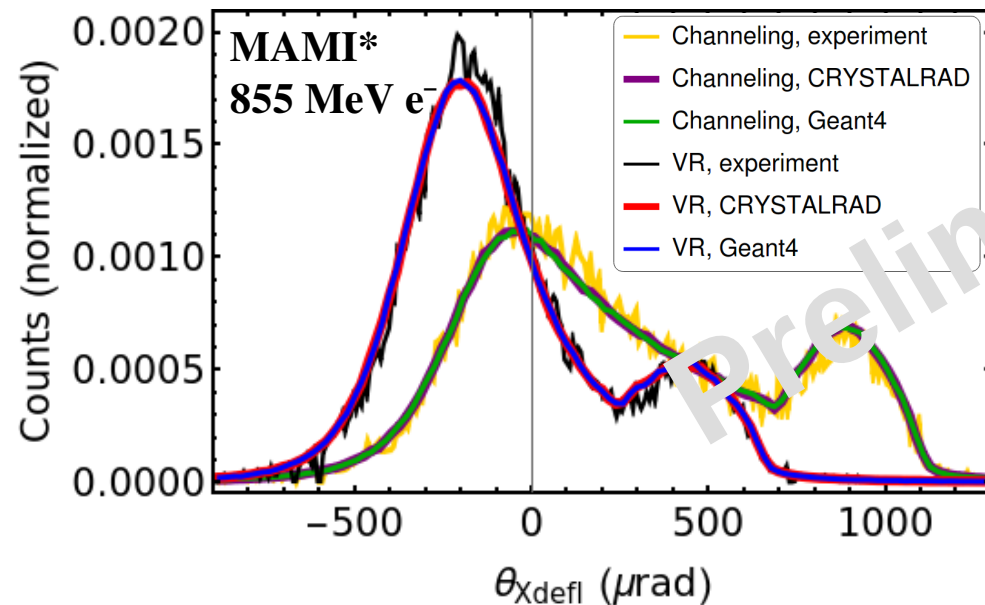
# The first step of TRILLION: Geant4 simulations of beam deflection by a bent crystal



Korea Institute of  
Science and Technology Information



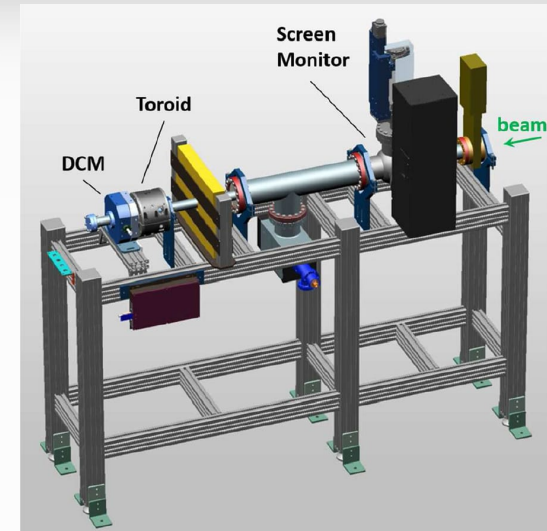
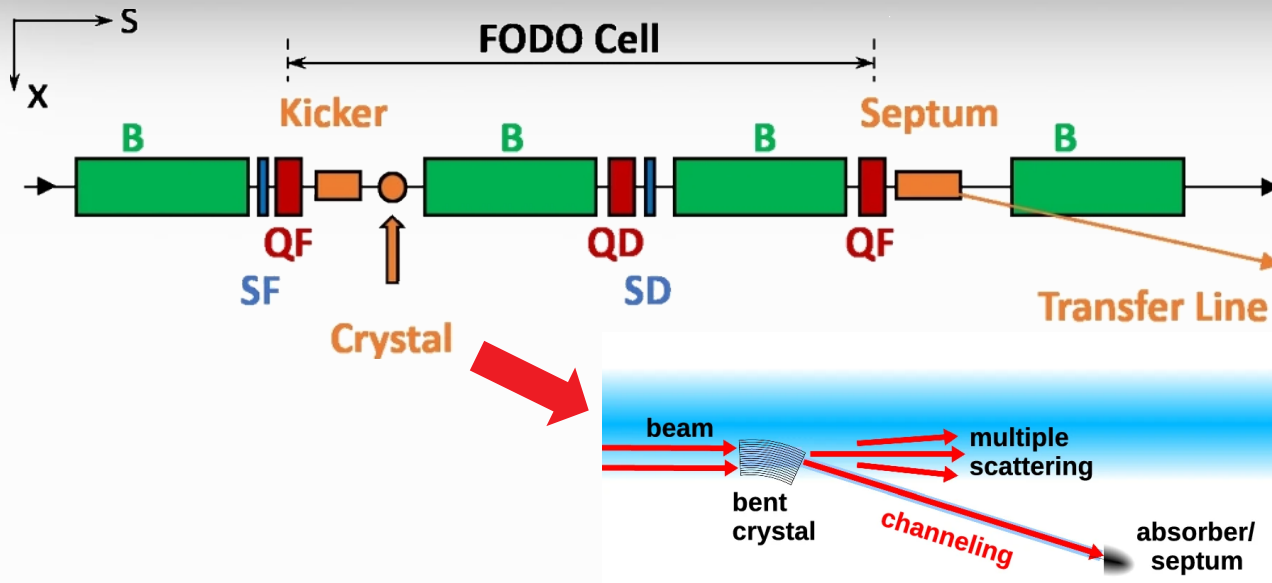
## Geant simulations vs experiment and CRYSTALRAD simulations



