



# ELECTROWEAK VACUUM

## LECTURE 4: BEYOND THE STANDARD MODEL

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The outline of Lecture 4 is

## Beyond the Standard Model

- ▶ UV sensitivity of EW vacuum
- ▶ Supersymmetry (MSSM)
- ▶ Little Higgs (LH)
- ▶ Gauge-Higgs Unification (GHU)
- ▶ Warped models
  - ▶ Randall-Sundrum model (RS)
  - ▶ Soft Wall models (SW)
  - ▶ Custodial models (dual to composite Higgs)
- ▶ Conclusion

## Drawbacks of SM

- ▶ **Big Hierarchy problem:** The Higgs mass is **sensitive to UV** physics. Quantum corrections are UV sensitive

$$\Delta m_H^2(F, B) = \mp \frac{n_{F,B} g_{F,B}^2}{16\pi^2} \Lambda^2$$

They are not protected by any symmetry which is enhanced when  $m_H = 0$

- ▶ On the contrary fermions masses

$$\Delta m_F \propto \frac{m_F}{16\pi^2} \log \Lambda$$

are protected by chiral symmetry for  $m_F = 0$

- ▶ Electroweak symmetry breaking requires a **tachyonic mass** for the Higgs
- ▶ **Dark Matter:** there is no candidate
- ▶ There is no gauge coupling **unification**
- ▶ Strong CP-problem: **axion** required

## The Little Hierarchy Problem and LEP paradox

- ▶ The leading quantum correction to the Higgs mass parameter is expected to come from the top sector as

$$\Delta m_H^2 = -\frac{3h_t^2}{8\pi^2}\Lambda^2$$

- ▶ In the absence of tuning this implies a lower bound on the cutoff scale as

$$\Lambda < 600 \text{ GeV} \left( \frac{m_H}{200 \text{ GeV}} \right) \simeq 400 \text{ GeV}$$

- ▶ Why did LEP2 not detect any deviation from the SM predictions? (**Barbieri's LEP paradox**)
- ▶ In particular one can parametrize the new effects as non-renormalizable operators ( $d = 6$ )

$$\mathcal{L}_{\text{eff}} = \frac{c_1}{\Lambda^2} (\bar{e}\gamma^\mu e)^2 + \dots$$

- ▶ If  $c_i = \mathcal{O}(1) \Rightarrow \Lambda > 10 \text{ TeV} \Rightarrow$  tension

Possible solutions to the Higgs hierarchy problems are motivating the presence of New Physics

### Possible solutions $\Leftrightarrow$ New Physics

- ▶ **Supersymmetry**: bosonic (fermionic) partners cancel the quadratic divergences produced by fermions (bosons)
- ▶ Higgs as **pseudo Goldstone boson**: **little Higgs** theories and **gauge-Higgs** unification in higher dimensions
- ▶ **Higgs as a condensate** that “dissolves” at high energies  $\Rightarrow$  strongly interacting gauge sector at TeV scales: **technicolor**, **holographic Higgs**, **warped extra dimensions**

## Minimal Supersymmetric Extension of the Standard Model

### Higgs sector

- ▶ An **extended Higgs** sector

$$H_1 = \begin{pmatrix} H_1^0 \\ H_1^- \end{pmatrix}_{-1/2}, \quad H_2 = \begin{pmatrix} H_2^+ \\ H_2^0 \end{pmatrix}_{1/2}$$

- ▶ After the Higgs mechanism  $\langle H_1^0 \rangle = v_1$ ,  $\langle H_2^0 \rangle = v_2$ ,  $\tan \beta = v_2/v_1$  there are **five Higgses** left: two scalar ( $h, H$ ), one pseudoscalar ( $A$ ) and two charged ( $H^\pm$ )
- ▶ Supersymmetry has to be broken, e.g. by embedding the MSSM into a local supersymmetry
- ▶ The Higgs spectrum is determined by two free parameters:  $m_A$  and  $\tan \beta$

$$m_{H^\pm}^2 = m_A^2 + M_W^2, \quad m_{h,H}^2 =$$

$$\frac{1}{2} \left[ m_A^2 + M_Z^2 \mp \sqrt{(m_A^2 + M_Z^2)^2 - 4m_A^2 M_Z^2 \cos^2 2\beta} \right]$$

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UV sensitivity of the electroweak vacuum

MSSM

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Pre-LHC plots  
Post-LHC plots  
Drawbacks of the MSSM

Little Higgs

Gauge-Higgs unification

Warped models

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## It solves the Big Hierarchy problem

- ▶ Because quantum corrections to the Higgs mass from bosonic loops have *opposite* signs to fermionic loops there is a **cancellation between supersymmetric partners**. **Supersymmetry protects the Higgs mass!**
- ▶ When supersymmetry is broken by *soft* terms the supersymmetric cancellation holds up to supersymmetry breaking terms
- ▶ Quadratic divergences are still absent
- ▶ Hierarchy problem is *technically* solved by the *non-renormalization theorems* of supersymmetry

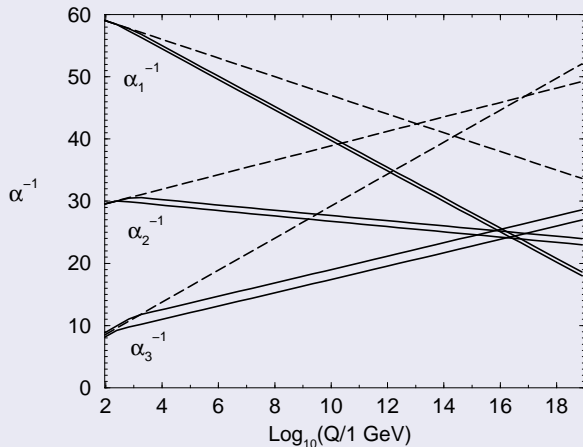
## It provides candidate to Dark Matter

There is a natural candidate for Cold Dark Matter (**WIMP**) in the MSSM: the **lightest neutralino (LSP)**, provided that *R*-parity is unbroken

