

**Precision Particle Physics**  
**The Standard Model and Beyond**

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**6 Lectures**

**Ferrara, Italy**

**May 20-22, 2013**



# **Precision Themes**

- QED Precision – Historical Perspective  
**Electromagnetic Dipole Moments** Theory vs Exp.
- **Muon Lifetime** & Electroweak Precision ( $m_t$ ,  $m_H$ )  
S & T “New Physics” Parameters
- **Higgs Boson Precision**  
Branching Ratios, CP Violation? **“Sick” Field Theory**
- **Precision Neutrino Masses & Mixing**  
CP Violation and Beyond

# *Ancient Perspective*

## *1492 Columbus Discovers America*

- *“There are more things in heaven and earth, Horatio,  
Than are dreamt of in your philosophy.”*

*Hamlet (≈1600)*

*Galileo: 1564-1642*

*Newton: 1642-1727*

-

*Maxwell: 1831-1879*

*Einstein: 1879-1955*

*Meanwhile*

# **Michelson (The Master of Precision) 1894**

“The more important fundamental laws and facts of Physical Science have all been discovered, and these are now so firmly established that the possibility of their ever being supplanted in consequence of new discoveries is exceedingly remote... Our future discoveries must be looked for in the sixth place of decimals.”

Radioactivity 1896

Electron Discovery 1897

Special Relativity

General Relativity

Quantum Mechanics; Spin

Dirac Equation 1928 (QM + S. Relativity + Spin + EM)

QED  $U(1)_{em}$  Photon

**Today**  $c = 299\,792\,458 \text{ m s}^{-1}$  **Exactly** (Meter Definition)

Natural Units  $c=1$

## Later

*Yang-Mills Non-Abelian Gauge Theories 1954*

*Standard Model of Particle Physics  $\geq 1967$*

*$SU(2)_L \times U(1)_Y$   $W^\pm$ ,  $Z$  bosons;  $SU(3)_C$  8 gluons*

*3 generations of quarks and leptons*

*2012: “Fundamental” Higgs (125GeV) Scalar Discovered!*

*Remnant of Electroweak Symmetry Breaking*

*Now: Entering the Age of Precision Higgs Physics!*

*“Sick” or “Rich” Quantum Field Theory?*

**Precision Measurements**  
**QED and Lepton Dipole Moments**

***Based in part on: “Lepton Moments”***  
***Editors B. Lee Roberts & W. Marciano***

**William J. Marciano**  
**Lectures 1 & 2**  
**Ferrara, Italy**  
**May 20, 2013**



# Outline

## 1.) Historical Introduction

- i) Wolfgang Pauli (**1924 Exclusion Principle!**)
- ii) Spin (1925)
- iii) The Dirac Equation (1928)  $g_e=2$  & Antiparticles
- iv)  $U(1)_{em}$  Local Gauge Invariance

## 2.) Post WWII Developments (1947-48)

### The Birth of Quantum Electrodynamics (QED)

- i) Electron Anomalous Magnetic Moment  $g_e-2$

#### Basic 1 Loop Calculation

- ii) Lamb Shift: Hydrogen  $2S_{1/2}-2P_{1/2}$
- iii) The Muon: “Who ordered that?”  $m_\mu \approx 207m_e$

### 3.) **Recent Developments**

i)  $g_e - 2$  (5 loops!)

ii) Lamb Shift?

iii)  $g_\mu - 2$  (New Physics - Supersymmetry/Something Else?)

### 4.) **“Light” Dark Photon (Dark Matter Force Mediator)**

**Viewer Discretion Advised** - Speculative

### 5.) **Muonic Hydrogen Lamb Shift**

**The Proton Size Puzzle** ( $r_p(\text{ep})$  vs  $r_p(\mu\text{p})$  atom)

**5-8 sigma difference**



- 6.) **Electric Dipole Moments** – “New Physics”
- 7.) The Standard Model –  $SU(3)_C \times SU(2)_L \times U(1)_Y$   
Electroweak Unification
  - i) The Muon Lifetime & Fermi Constant
  - ii) Natural relationships
$$\sin^2\theta_w = 1 - (m_w^0/m_z^0)^2 = (e^0/g^0)^2$$
  - iii) **CKM Unitarity**
- 8.) Higgs Properties & Problems (Naturalness)  
 $\lambda\phi^4$  theory is unnatural! Sick?
- 9.) Neutrino Oscillations – Status & Future
- 10.) Concluding Remarks

# 1.) Historical Introduction

1897 Electron ( $e^-$ ) Discovered J.J. Thomson  
followed by major developments

Early 20<sup>th</sup> Century

Quantum Mechanics ( $\gamma$  photon)

Special & General Relativity

1919 Proton ( $p^+$ ) Discovered  $m_p \approx 1840 m_e$  Ernest Rutherford

1926 Schrodinger Equation – Non-Relativistic QM

In a 1924 letter to Lande, W. Pauli presented his now famous  
**“Pauli Exclusion Principle”**

Atomic Spectroscopy of the Bohr Atom, electrons  
classified by quantum no.:  $n, l, m$  &  $t$ =**twofoldness**

**No two electrons can have identical quantum numbers!**

Fundamental Property of Nature → Chemistry,  
Neutron Stars, Baryon Spectroscopy (quark color)...

***But, what was “twofoldness”?***

# Wolfgang Pauli

Pauli Portraits

6/1/11 11:41 AM

## Wolfgang Pauli



## ii) **Electron Spin (1925)**

In 1925, Kronig (unpublished) and independently Uhlenbeck and Goudsmit interpret “twofoldness” as Electron spin  $S = \pm \frac{1}{2}$ . Wavefunction antisymmetric under Interchange of identical electrons.

**Pauli:** *“A clever idea but nothing to do with nature!”*

Eventually spin established (Thomas relativistic factor of 2)

Electron magnetic moment  $\mu_e = g_e e / 2m_e \mathbf{S}$

**$g_e = \text{gyromagnetic ratio} = 2$**

**Ironic:** Pauli 2x2 **spin** matrices (Non-relativistic)

iii) **The Dirac Equation** (1928)  $g_e=2$

*“The Dirac equation like youth is often wasted on the young”*

**The Stage in 1928**

Non Relativistic Schroedinger Eq. First Order

Relativistic Klein-Gordon Scalar Eq. (spin 0) Second Order

Spin 1/2 - Pauli 2x2 Matrices (non-relativistic spin)

**The Genius of Dirac**

QM+Special Rel.+Spin+EM Gauge Invariance  $U(1)_{em}$

First Order Equation Spinor (4 Component)

$$i(\partial_\mu - ieA_\mu(\mathbf{x}))\gamma^\mu\psi(\mathbf{x}) = m_e\psi(\mathbf{x}),$$

4x4  $\gamma^\mu$  (Dirac) matrices:  $\gamma^\mu\gamma^\nu + \gamma^\nu\gamma^\mu = 2g^{\mu\nu}$

**Similar eq. for the proton  $m_p \approx 1840m_e$**

Mag. Moment:  $\mu = g_e e/2m_e \mathbf{s}$   $g_e = \underline{2}$  Not 1!

As Observed Experimentally

Automatic Unexpected Success of Dirac Eq.