\*A. Mazzolari et al. Phys. Rev. Lett. 112, 135503 (2014)

\*\*T. N. Wistisen, ..., and A. Sytov. Phys. Rev. Lett. 119, 024801 (2017)

# Crystal-based extraction: possible setup at DESY-II



Crystal-based beam extraction: applied only for protons,  
never applied for electrons

## Advantages:

- Extraction of **primary** low-emittance and very **intense electron beam** in a **parasitic mode**.
- The **extraction line** including septum magnets already **exists** => **ideal for prove-of-principle**
- Few GeV electron beam, **typical for electron synchrotrons** existing in the world.

## Can be applied at:

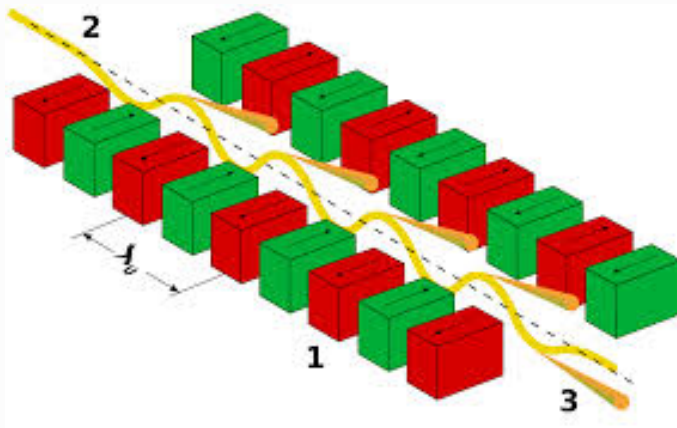
- DESY-II and any e-/e+ synchrotron or a **synchrotron light source**

Have been already applied at:

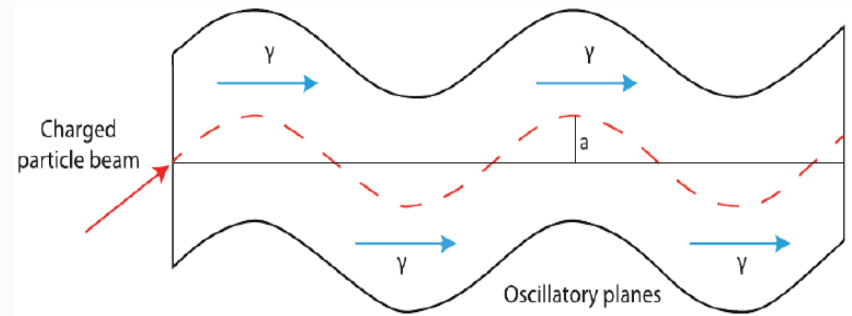
- **LHC, Tevatron, SPS, RHIC, U-70**

# Channeling radiation in a bent crystal: Crystalline undulator

Classical scheme: magnetic undulator in a free electron laser  
laser **soft X-rays**  $\lambda_u \sim \text{cm}$