## It predicts Gauge coupling unification

Consistently with LEP measurements and if superparticles are at  $\sim$  TeV scale gauge couplings unify at a scale

$$M_{GUT} \sim 2 \times 10^{16} \text{ GeV}$$



### Outline

UV sensitivity of the electroweak vacuum

### MSSM

#### MSSM features

- The Higgs mass
- Pre-LHC plots
- Post-LHC plots
- Drawbacks of the MSSM

### Little Higgs

### Gauge-Higgs unification

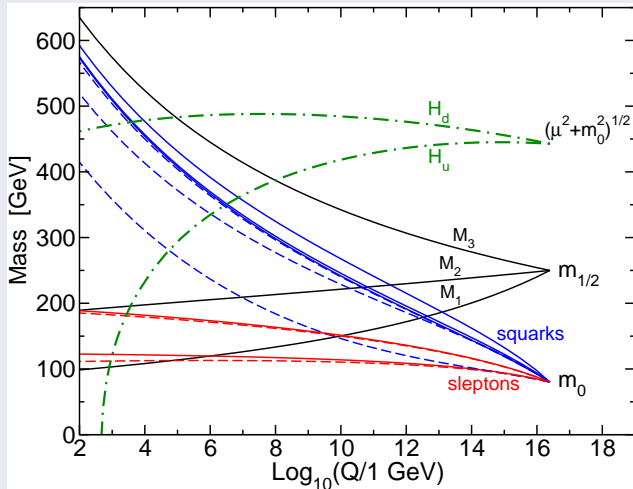
### Warped models

### Conclusion



## It triggers Electroweak breaking

If soft breaking parameters are generated at  $M_{GUT}$  a **tachyonic mass** can be **triggered by RGE** at the weak scale



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**MSSM features**

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## It solves the Stability/Triviality problems

- ▶ The stability ( $\lambda < 0$ ) and triviality/Landau pole ( $\lambda \rightarrow \infty$ ) problems are solved because of the supersymmetric relation

$$\lambda = \frac{1}{8}(g^2 + g'^2)$$

- ▶ Because the gauge couplings remain perturbative (and positive) up to  $M_{GUT}$  there is no stability and/or triviality problem in the MSSM
- ▶ As a consequence: the Higgs mass (unlike in the SM) is **NOT** a free parameter. For the SM-like Higgs

$$m_h^2 \lesssim M_Z^2 \cos^2 2\beta + \text{radiative corrections}$$

- ▶ The Higgs mass is a **prediction** in a supersymmetric theory  $\Rightarrow$  theoretical constraints

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**MSSM features**

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# THE HIGGS MASS

- ▶ The Higgs mass is a **prediction** in the MSSM
  - ▶ At the **tree level** there is the absolute bound

$$m_h^2 \leq M_Z^2$$

- ▶ At **one-loop** there is an important contribution controlled by the top/stop sector

## One-loop

$$\Delta m_h^2 = \frac{3G_F m_t^4}{\sqrt{2}\pi^2} \left[ \log \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{X_t^2}{m_{\tilde{t}}^2} \left( 1 - \frac{X_t^2}{12m_{\tilde{t}}^2} \right) \right]$$

$$X_t = A_t - \mu / \tan \beta$$

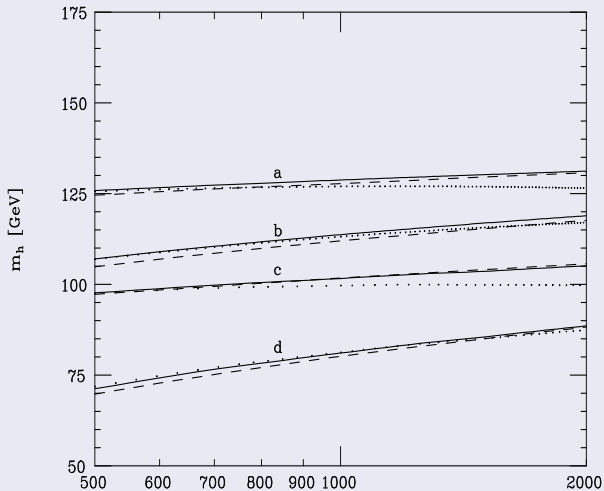
- ▶ Even if the one-loop contribution can be larger than the tree-level **perturbation theory holds**

## Little fine-tuning problem

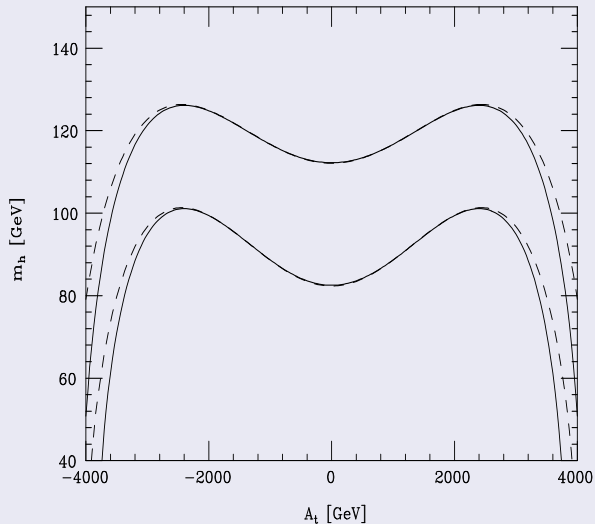
To satisfy the experimental bound on the Higgs mass a **stop around the TeV scale** is needed which produces a  $\sim 1\%$  fine-tuning in the determination of the Z-mass