**Dirac Derivation of  $g_e = 2$  (1928 & “QM” Book)**

(Advanced Exercise for students)

Go to second order formalism (apply Dirac operator)

$$[-i(\partial_\mu - ieA_\mu(\mathbf{x}))\gamma^\mu - m_e] \times [i(\partial_\mu - ieA_\mu(\mathbf{x}))\gamma^\mu - m_e]\psi(\mathbf{x})$$

and find terms in Klein-Gordon Eq.

$$\mu \bullet \mathbf{H} + i\rho_1 \mu \bullet \mathbf{E} \text{ (edm?) } \mu = \underline{2}e/2m_e \mathbf{s}$$

Imaginary Part? - **Non Physical?** → Ignore?

By the 4th edition of “QM” he got rid of it

(What is an electric dipole moment (edm)?

and what is a chiral phase?)

**Later realized Negative Energy Solutions!**

**(Dirac Equation Largely Ignored)**

**W. Pauli was a primary antagonist**

***Dirac predicts positron, antiproton, antihydrogen...!!!***

***Antimatter Discovery Dirac's crowning glory!***

***Doubled Particle Spectrum!***

**Why is the Universe Matter-Antimatter Asymmetric?**

**Baryogenesis! Leptogenesis! (Sakharov Conditions)**

**(1964-CP Violation Discovered-CKM Not Enough)**

**“New Physics” Source of CP Violation Needed!**

**Supersymmetry, 4th Generation, Multi-Higgs...**



# Baryogenesis: $N_B/N_\kappa \approx 10^{-10}$

1957 - Parity Violation in Weak Interactions (Maximal!)

Lee & Yang Why is nature left-handed (Chiral)?

1964- CP Violation Discovered in Kaon Decays

1967 Sakharov Conditions:

- 1) Baryon Number Violation
- 2) CP Violation (strong source)
- 3) Non-Equilibrium 1<sup>st</sup> Order Phase Transition

*\*(Leptogenesis – Very Early Universe Alternative)*

# Completing the Picture?

1930 Pauli Proposes the Neutrino ( $\nu$ ) (weak interactions)

1931 Neutron ( $n$ ) Discovered (strong interactions)

1932 Positron ( $e^+$ ) Discovered (***Anti-Matter Exists!***)

- 
- 
- 

**p, n, e,  $\nu$  basic ingredients of our Universe (Existence)**  
**strong, weak, electromagnetic & gravitational interactions**

# Today

Elementary Particle Physics (Many Particles!)

$SU(3)_C \times SU(2)_L \times U(1)_Y$  Standard Model

8 gluons +  $W^\pm, Z, \gamma$  **gauge bosons (spin 1)**

(Pauli: Yang-Mills Theory is infrared sick! or Rich?)

$SU(3)_C$  Quantum Chromodynamics

One of the **greatest Scientific Discoveries of the Twentieth Century!**

3 generations of **quarks & leptons (mix- $\rightarrow$ CP violation)**

**$e, \nu_e, u, d$     $\mu, \nu_\mu, c, s$     $\tau, \nu_\tau, t, b$  ( $m_t/m_\nu > 10^{13}!!$ ) (spin  $\frac{1}{2}$ )**

**Scalar Doublet:  $S^\pm, S^0, H$  source of mass (spin 0)**

# **2012: The Year of the Higgs Boson!**

**Now Standard Model Complete!**

**Higgs (H) Boson Discovery**

**Remnant of Particle Mass Origin (Remember Michelson)**

**What Else Is There? New Particles? Interactions?**

**Supersymmetry (*Doubles The Spectrum!*)**

**But Badly Broken**

**Waiting for SUSY or “Something” Else**

***So far: No direct evidence for Supersymmetry,  
At The LHC (Large Hadron Collider)!***

***Still Early – Nevertheless MSSM in trouble***

***The Higgs – May Be Last Particle Ever Discovered?  
(Probably Not  $\lambda\phi^4$  theory is sick/unnatural)***

Left with Mysteries: Why Baryogenesis? CP?  
Why 3 Generations?  
Why Parity Violation?  
Dark Matter, Energy...

## We could add extra terms to the Dirac Equation

(using  $F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$ )

$$e/4m_e a_e F_{\mu\nu}(x) \sigma^{\mu\nu} \psi(x) + i/2d_e \gamma_5 F_{\mu\nu}(x) \sigma^{\mu\nu} \psi(x)$$

Anomalous Mag. Mom.

$$g_e = 2(1 + a_e)$$

$a_e =$  Pauli Term

Electric Dipole Mom.

Violates P&T(CP)

Not Observed

$$d_e < 10^{-27} \text{ e-cm}$$

But Must Exist!

Pauli opposed the Dirac Equation (Neg Energy Sol.)

Later became so converted that he opposed proton

Mag. Moment exp. "It must be  $g_p e/2m_p \mathbf{s}$   $g_p = 2!$ "

***Experiment  $g_p = 5.59$***

## iv) $U(1)_{em}$ Local Gauge Invariance

Electrodynamics (with charged electron source)

Invariant under local  $U(1)_{em}$  gauge transformations

$$L = \frac{1}{4} F_{\mu\nu}(x) F^{\mu\nu}(x) + \psi^*(x) \gamma^0 \{ i(\partial_\mu - ieA_\mu(x)) \gamma^\mu - m_e \} \psi(x)$$

$$A_\mu(x) \rightarrow A_\mu(x) - ie\partial_\mu \Lambda(x) \quad \psi(x) \rightarrow \exp(ie\Lambda(x)) \psi(x)$$

**Generalization of Charge Conservation**

**Fundamental principle of interactions**

**Equations of motion: Maxwell's Eqs & Dirac Eq.**

## 2.) Post WWII Developments (1947-48)

### 1947 Small Anomalous Atomic Fine Structure Effects

G. Breit: maybe  $a_e = (g_e - 2)/2 \neq 0$

### 1948 Schwinger Calculates: $a_e = \alpha/2\pi \approx \underline{0.00116}$ ( $\alpha = e^2/4\pi = 1/137$ )

Agreed with measurement of Kusch & Foley!

### Great Success of QED -Quantum Field Theory

*Exercise: 1 loop QED Correction*

$$a_e = (g_e - 2)/2 = \alpha/2\pi$$

### 1947 Lamb measures the $2P_{1/2} - 2S_{1/2}$ splitting

vacuum polarization, electron self-interaction

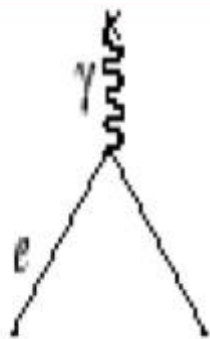
***$a_e$  and Lamb shift start of QED (Quantum Electrodynamics)***

### 1947 Muon established $m_\mu \approx 207m_e$ "Who ordered that?"

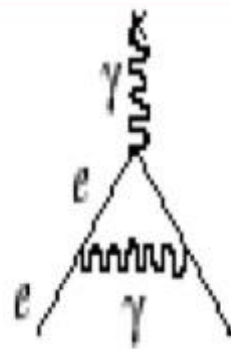
Later  $\tau_\mu = 2.2 \times 10^{-6} \text{sec}$  very long very important



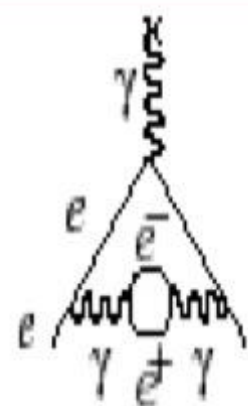
## Anomalous Magnetic Moment Contributions



Dirac



Schwinger



# **Basic Quantum Electrodynamics** **Dirac Eq. the Foundation**

Quantize  $A_\mu(x)$  and  $\psi(x)$  fields  $\rightarrow$  operators

Represents interacting photons and electrons (positrons)