Innovative scheme: Crystalline undulator  $\rightarrow$  **Hard X-rays and gamma rays**  
 $\lambda_u < \text{mm}$



## Advantage:

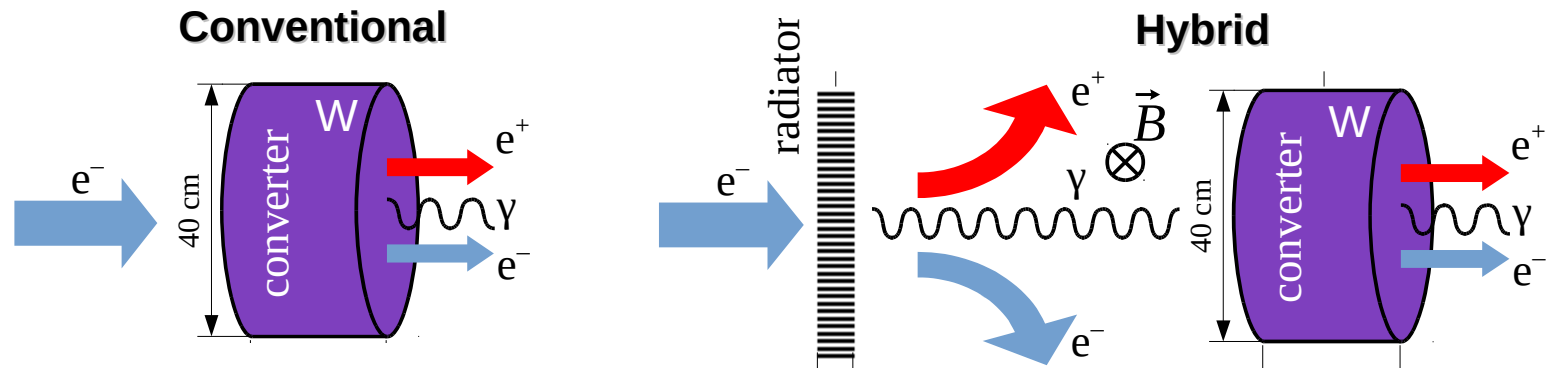
- Intense X- and gamma-rays produced in a crystal, in a compact piece of material

Crystalline X and gamma-ray source **can be applied** in:

- **Nuclear physics**
- **Medical physics**

 EU project MSCA RISE N-LIGHT G. A. 872196  
Coordinator MBN RESEARCH CENTER (Germany)

# Crystal-based hybrid positron source\*



**Coherent effects in a crystal accelerate electromagnetic shower development**

## Coherent effects of e.m. shower in a crystal:

- Channeling radiation/coherent bremsstrahlung
- Coherent pair production

## Advantages of the hybrid positron source:

- **Higher** positron yield
- Considerably lower peak deposited energy inside the target => **higher beam intensities, longer target lifetime**

## Hybrid positron source can be applied at:

- FCC-ee
- ILC
- Muon collider



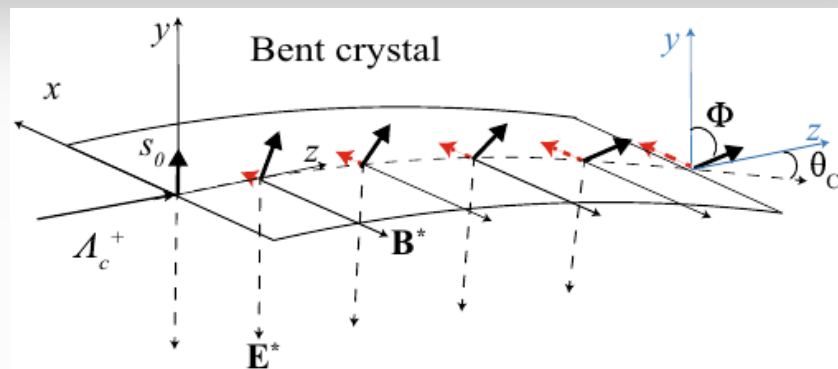
**Simulation model can be also applied for ultrashort crystalline calorimeter**