# PRE-LHC PLOTS

$m_h$  Vs.  $M_{SUSY}$  [ $m_A \sim 1$  TeV, (a,b)  $\tan \beta = 15$   
 $A_t/M_{SUSY} = (\sqrt{6}, 0)$ ; (c,d)  $\tan \beta = 2$ ]



# $m_h$ Vs. $A_t$ [ $M_{SUSY}, m_A \sim 1$ TeV, $\tan \beta = 15, 2$ ]



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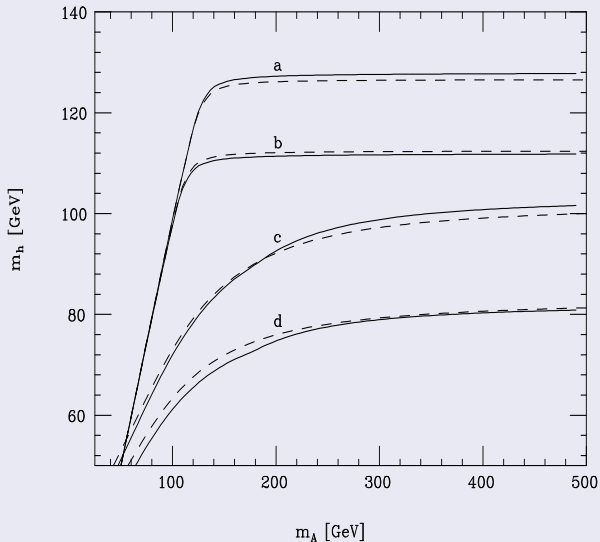
## Little Higgs

Gauge-Higgs  
unification

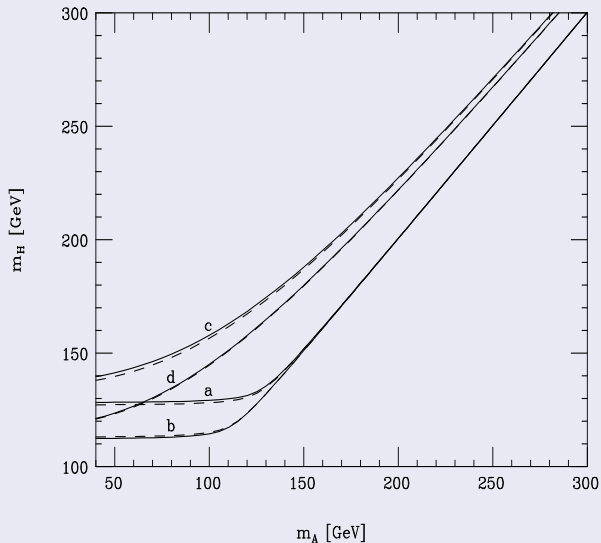
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# $m_h$ Vs. $m_A$ [ $M_{SUSY} \sim 1$ TeV]



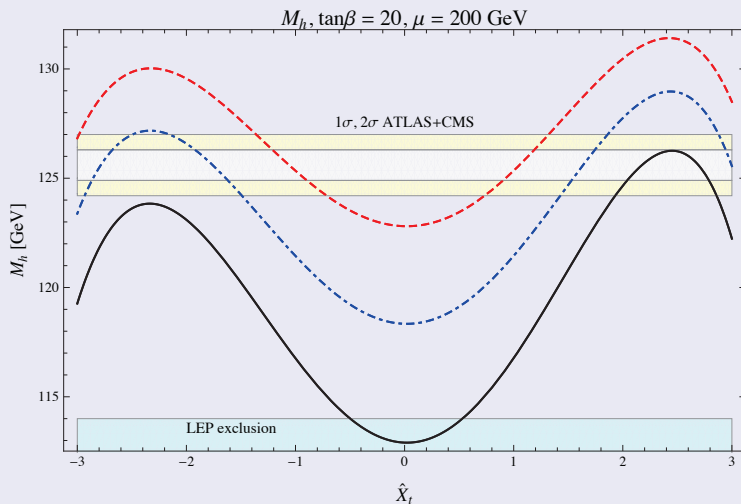
# $m_H$ Vs. $m_A$ [ $M_{SUSY} \sim 1$ TeV]



# POST-LHC PLOTS

Some recent results <sup>1</sup>

$$M_{SUSY} = 1, 2, 4 \text{ TeV}, \hat{X}_t = X_t/M_{SUSY}$$



<sup>1</sup>P. Draper, G. Lee and C. E. M. Wagner, arXiv:1312.5743 [hep-ph]