Parameters  $m_e^0$  and  $e_0$  bare electron mass and charge

Renormalized to  $m_e$  and  $e$  physical mass and charge

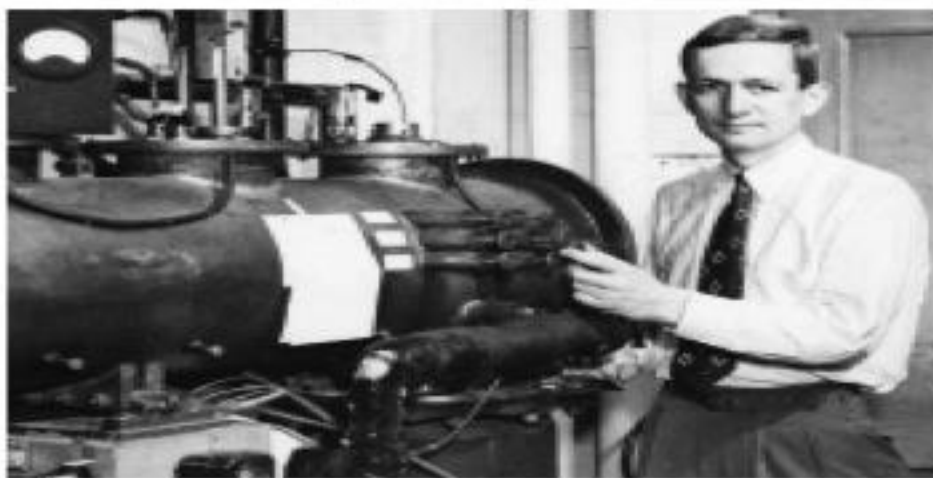
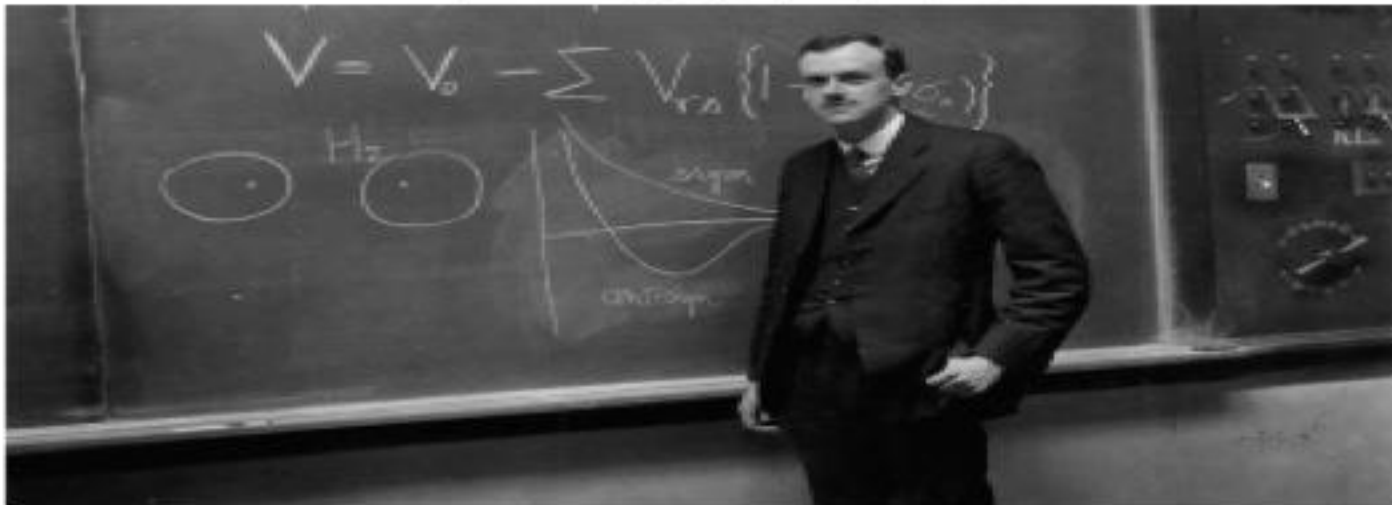
Interaction strength  $e^2/4\pi \approx 1/137$  fine structure constant

**Dirac Strongly Opposed Idea of Infinite Renormalization**

Clockwise:

Julian Schwinger,  
Polykarp Kusch,  
Paul Dirac,  
Norman Ramsey and  
Edward Purcell

Courtesy AIP Emilio  
Segrè Visual Archives  
(full credits overleaf)



Mount Auburn Cemetery



JULIAN SCHWINGER

2·12·1918 — 7·16·1994

# Anomalous Magnetic Moments Today

$$a_l = (g_l - 2)/2 \quad l = e, \mu$$

$$a_e(\text{exp}) = 0.00115965218073(28) \quad \text{unc. } 2.8 \times 10^{-13}!$$

(Hanneke, Fogwell, Gabrielse: PRL 2008)

$$\begin{aligned} a_e(\text{SM}) = & \alpha/2\pi - 0.328478444002546(\alpha/\pi)^2 \\ & + 1.181234016(\alpha/\pi)^3 - 1.9097(20)(\alpha/\pi)^4 \\ & + \underline{9.16(58)(\alpha/\pi)^5} \dots + 1.68 \times 10^{-12}(\text{had}) + 0.03 \times 10^{-12}(\text{EW}) \end{aligned}$$

Aoyama, Hayakawa, Kinoshita, & Nio 2012 Update

$$\alpha^{-1}(^{87}\text{Rb}) = 137.035999049(90)$$

Bouchendira et al. PRL. (2011)

$$a_e(\text{exp}) - a_e(\text{theory}) = -1.05(0.82) \times 10^{-12}$$

Overall Factor 10 Sensitivity Improvement!

Further Improvement? Factor of 2? More?

## ii) Hydrogen Lamb Shift Update?

Depends on proton structure (size)  $r_p$  (radius)

***How large is the proton (rms) radius?***

About a Fermi (fm)  $=10^{-13}\text{cm}$

$\langle r_p^2 \rangle = \lim_{Q^2 \rightarrow 0} -6 \, dF(Q^2)/dQ^2$  em form factor

**CODATA:**  $r_p \approx \underline{0.8768(69)\text{fm}}$  (ep atom) hydrogen spectrum  
(2008) (Main sensitivity - Lamb Shift)

Depends on Rydberg Constant

$R_\infty = 1.0973731568527(73) \times 10^7 \text{m}^{-1}$

**known to 13 significant figures!**

$R_\infty \cong \alpha^2 m_e c / 2h$  "One of the Two most accurately measured fundamental physical constants" **What is better known?**

## 3.ii) Muon Anomalous Magnetic Moment

1957 Garwin, Lederman & Weinrich study  $\pi \rightarrow \mu, \mu \rightarrow e \nu \nu$   
found parity violation & measured  $g_\mu = 2.00 \pm 0.10$

Parity Violation Decay  $\rightarrow$  Self Analyzing Polarimeter  
led to Three Classic CERN Exps. ending in 1977

“The Last  $g_\mu - 2$  Experiment”

- Until Experimental E821 at BNL (2004 Final)

- $a_\mu^{\text{exp}} \equiv (g_\mu - 2)/2 = 116592089(54)_{\text{stat}}(33)_{\text{sys}} \times 10^{-11}$

$$= \underline{116592089(63)} \times 10^{-11}$$

Factor of 14 improvement over CERN results

(Proposed Future Factor 4 Improvement at FNAL)