# Search of MDM&EDM of short living particles using the effect of spin rotation in oriented crystals\*

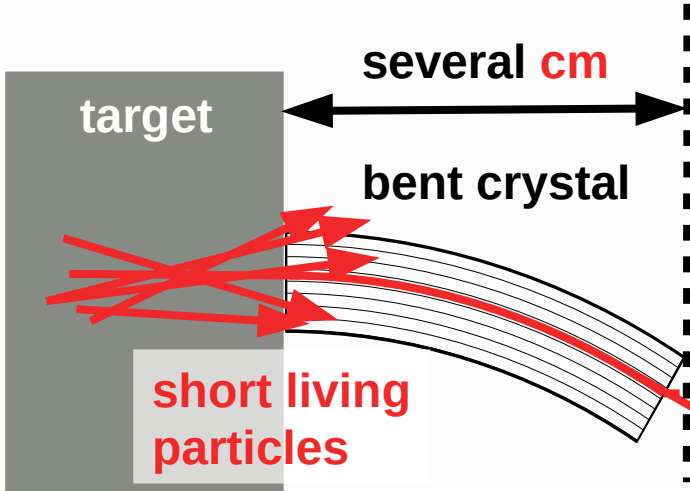
What we want:

- To measure **MDM** and **EDM** of exotic baryons



Experimental proof at Tevatron for  $\Sigma^{+**}$

HE beam (e.g. 7 TeV protons)



Crystal thickness must be comparable with the life distance of the particle

Possible particles:  
 $\Lambda_c^+, \Xi_c^+, \dots, \tau$

Detector (e.g. LHCb)  
polarization measurement

\* V. G. Baryshevskii, Pis'ma Zh. Tekh. Fiz. 5, 182 (1979)

\*\*D. Chen et al. (E761 Collaboration) Phys. Rev. Lett. 69, 23 (1992)

# Plasma wake-field acceleration in oriented crystals\*

$$E[\text{GV/m}] = m_e \omega_p c / e \approx 100 \sqrt{n_0 [10^{18} \text{cm}^{-3}]}$$

**Acceleration  
gradient:**

1-10 TeV/m

Considerably **higher electron density** in a **solid state** than in a gaseous plasma

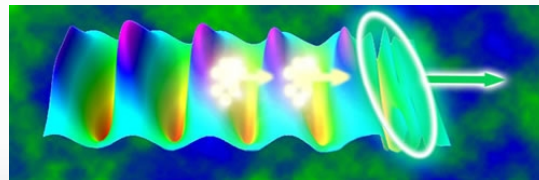
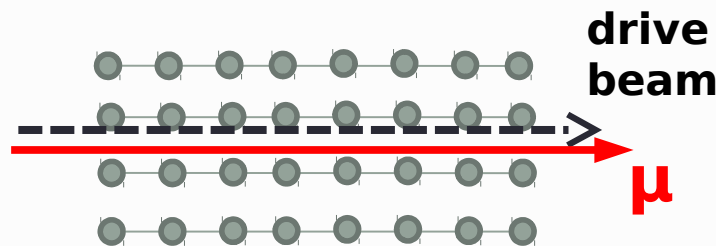
**Channeling** makes crystal almost **transparent** both to accelerated and to drive beam