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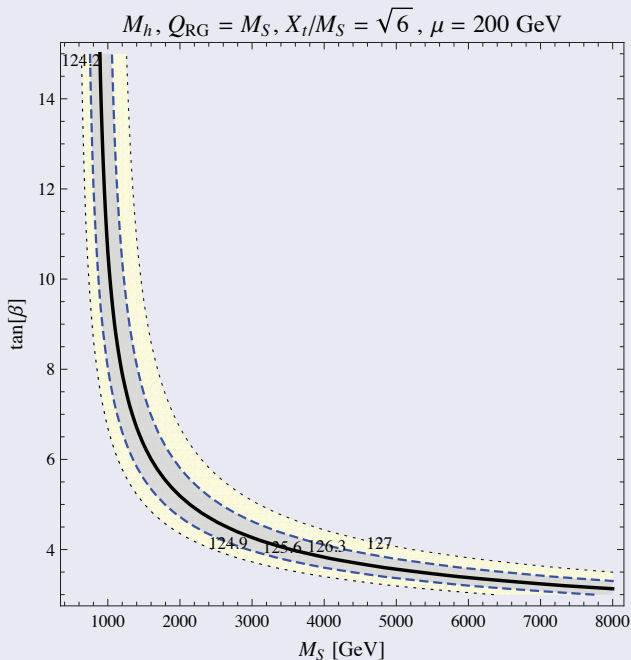
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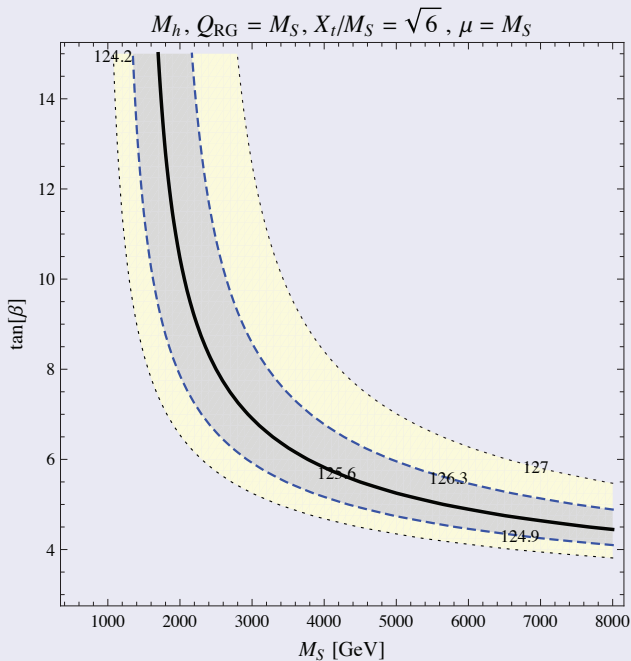
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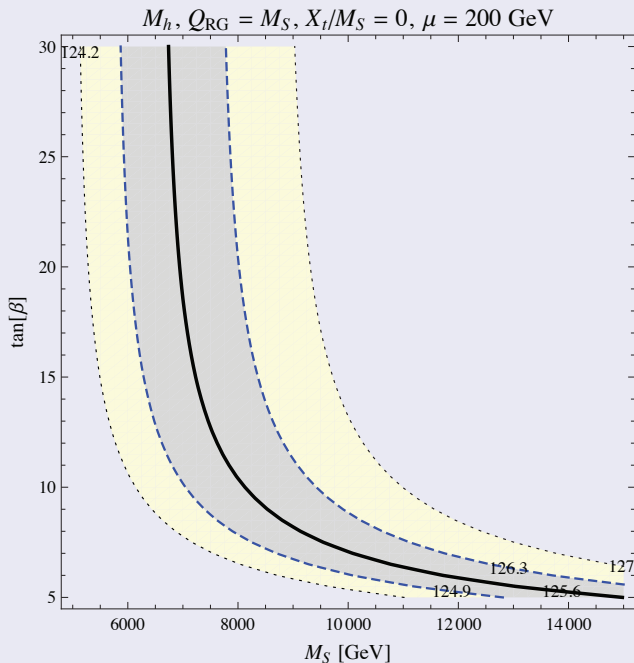
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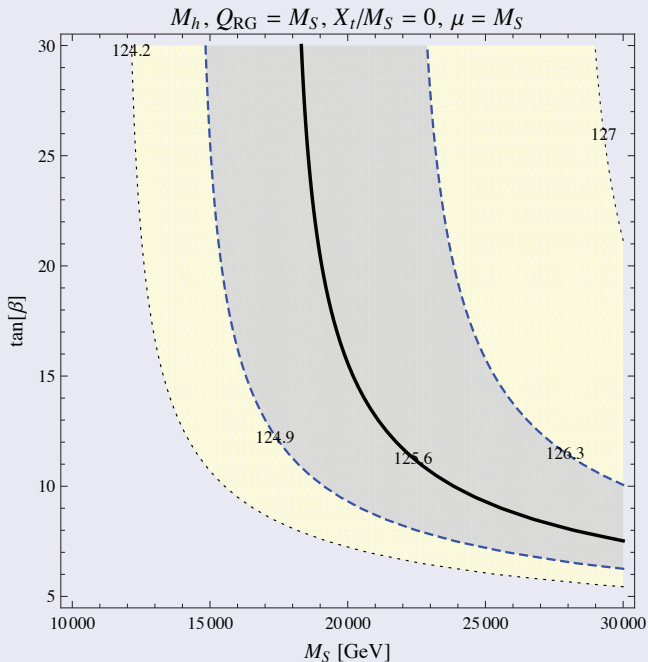
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# Drawbacks of the MSSM

- ▶ Little fine tuning:  $\sim 1\%$  **fine-tuning**
- ▶ **Large number** ( $\sim 10^2$ ) of free parameters
- ▶ Uncertainty in the mechanism of **supersymmetry breaking**:
  - ▶ **Gravity mediation**:
    - ▶ Universal mechanism solving the  $\mu/B\mu$  problem
    - ▶ Its minimal version reduces the number of free parameters to a few
    - ▶ So-called **Supergravity** models
  - ▶ **Gauge mediation**
    - ▶ It is **flavor blind**
    - ▶ It has a  $\mu/B\mu$  problem
    - ▶ **Gravitino is the LSP**
  - ▶ **Anomaly mediation**
    - ▶ **Tachyonic** sleptons
- ▶ **Supersymmetric flavor problem**: supersymmetric partners can create FCNC and CP violating operators
- ▶ Gravity mediation has to be **subdominant** ( $\sim 0.1\%$  of gauge mediation)

# LITTLE HIGGS

- ▶ Little Higgs models aim to solve the **Little Hierarchy** problem (say between EW scale and 10 TeV)
- ▶ The symmetry that protects the (little) hierarchy is a **global symmetry** of which the **Higgs** is an approximate **(pseudo) Goldstone boson**
- ▶ It is inspired from low energy hadronic physics: there  $\pi^{\pm 0}$  are Goldstone bosons associated to the spontaneous breaking  $SU(2)_L \times SU(2)_R \rightarrow SU(2)_I$
- ▶ Similarly the Higgs is the Goldstone boson of a global symmetry  $G_0 \rightarrow H_0$ . It is in the coset space  $H \in G_0/H_0$
- ▶ The symmetry  $H \rightarrow H + c$  is broken (in particular) by Yukawa interactions

$$\Rightarrow m_H^2 \sim \frac{\alpha_t}{4\pi} \Lambda^2 \Leftrightarrow \text{LEP paradox}$$