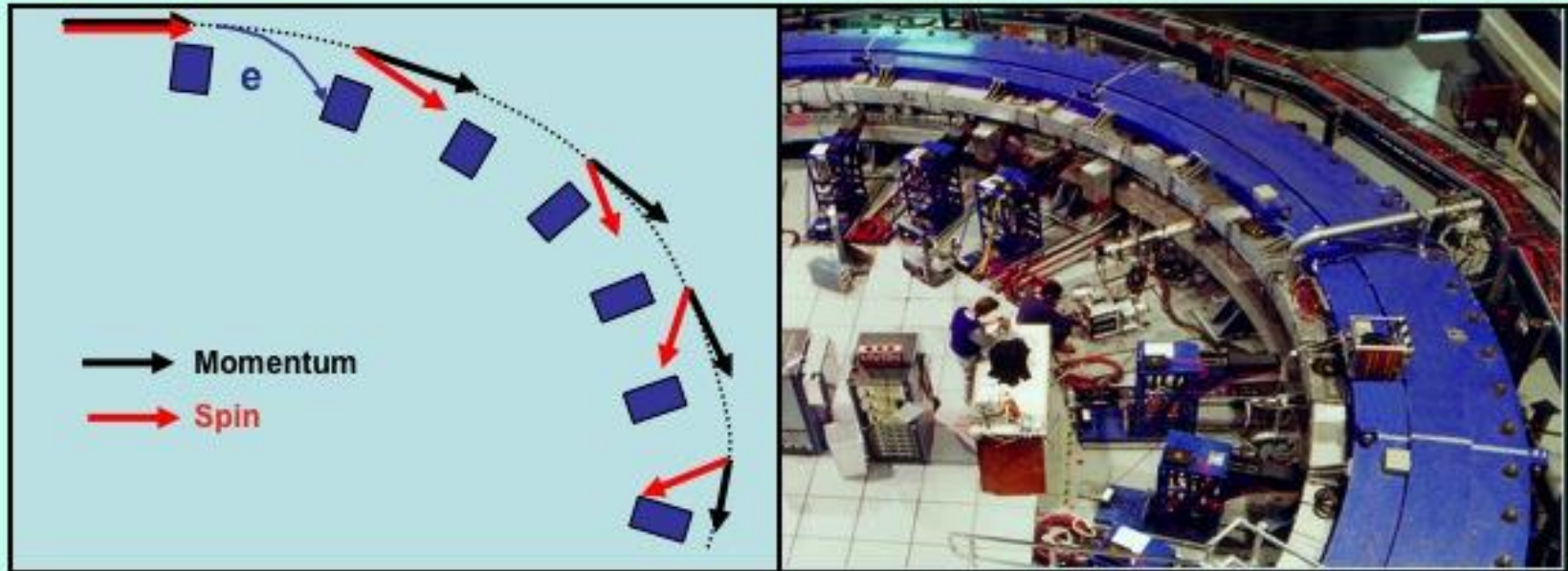
**D. Hertzog, B.L. Roberts...**

# BNL Muon $g-2$ Experiment



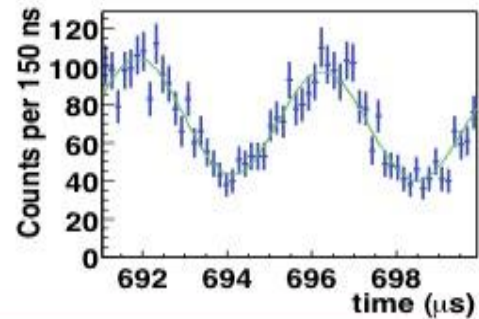
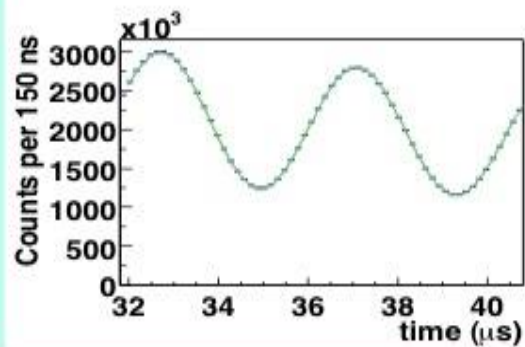
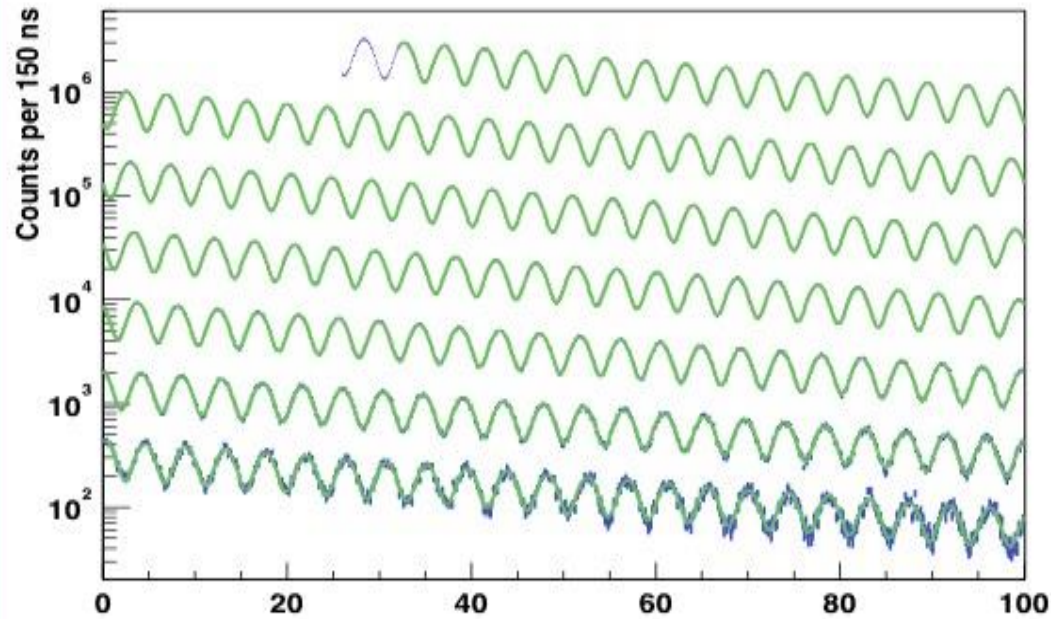


- $a_{\mu}$  is proportional to the difference between the spin precession and the rotation rate



$$\Delta\omega = \omega_a = \left( \frac{g - 2}{2} \right) \frac{eB}{mc}$$

$$N(t) = N_0 e^{-t/\tau} [1 + A \cos(\omega_a t + \phi)]$$



# Standard Model Prediction

$$a_{\mu}^{\text{SM}} = a_{\mu}^{\text{QED}} + a_{\mu}^{\text{EW}} + a_{\mu}^{\text{Hadronic}}$$

## QED Contributions:

- $a_{\mu}^{\text{QED}} = 0.5(\alpha/\pi) + 0.765857425(17)(\alpha/\pi)^2 + 24.05050996(32)(\alpha/\pi)^3 + \underline{130.8796(63)}(\alpha/\pi)^4 + 753.29(1.04)(\alpha/\pi)^5 + \dots$