**Possible drive beam:**

- X-rays
- electrons
- heavy high-Z beams

**Possible accelerated beam:**

- **muons**
- e+/e-
- protons

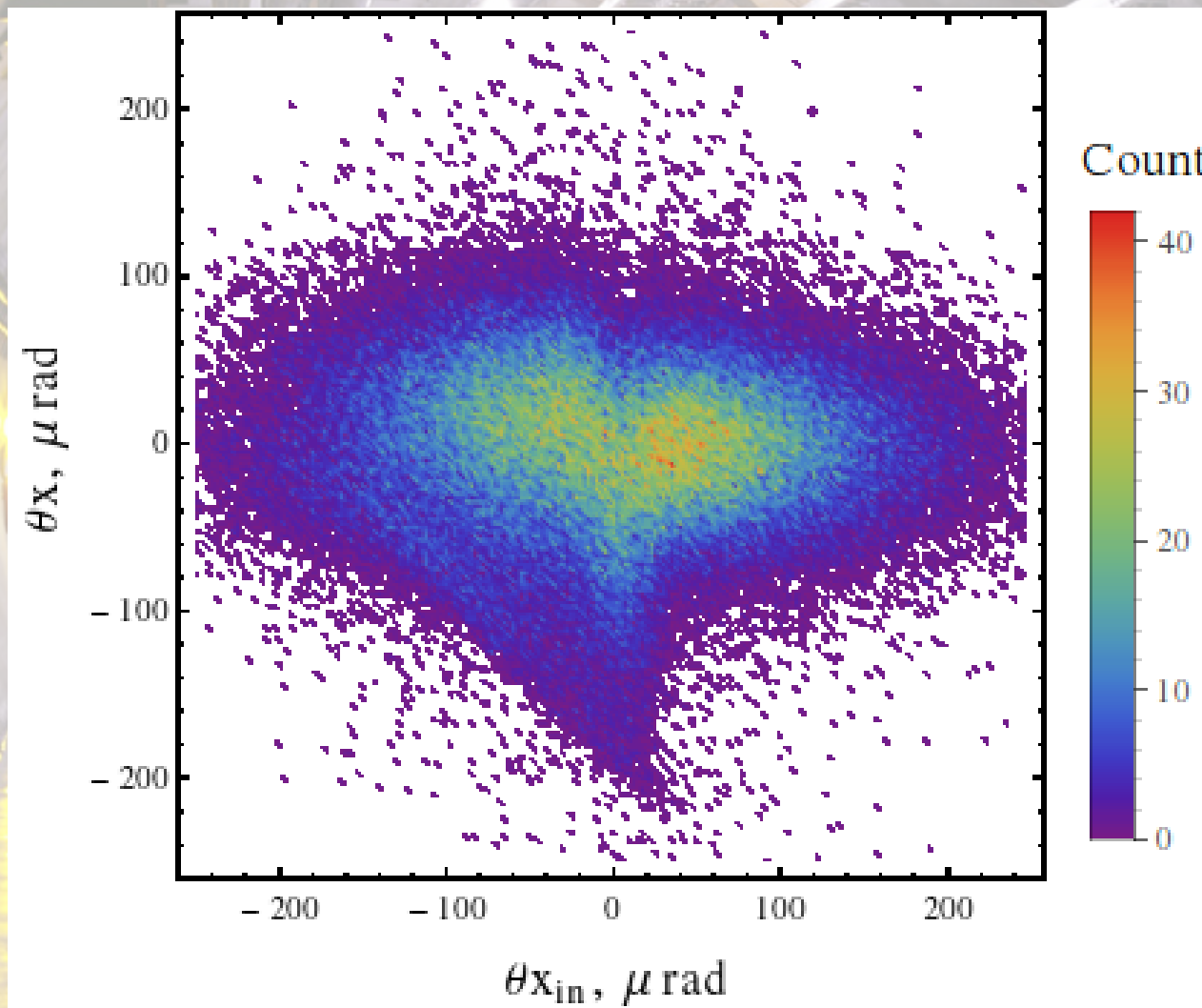


**Compact muon collider?**

\* R. Ariniello, ..., and T. Tajima, **Snowmass**'2021 AF6: Advanced Acceleration Concepts, arXiv: 2203.07459