- ▶ LH is a clever construction to avoid the appearance of the lowest order contribution to  $m_H^2$

## Collective breaking

- ▶ The mass of a Higgs pseudo-Goldstone boson from the different couplings  $\alpha_i$  that break the Goldstone symmetry is

$$m_H^2 = \left( c_i \frac{\alpha_i}{4\pi} + c_{ij} \frac{\alpha_i \alpha_j}{(4\pi)^2} \right) \Lambda^2$$

where the coefficients are controlled by selection rules

- ▶ If the Goldstone symmetry is **restored when any single coupling  $\alpha_i = 0$**

$\Rightarrow$  To totally destroy the Goldstone symmetry one requires the combined effect **[collective breaking]** of **at least two non-zero couplings**

$$\Rightarrow m_H^2 \sim \left( \frac{\alpha}{4\pi} \right)^2 \Lambda^2 \Rightarrow \Lambda \sim 10 \text{ TeV}$$

- ▶ This is a solution to the LEP paradox/Little Hierarchy problem

## General structure

- ▶ There is a global group  $G_g$  which spontaneously breaks to a subgroup  $H_g$  at a scale  $f \sim 1$  TeV and the theory becomes strong at the scale  $\Lambda \sim 4\pi f \sim 10$  TeV [Scales are similar to  $\Lambda_{QCD}$  and  $f_\pi$  in QCD]
- ▶ The subgroup  $G_I \subset G_g$  is gauged:  $G_I \supset SU(2) \times U(1)$
- ▶ The combination of spontaneous and collective breaking makes:  $G_I \rightarrow SU(2) \times U(1)$  leaving heavy vector bosons and fermions with masses

$$M_{Heavy} \sim g f \sim 1 \text{ TeV}$$

- ▶ Higgs is part of the Goldstone multiplet which parametrizes the coset space  $G_g/H_g$

Model	$G_g$	$H_g$
<i>Littlest</i>	$SU(5)$	$SO(5)$
<i>Simplest</i>	$SU(3)^2$	$SU(2)^2$

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## General structure

- ▶ The generators of  $G_I$  do not commute with the generators of the Higgs and thus **gauge and Yukawa couplings collectively break the Goldstone symmetry and induce a Higgs mass**
- ▶ The global invariance of the SM must be **extended** according to the different models (Littlest, Simplest,...)
- ▶ There are **same spin partners** for every SM field.
- ▶ When computing corrections to the Higgs mass these partners enforce the selection rule  $c_i = 0$  by cancelling the one-loop quadratic divergent contributions of the Higgs field
- ▶ For instance if  $SU(3) \subset G_g$ 
  - ▶ The quarks appear in triplets or singlets

$$\begin{pmatrix} t \\ b \\ T \end{pmatrix}_L, t_R, b_R, T_R$$

- ▶ The Higgs boson arises as a pseudo-Goldstone boson from the spontaneous breaking  $SU(3) \rightarrow SU(2) \times U(1)$

## General structure

- ▶ The gauge structure is also enlarged

Model	$G_g$	$H_g$	$G_l$
<i>Littlest</i>	$SU(5)$	$SO(5)$	$[SU(2) \times U(1)]^2$
<i>Simplest</i>	$SU(3)^2$	$SU(2)^2$	$SU(3) \times U(1)$

- ▶ **Littlest:**

- $SU(5) \rightarrow SO(5)$ :  $24-10=14$  Goldstone bosons
- 4 absorbed by the broken gauge group
- 10 Goldstone bosons = 4 (Higgs doublet) + 6 (Higgs triplet)

- ▶ The one-loop **quadratic divergence** from the **top** quark

$$\Delta M_H^2 \sim -\frac{\alpha_t}{4\pi} \Lambda^2$$

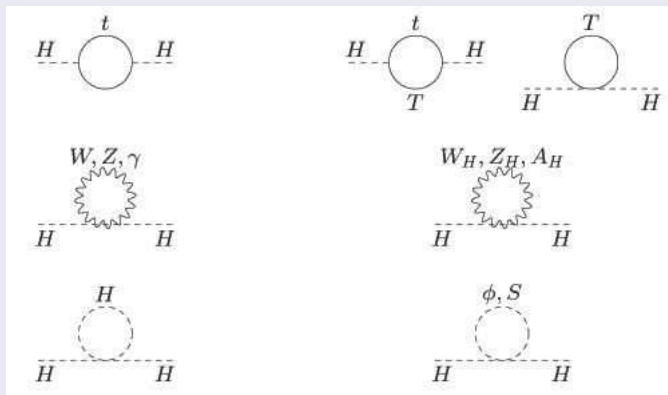
is cancelled by that from the  $T$  quark

- ▶ The one-loop **quadratic divergence** from the  $W$  gauge boson

$$\Delta M_H^2 \sim \frac{\alpha_W}{4\pi} \Lambda^2$$

is cancelled by that from the  $W_H$  gauge boson

## Cancellation of quadratic divergences



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## Electroweak breaking

It is triggered by the  $t - T$  sector analogously to the MSSM

$$\Delta m_H^2 = -\frac{3}{8\pi^2} h_t^2 m_T^2 \log \frac{\Lambda}{m_T}$$

Since  $\Delta m_H^2 \sim m_T^2$  electroweak breaking requires some **tuning** of at least 5% as in the MSSM

## Dark Matter

In the **Littlest** LH models one can introduce a  $T$ -parity such that **SM particles** (extra particles) are **T-even** (**T-odd**). In this case the lightest T-odd gauge boson is a candidate to DM