## 2012 Update: Aoyama, Hayakawa, Kinoshita, & Nio

$$\alpha^{-1(^{87}\text{Rb})} = 137.035999049(90)$$

$$a_{\mu}^{\text{QED}} = \underline{116584718.864(36)} \times 10^{-11} \text{ Very Precise!}$$

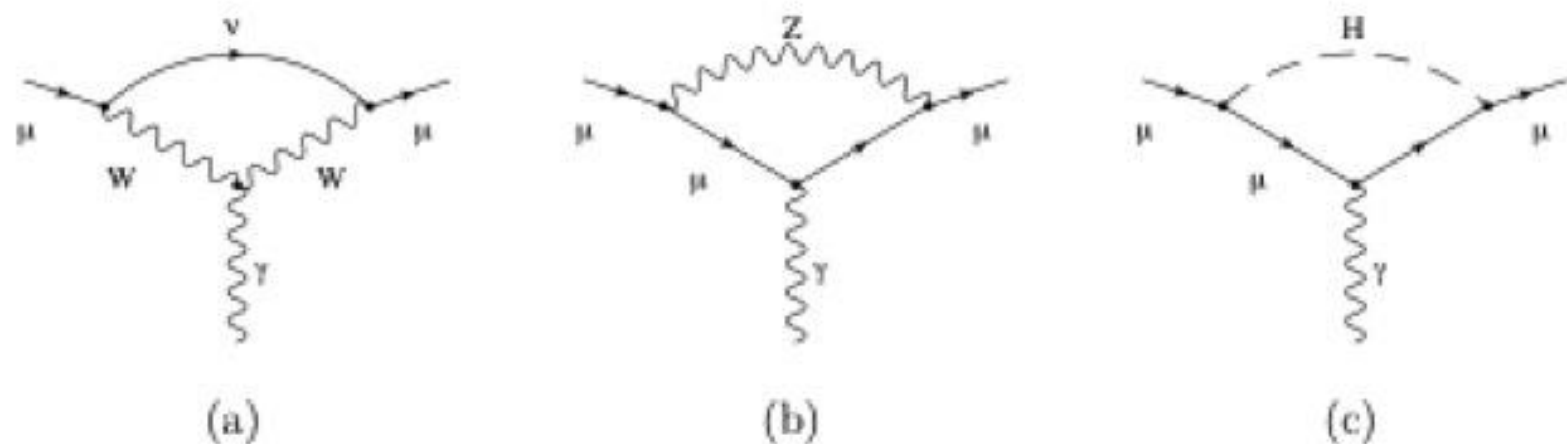


Figure 2: One-loop electroweak radiative corrections to  $a_\mu$ .

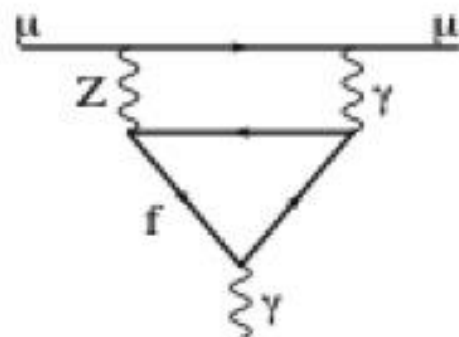


FIG. 3: Effective  $Z\gamma\gamma^*$  coupling induced by a fermion triangle, contributing to  $a_\mu^{\text{EW}}$ .

# Electroweak Loop Effects

$a_{\mu}^{\text{EW}}(1 \text{ loop}) = \underline{194.8 \times 10^{-11}}$  original goal of E821

$a_{\mu}^{\text{EW}}(2 \text{ loop}) = \underline{-40.3(1.0) \times 10^{-11}}$  (Higgs Mass = 126 GeV)

3 loop EW leading logs very small  $O(10^{-12})$

•  $a_{\mu}^{\text{EW}} = \underline{154(1) \times 10^{-11}}$  ***Non Controversial***

## Hadronic Contributions (HVP & HLBL)

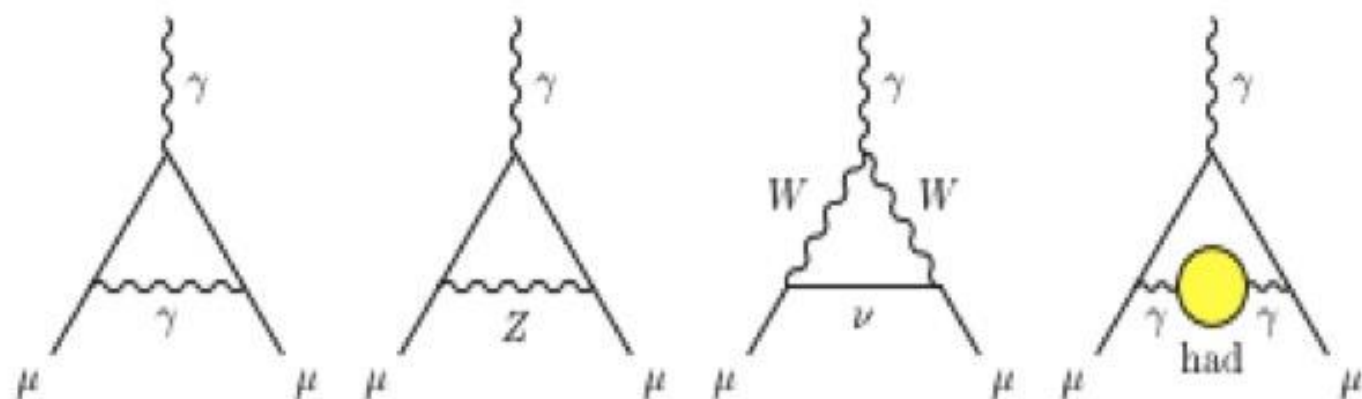
$a_{\mu}^{\text{Had}}(\text{V.P.})^{\text{LO}} = \underline{6923(40)(7) \times 10^{-11}}$  (Hoecker update 2010)