# Conclusions

- The goal of **TRILLION** is to implement **electromagnetic processes in oriented crystals** into **Geant4** which will bring most of possible applications of a crystal to a large scientific and industrial community.
- The Geant4 examples that will be developed can be **applied** in **nuclear and medical physics** (radiation source), at e-/e+ colliders – **ILC, FCC-ee** and **muon collider** (positron source) and at all **e-/e+ synchrotrons** existing in the world (crystal-based beam extraction).
- Additional applications can be applied in **detector physics** (crystalline ultrashort calorimeter), **particle physics** (magnetic and electric dipole measurement) and **innovative accelerator physics** (plasma acceleration).



**Thank you for attention!**

# Solution: Geant4 FastSim interface

A. Sytov thanks **Prof. Vladimir Ivanchenko** (CERN) for this solution and the group of **Prof. P. Cirrone** (INFN LNS), in particular **Dr. L. Pandola** for fruitful discussions!

## FastSim model:

- **Physics list independent**
- Declared in the **DetectorConstruction**
- Is activated only in a **certain G4Region** at a **certain condition** and only for **certain particles**
- **Stops Geant processes** until the exit from the model and then resumes them

Baseline simulation code: **CRYSTALRAD\***

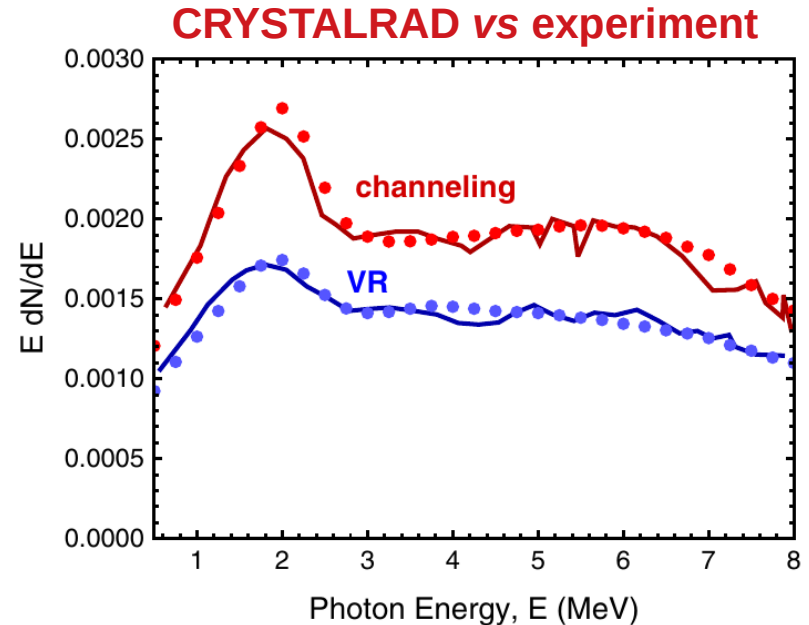
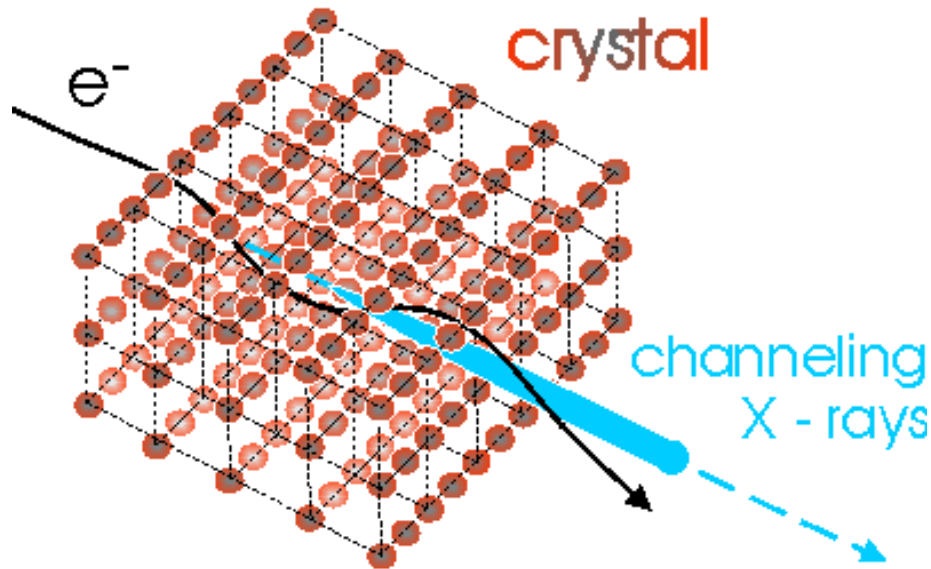
```
71  G4bool TestModel::IsApplicable(const G4ParticleDefinition& particleType)
72  {
73      return
74          &particleType == G4Proton::ProtonDefinition() ||
75          &particleType == G4AntiProton::AntiProtonDefinition() ||
76          &particleType == G4Electron::ElectronDefinition() ||
77          &particleType == G4Positron::PositronDefinition(); // ||
78          //&particleType == G4Gamma::GammaDefinition();
79  }
80
81  //.....ooo00000ooo.....ooo00000ooo.....ooo00000ooo.....ooo00000ooo.....
82
83  G4bool TestModel::ModelTrigger(const G4FastTrack& fastTrack)
84  {
102 }
103
104 //.....ooo00000ooo.....ooo00000ooo.....ooo00000ooo.....ooo00000ooo.....
105
106 void TestModel::DoIt(const G4FastTrack& fastTrack,
107                     G4FastStep& fastStep)
108 {
109 |
```