## Electroweak precision tests

T-parity forbids the mixing between T-odd and T-even gauge bosons leading naturally to  $S = 0$

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# Gauge Higgs Unification

- ▶ We have explored two symmetries protecting the Higgs from quadratic divergences: **supersymmetry and a global symmetry**
- ▶ In higher dimensional theories there is another symmetry which could do the job: **a gauge symmetry**
- ▶ The gauge bosons of a higher dimensional gauge symmetry decompose as

## Lorentz Decomposition

$$A_M^A = A_\mu^A, A_i^A \quad [\mu = 0, \dots, 3, i = 1, \dots, d]$$

- ▶  $A_\mu^A$  are gauge bosons in four dimensions
- ▶  $A_i^A$  are scalar in the **adjoint** representation

## Orbifold constructions

We need to compactify extra dimensions in an orbifold:

e.g. for  $d = 1$  ( $A_\mu, A_5$ )

$$S^1/\mathbb{Z}_2$$

- ▶ The orbifold group has to act non trivially on the group generators such that:

## Orbifold Decomposition

$$A_{\mu}^A = A_{\mu}^a(\text{even}), A_{\mu}^{\hat{a}}(\text{odd})$$

$$A_5^A = A_5^a(\text{odd}), A_5^{\hat{a}}(\text{even})$$

- ▶ Only even fields have zero modes  $\phi_{\text{even}}^{(n)}$ ,  $n = 0, 1, 2, \dots$  while odd field have only non zero modes  $\phi_{\text{odd}}^{(n)}$ ,  $n = 1, 2, \dots$
- ▶ The Higgs mechanism acts for all modes as

## Higgs mechanism

$$(A_{\mu}^{\hat{a}} \text{ massless} + A_5^{\hat{a}})^{(n \neq 0)} = A_{\mu}^{\hat{a}(n \neq 0)} \text{ massive}$$

$$(A_{\mu}^a \text{ massless} + A_5^a)^{(n \neq 0)} = A_{\mu}^{a(n \neq 0)} \text{ massive}$$

- ▶ The massless states are the zero modes

## Massless states

$$A_{\mu}^{a(n=0)}, A_5^{\hat{a}(n=0)}$$

# HOW TO GET A DOUBLET FROM AN ADJOINT

- ▶ To get a doublet out of an adjoint one has to make a careful orbifold breaking
- ▶ One has to **enlarge** the gauge group since the

SM Higgs is **NOT** in the adjoint representation of  $SU(2) \times U(1)$

- ▶ For instance

$$SU(3) \rightarrow SU(2) \times U(1)$$

Achieved by the orbifold action

$$A_\mu(-y) = UA_\mu(y)U^\dagger, \quad A_5(-y) = -UA_5(y)U^\dagger \text{ with}$$

$$\text{diag}(-1, -1, +1)$$

which breaks  $SU(3)$  into  $SU(2) \times U(1)$

- ▶ The Higgs mass is protected from **quadratic divergences** in the bulk by the **5D gauge symmetry**

- ▶ The orbifold has two **fixed points** at  $y = 0, \pi R$  which are singular and four-dimensional
- ▶ The Higgs mass is protected from **quadratic divergences at the fixed points** by the **shift symmetry** (inherited from the five-dimensional gauge invariance)  $\delta A_5 = \partial_y A_5$

## How to get the gauge bosons

$$\left( \begin{array}{ccc} A_\mu^3 + A_\mu^8/\sqrt{3} & A_\mu^2 - iA_\mu^2 & A_\mu^4 - iA_\mu^5 \\ A_\mu^1 + iA_\mu^2 & -A_\mu^3 + A_\mu^8/\sqrt{3} & A_\mu^6 - iA_\mu^6 \\ A_\mu^4 + iA_\mu^5 & A_\mu^6 + iA_\mu^7 & -2A_\mu^8/\sqrt{3} \end{array} \right)$$

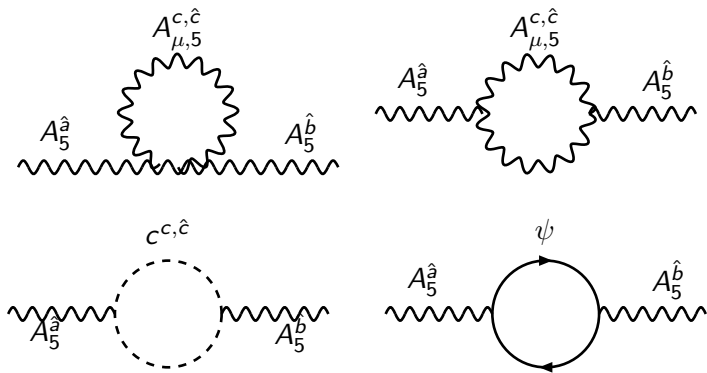
## How to get the Higgs bosons

$$\left( \begin{array}{ccc} A_5^3 + A_5^8/\sqrt{3} & A_5^2 - iA_5^2 & A_5^4 - iA_5^5 \\ A_5^1 + iA_5^2 & -A_5^3 + A_5^8/\sqrt{3} & A_5^6 - iA_5^6 \\ A_5^4 + iA_5^5 & A_5^6 + iA_5^7 & -2A_5^8/\sqrt{3} \end{array} \right)$$



- ▶ Since the space is compactified there can be **finite** contributions to the  $A_5^{\hat{a}}$  mass proportional to  $1/R$

The diagrams contributing to the mass of  $A_5^{\hat{a}}$  are



$$m_{\hat{a}}^2 = \frac{3g^2}{32\pi^4 R^2} \zeta(3) [3C_2(\mathcal{G}) - 4T(R)N_f]$$

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unificationHow to get a doublet  
from an adjoint**Radiative symmetry  
breaking**