$a_{\mu}^{\text{Had}}(\text{V.P.})^{\text{NLO}} = -98(1) \times 10^{-11}$

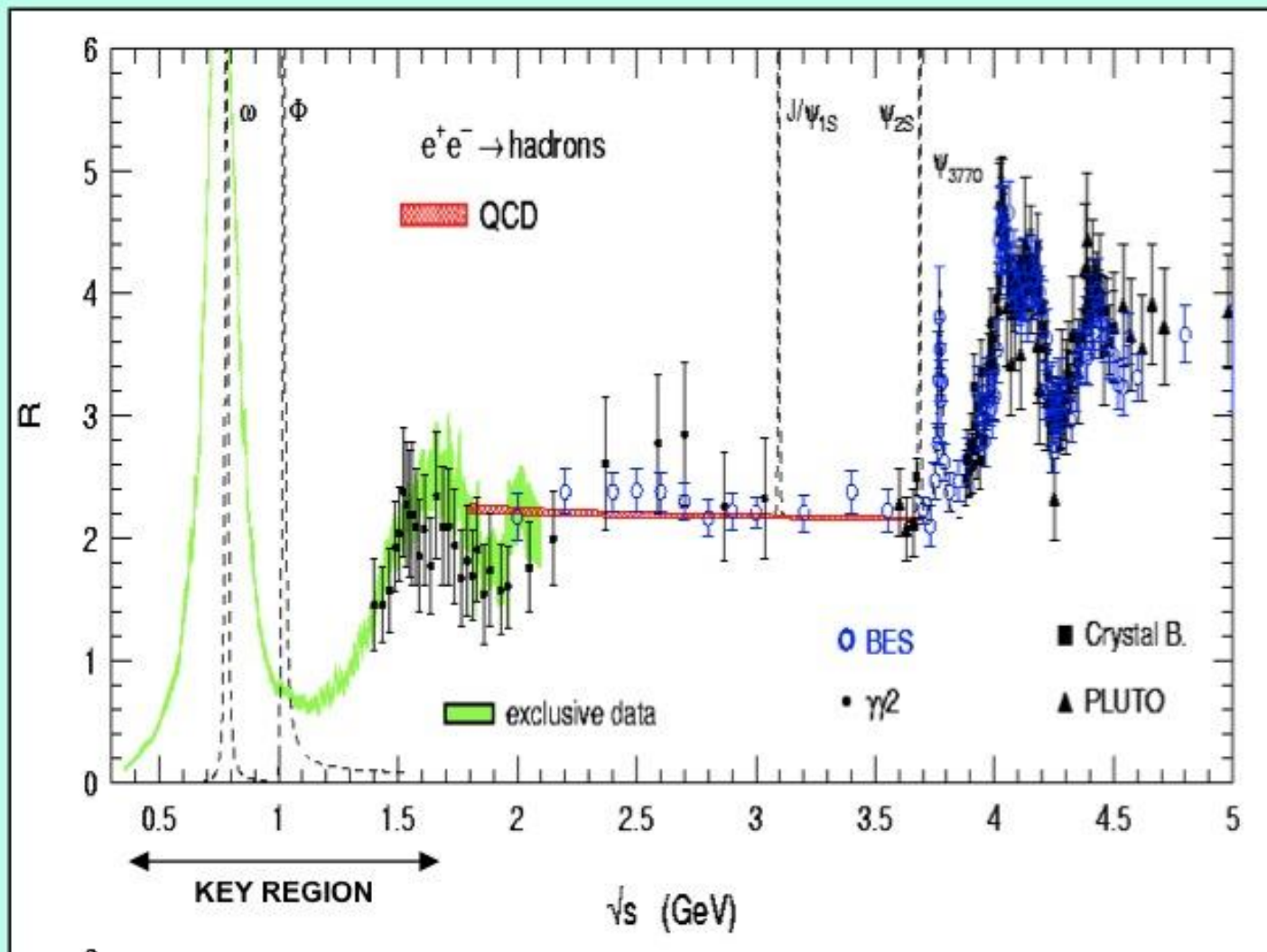
$a_{\mu}^{\text{Had}}(\text{LBL}) = 105(26) \times 10^{-11}$  (Consensus?)

$a_{\mu}^{\text{SM}} = \underline{116591803(49) \times 10^{-11}}$  (*Future Improvement?*)

$\Delta a_{\mu} = a_{\mu}^{\text{exp}} - a_{\mu}^{\text{SM}} = \underline{286(63)(49) \times 10^{-11}}$  (***3.6 $\sigma$  deviation!***)



**Figure 1:** Representative diagrams contributing to  $a_{\mu}^{\text{SM}}$ . From left to right: first order QED (Schwinger term), lowest-order weak, lowest-order hadronic.



From  $e^+e^- \rightarrow \text{hadrons}$  data + dispersion relation

$$a_\mu^{\text{Had}}(\text{V.P.})^{\text{LO}} = \underline{6923(40)(7)} \times 10^{-11} \text{ (Hoecker update 2010)}$$

$$\underline{3 \text{ loop}} = a_\mu^{\text{Had}}(\text{V.P.})^{\text{NLO}} + a_\mu^{\text{Had}}(\text{LBL})$$

$$a_\mu^{\text{Had}}(\text{V.P.})^{\text{NLO}} = -98(1) \times 10^{-11}$$

$$a_\mu^{\text{Had}}(\text{LBL}) = 105(26) \times 10^{-11} \text{ (Consensus?)}$$

Prades, de Rafael, Vainshtein

$$a_\mu^{\text{Had}} = 6930(40)(7)(26) \times 10^{-11} \approx 46 a_\mu^{\text{EW}}$$

$$a_\mu^{\text{SM}} = \underline{116591803(49)} \times 10^{-11}$$



# Comparison of Experiment and Theory

(Most Recent)

- $\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 286(63)(49) \times 10^{-11}$  ( $3.6\sigma!$ )

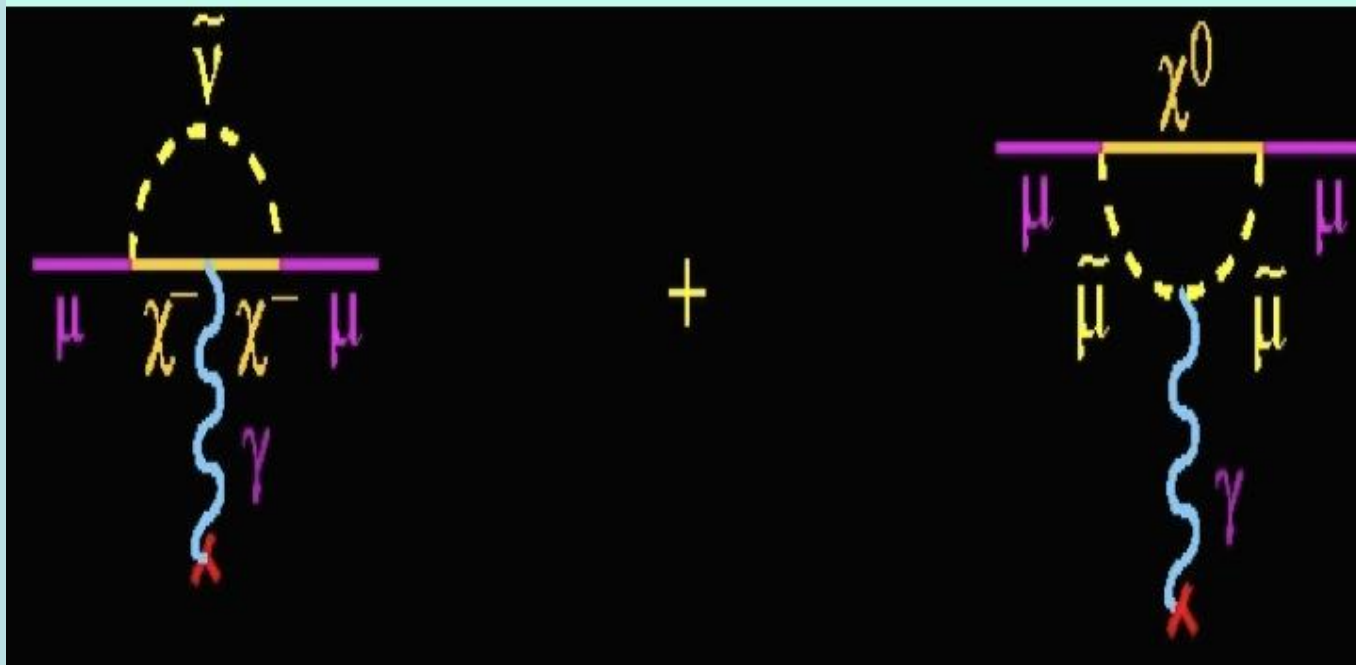
**This is a very large deviation!**

Remember, the EW contribution is  
only  $154 \times 10^{-11}$

**New Physics Nearly 2x Electroweak?**

Why don't we see it in other measurements?