Insert particles for which the model is applicable

Insert the condition to enter the model

Insert what the model does

# Baier-Katkov algorithm from CRYSTALRAD



## Baier-Katkov formula:

integration is made over the classical trajectory

$$\frac{dE}{d^3k} = \omega \frac{dN}{d^3k} \frac{\alpha}{4\pi^2} \iint dt_1 dt_2 \frac{[(E^2 + E'^2)(v_1 v_2 - 1) + \omega^2 / \gamma^2]}{2E'^2} e^{-ik'(x_1 - x_2)}$$

The **Baier-Katkov** method permits to simulate the emitted radiation in crystals in a wide energy range, from **sub-GeV** to **hundreds of GeV**.

\*L. Bandiera, et al., Nucl. Instrum. Methods Phys. Res., Sect. B 355, 44 (2015)

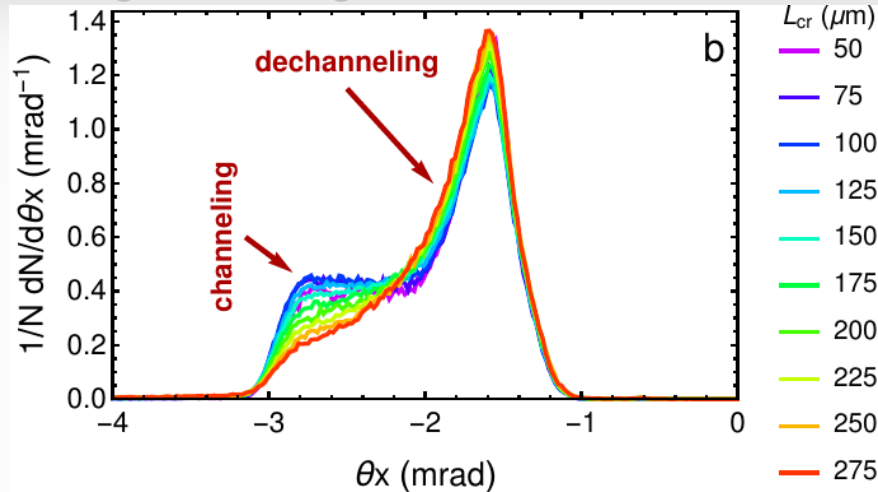
\*\*V.N. Baier, V.M. Katkov, V.M. Strakhovenko World Scientific, Singapore (1998)