Difficulties with GHU

Warped models

Conclusion

There is a number of difficulties with this (otherwise very nice) scenario

## Drawbacks

- ▶ In more than five dimensions a (quadratically divergent) **tadpole** localized at the fixed points  $F_{ij}$  is generated by radiative corrections while the **quartic** Higgs coupling is sizeable and generated by the term  $F_{ij}^2$  in the bulk
- ▶ In **five** dimensions there is no localized tadpole but there is neither a tree-level quartic coupling which means difficulties with *too small a Higgs mass*
- ▶ It is difficult to have a theory with the correct prediction for the **weak** angle [extra  $U(1)$ 's are usually required]
- ▶ **Fermion masses** are difficult to accommodate since they come from gauge couplings: in particular the top quark used to be too light
- ▶ The compactification scale is usually too small in conflict with EWPT
- ▶ The theory has a very **low cutoff** after which it becomes non-perturbative

# WARPED MODELS

Some of these difficulties can be alleviated by embedding GHU in a **warped** (Randall-Sundrum) 5D space time

## Ways out

- ▶ Warped models are valid up to scales of order  $M_{GUT}$  or  $M_{Planck}$  and they can unify
- ▶ The Higgs is **holographic**, i.e. it is localized towards the IR brane [at higher scales it is composite]
- ▶ **Fermion masses** can be implemented by means of their **localization**, i.e. five-dimensional masses
- ▶ The top quark (to get a big mass) is **localized** as the Higgs. So it is also **holographic**
- ▶ EWPT as well as corrections to the  $Zb\bar{b}$  vertex lead to KK-masses in the 2.5 – 4 TeV, which imply  $\sim 1\%$  fine-tuning for the Higgs mass (similar to the MSSM)
- ▶ These models are the modern version of technicolor theories: they make use of the **AdS/CFT** correspondence for **calculability**



- ▶ An **AdS 5D** theory with two branes was proposed <sup>2</sup>

$$ds^2 = e^{-2A(y)} \eta_{\mu\nu} dx^\mu dx^\nu + dy^2, \quad A(y) = ky$$

- ▶ To solve the **hierarchy problem** the Higgs should be
  - ▶ **Localized** on the **IR** brane (**composite**): theory is EWPT disfavored, **or**
  - ▶ Propagating in the **bulk** but with a profile along the extra dimensions leaning towards the **IR** brane (**a degree of compositeness**)

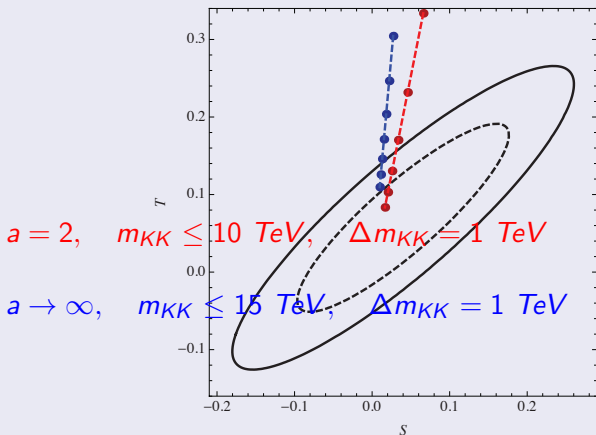
$$h(y) = h(0)e^{aky}, \quad a > 2 \quad (\text{to solve hierarchy problem})$$

- ▶ The hierarchy problem is solved because the Planckian Higgs mass is warped down to the weak scale by the **geometry** or in the dual picture because the **conformal operator breaking EW has dimension  $> 2$**
- ▶ To "solve" the flavour problem fermions should propagate in the bulk and with different localizations
- ▶ Fermion localization is controlled by Dirac mass  $c_f A'(y)$

<sup>2</sup>L. Randall and R. Sundrum, hep-ph/9905221 

Electroweak data impose very strong constraints

$$m_{KK} \gtrsim 10 \text{ TeV}$$



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Conclusion

- ▶ The RS model has to be modified to avoid the large corrections to EW observables.
- ▶ It can be done by deforming the AdS metric in the IR <sup>3</sup>
- ▶ A particularly simple model for the metric has been used as

## IR deformed model

$$A(y) = ky - \frac{1}{\nu^2} \log \left( 1 - \frac{y}{y_s} \right)$$

$$\phi(y) = -\frac{\sqrt{6}}{\nu} \log[\nu^2 k(y_s - y)]$$

- ▶ A UV brane at  $y = 0$  and a IR brane at  $y_1 = y_s - \Delta$  with  $k\Delta \ll ky_s$

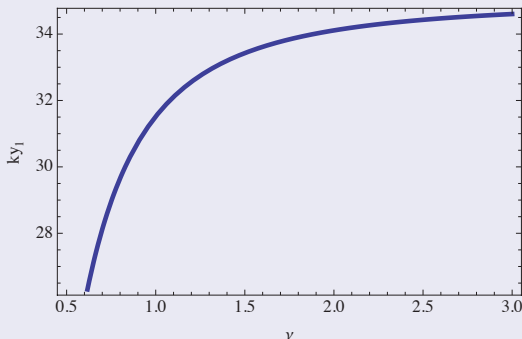
<sup>3</sup>J. A. Cabrer, G. von Gersdorff, MQ, arXiv:1011.2205 [hep-ph], arXiv:1103.1388 [hep-ph]





- ▶ One is the lowering of the compactification volume  $ky_1$

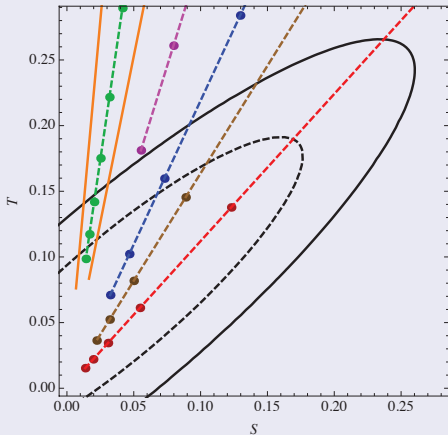
$$k\Delta = 1 \text{ and } A(y_1) = 35$$