3.2 “New Physics” Effects  
SUSY 1 loop  $a_\mu$  Corrections  
**(Most Likely Scenario)**



- SUSY Loops are like EW, but depend on:
- 2 spin 1/2  $\chi^-$  (charginos)
- 4 spin 1/2  $\chi^0$  (neutralinos) including dark matter!
- spin 0 sneutrinos and sleptons with **mixing!**
  
- Enhancement factor  $\tan\beta = \langle\phi_2\rangle / \langle\phi_1\rangle \sim 3-40!$

# Interpretations

$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 286(80) \times 10^{-11} \quad (3.6\sigma!)$$

## Generic 1 loop SUSY Contribution:

$$a_\mu^{\text{SUSY}} = (\text{sgn}\mu) 130 \times 10^{-11} (100 \text{ GeV} / m_{\text{susy}})^2 \tan\beta$$

$\tan\beta \approx 3-40$ ,  $m_{\text{susy}} \approx 100-500 \text{ GeV}$  Some LHC-MSSM Tension

Other Explanations: *Hadronic  $e^+e^-$  Data? HLBL(3loop)?*

*Lattice Gauge Theory Efforts!*

**Multi-Higgs Models**

**Extra Dimensions  $< 2 \text{ TeV}$**

\* Dark Photons  $\sim 10-200 \text{ MeV}$ ,  $\alpha' = 10^{-8}$

**Light Higgs Like Scalar  $< 10 \text{ MeV}$ ?**

*etc.*

“The deviation in  $a_\mu$  could be to Supersymmetry what the anomalous precession of the perihelion of Mercury was for General Relativity”

**J. Marburger**

Former U.S. Presidential Science Advisor  
(Former BNL Director)

If SUSY is responsible for  $g_\mu - 2$  Happy Days

Implications:  $\text{sgn}\mu > 0$  (dark matter searches easier)

**SUSY at LHC very likely (Eventually?)**

edms,  $\mu \rightarrow e\gamma$ , ... Good Bets

*So far not very Happy Days*

## Low Mass New Physics & g-2

Dark Photon  $m_{Z_d}$  of g-2 interpretation with  $\epsilon^2\alpha\sim 10^{-6}$   
easy to find at JLAB or Mainz (Bremsstrahlung)

$$e+X \rightarrow e+X+Z_d \quad (Z_d \rightarrow e^+e^-)$$

*Would Revolutionize Physics*

*Contact with Dark Matter!*

*Many Experimental Searches*

### Alternative

*Very Light Higgs like boson  $\leq 10\text{MeV}$*

*could also account for discrepancy*

*Who Ordered That?*

# *The Dark Boson – A Portal to Dark Matter*

What if some dark **sector** particles interact with one another via a new massive but relatively “light”  $Z_d$  (Dark Boson)?  
 $U(1)_d$  local gauge symmetry of the Dark Sector

Introduced for 1) Sommerfeld Enhancement

2)  $Z_d \rightarrow e^+e^-$  (source of positrons,  *$\gamma$ -rays*)