\*\*\*V. Guidi, L. Bandiera, V. Tikhomirov, Phys. Rev. A 86 (2012) 042903

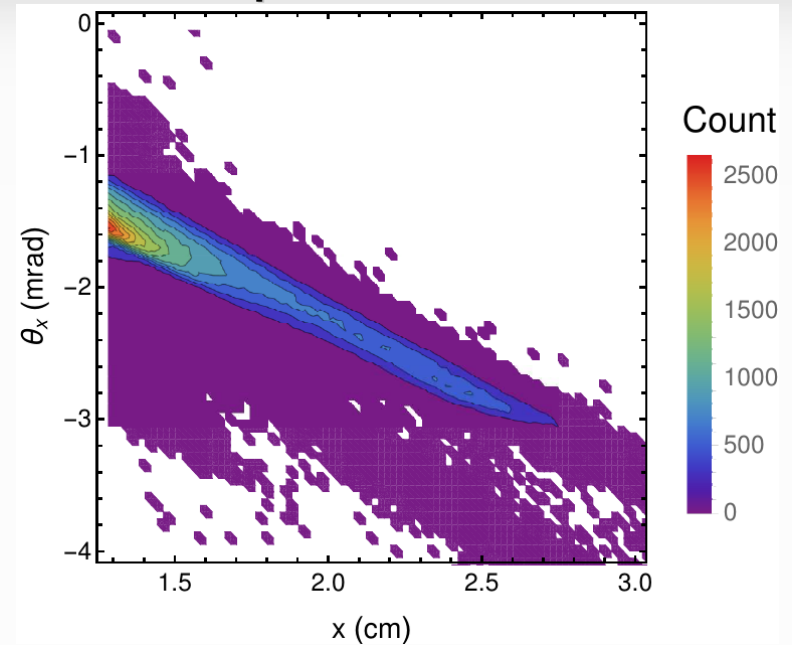
\*\*\*\*A. I. Sytov, V. V. Tikhomirov, and L. Bandiera. PRAB 22, 064601 (2019)

# Crystal-based extraction: CRYSTALRAD simulation results

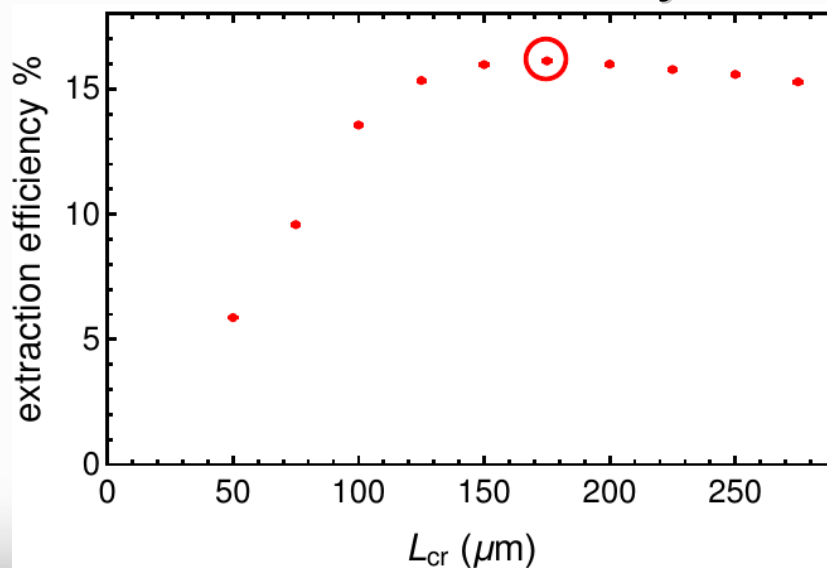
## Angular divergence of extracted beam



## Phase space of extracted beam



## Extraction efficiency



## Crystal parameters:

- Si (111)
- bending angle **1.75 mrad**
- Crystal length **0.175 mm**
- Crystal transverse thickness **1 cm**

**Maximal extraction efficiency:**  
**16.1 %**