- ▶ As the  $T$  parameter is enhanced by  $ky_1$



SW:  $a = 3.1$ ,  $m_{KK} \leq 3$  TeV,  $\Delta m_{KK} = 0.5$  TeV



$\nu = 0.5, 0.525, 0.55, 0.6;$

$\nu = 5, m_{KK} \leq 12$  TeV,  $\Delta m_{KK} = 1$  TeV

ELECTROWEAK  
VACUUM

Mariano Quirós

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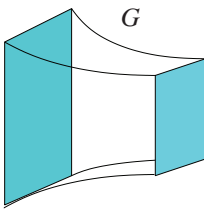
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Conclusion

# CUSTODIAL MODELS

- ▶ Another solution to the large  $T$  problem in RS is introducing a gauge custodial symmetry in the bulk to protect the  $T$  parameter
- ▶ The gauge symmetry  $G$  can protect the mass of extra dimensional components of gauge bosons
- ▶  $A_{\mu}^A$  ( $A_5^A$ ) are gauge bosons (scalars) in four dimensions
- ▶  $G$  is broken by boundary conditions to  $H_{UV}$  ( $H_{IR}$ ) on the UV (IR) brane



The diagram shows a 5D spacetime with a curved geometry. A vertical plane represents the UV brane, and a horizontal plane represents the IR brane. A gauge symmetry  $G$  is indicated in the bulk. Boundary conditions are specified for the UV and IR branes.

$$H_{UV} : \begin{cases} A_{\mu}(+) \text{ i.e. } \partial_5 A_{\mu}^{H_{UV}} = 0 \\ A_5(-) \text{ i.e. } A_5^{H_{UV}} = 0 \end{cases}$$
$$G/H_{UV} : \begin{cases} A_{\mu}(-) \text{ i.e. } A_{\mu}^{G/H_{UV}} = 0 \\ A_5(+) \text{ i.e. } \partial_5 \left( \frac{R}{z} A_5^{G/H_{UV}} \right) = 0 \end{cases}$$
$$H_{IR} : \begin{cases} A_{\mu}(+) \text{ i.e. } \partial_5 A_{\mu}^{H_{IR}} = 0 \\ A_5(-) \text{ i.e. } A_5^{H_{IR}} = 0 \end{cases}$$
$$G/H_{IR} : \begin{cases} A_{\mu}(-) \text{ i.e. } A_{\mu}^{G/H_{IR}} = 0 \\ A_5(+) \text{ i.e. } \partial_5 \left( \frac{R}{z} A_5^{G/H_{IR}} \right) = 0 \end{cases}$$

- ▶ For  $\mathcal{H}_{UV} = SU(2)_L \otimes U(1)_Y$  the number of PGB is  $\dim(G/\mathcal{H}_{IR})$
- ▶ Different models differ so by  $G$  and  $\mathcal{H}_{IR}$ <sup>4</sup>

Model	# Goldstones ( $A_5^{\hat{a}}$ )
$SO(4)/SO(3)$	6-3=3 (Higgsless SM)
$SU(3)/SU(2) \times U(1)$	8-4=4 ( $H_{SM}$ )
$SO(5)/SO(4)$	10-6=4 ( $H_{SM}$ )
$SO(6)/SO(5)$	15-10=5 ( $H_{SM}$ + singlet)
$SO(6)/SO(4) \times SO(2)$	15-6-1=8 ( $H_u, H_d$ )

- ▶ Some of the models contain the custodial group  $SO(4)$  on the IR brane and so contribution to  $T$  parameter protected
- ▶ In the dual theory  $G/\mathcal{H}_{IR}$  is characterized by the scale  $f$

## The expansion parameter in the theory

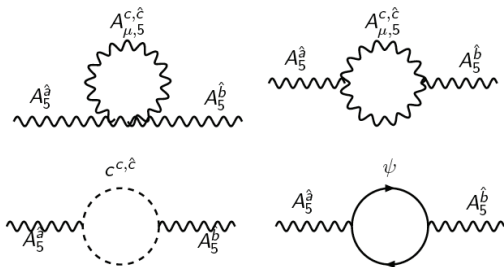
$$\xi = \left(\frac{v}{f}\right)^2$$

$$h_{WWH}^2 = h_{WWH,SM}^2 [1 - \xi]$$

- ▶  $\xi \rightarrow 0 \Rightarrow$  SM limit
- ▶  $\xi \rightarrow 1 \Rightarrow$  Technicolor limit

<sup>4</sup>R. Contino et al., hep-ph/0306259 and hep-ph/0612048; K. Agashe et al.,

$SU(2)_L \otimes U(1)$  breaking is **radiative**



One can consider an **effective theory**<sup>a</sup> parametrized by  $\xi$  which measures the degree of **compositeness** of the Higgs

<sup>a</sup>J. R. Espinosa et al., arXiv:1003.3251 [hep-ph]

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# CONCLUSIONS

- ▶ The last word will be from **LHC**
- ▶ One possibility is that the theory below  $M_{Planck}$  is **just the Standard Model**: in that case we should try to find other solutions to the hierarchy problem, as e.g. an anthropic solution/landscape
- ▶ If New Physics is found at LHC it should possibly provide a (partial) solution to the "experimental" SM problems (DM, strong CP problem, baryogenesis, . . .) and/or the "theoretical" problems (hierarchy problem, vacuum instability/metastability/stability, flavour structure, neutrino patterns, . . .)
- ▶ Hopefully New Physics will interfere with the mechanism of electroweak breaking and should leave an "imprint" in Higgs observables.
- ▶ As for Higgs precision physics we will (probably) need a high-energy linear or circular collider