3) Cosmic Stability  $U(1)_d$

*eg Wimp Number (S. Weinberg!)*

\*4) Muon Anomalous Magnetic Moment

***Can we find direct evidence for such a particle (boson)?  
(or rule out some scenarios)***

# Dark Symmetry & Our World

**\*1. Kinetic  $U(1)_Y \times U(1)_d$  Mixing (B. Holdom)**

**\*2.  $Z$ - $Z_d$  mass mixing**

**3.  $U(1)_d = B-L, L_\mu-L_\tau, L_e-L_\mu, L_e-L_\tau \dots$**

**(All or some ordinary particles have dark charge)**

**$U(1)_d$  Vector Like Small Unquantized Couplings**

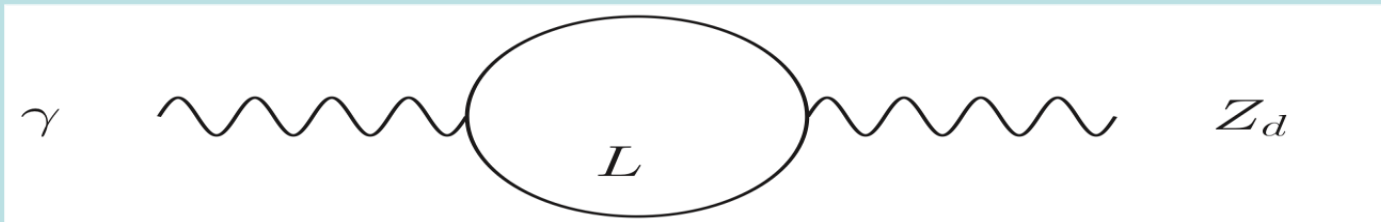


## Example

**One Loop gamma- $Z_d$  Kinetic Mixing  
(Through Heavy Charged Leptons)**

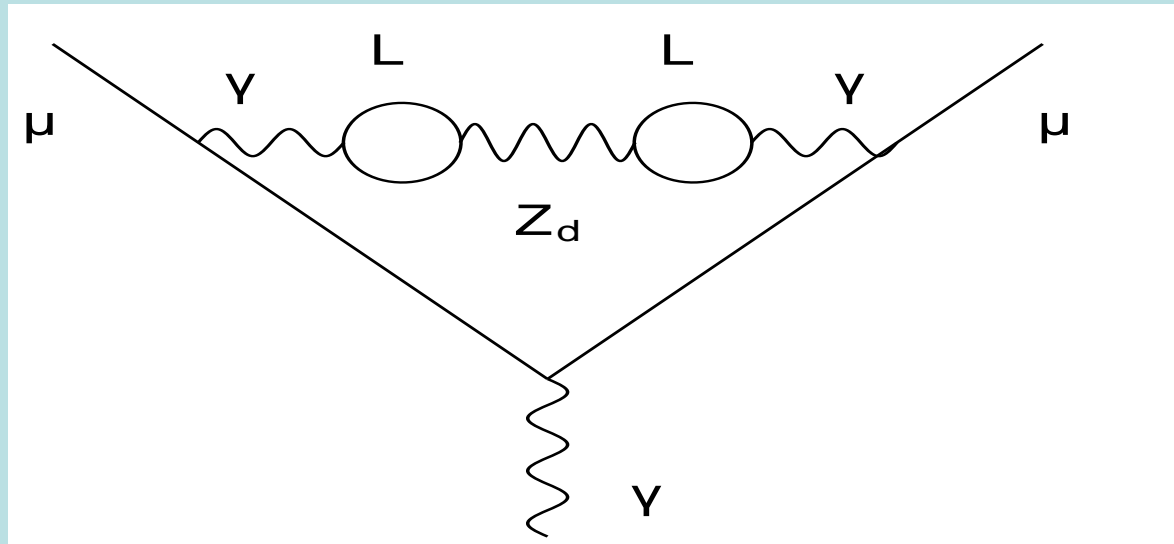
**That also carry  $U(1)_d$  charge**

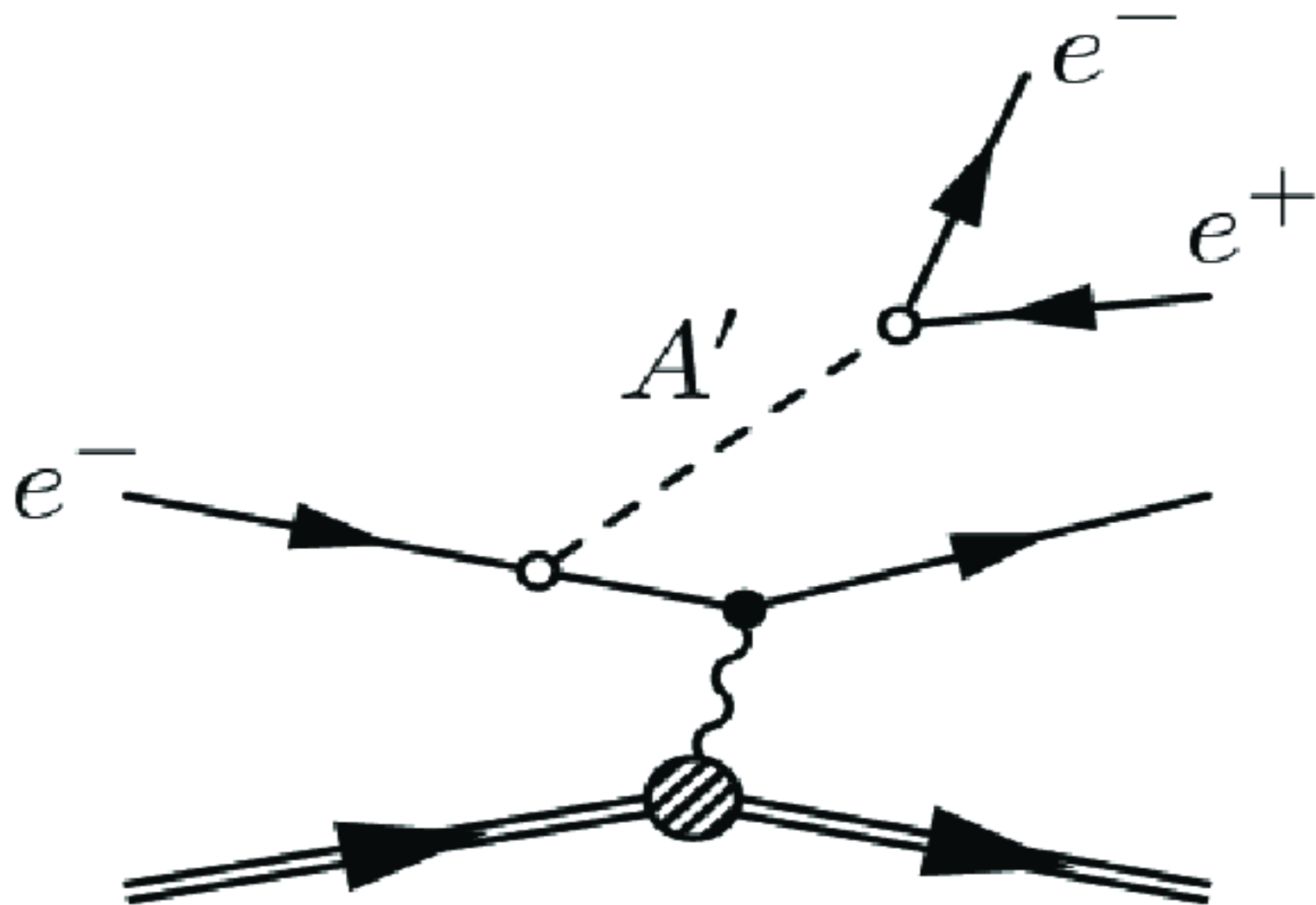
**Expect  $\epsilon \sim eg_d/8\pi^2 \approx O(10^{-3})$**



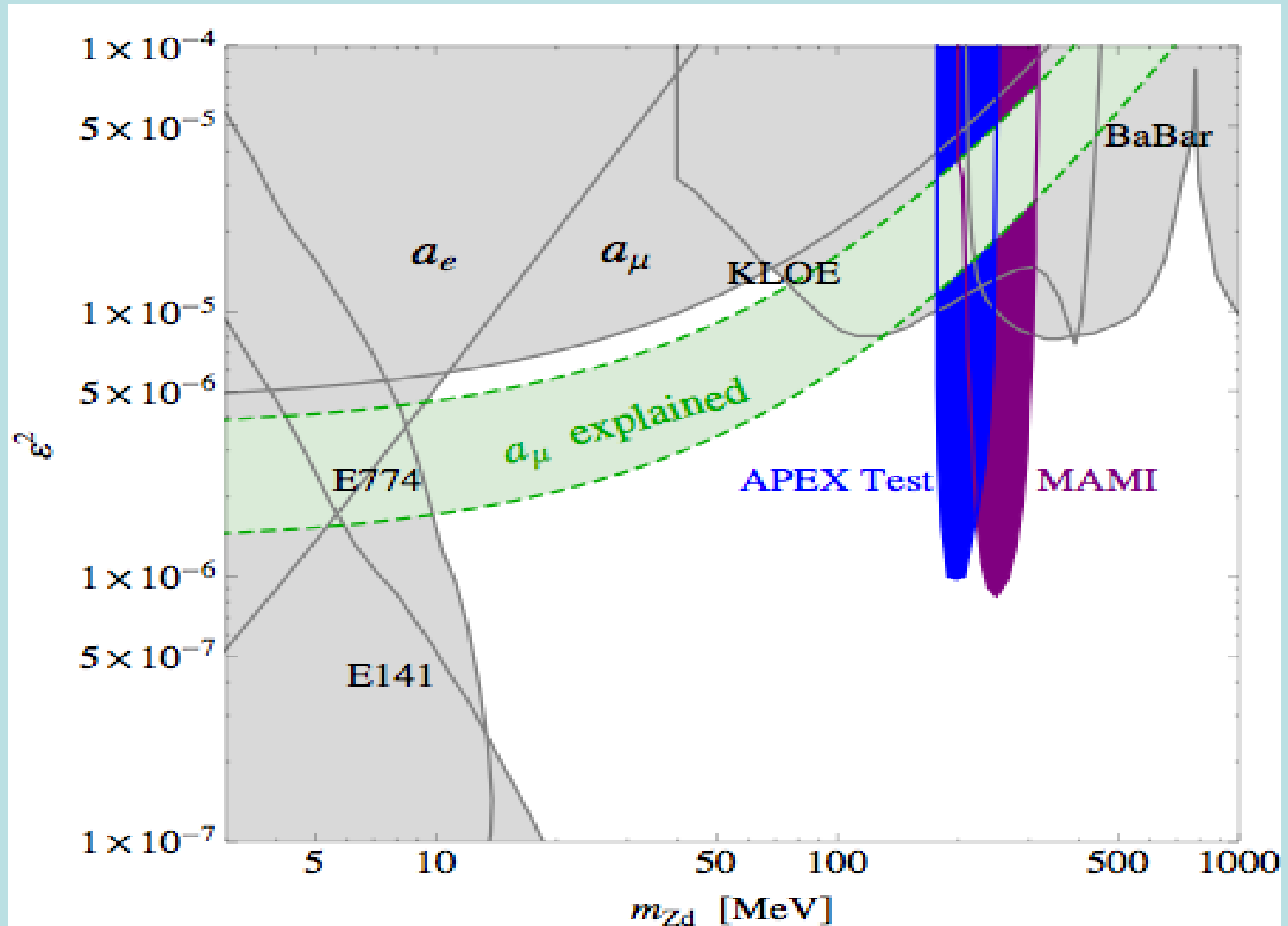
# Effective 3 loop $g_\mu$ -2 Diagram

$a_\mu^{Z_d} = \alpha/2\pi\epsilon^2 F(m_{Z_d}/m_\mu)$ ,  $F(0)=1$  solves  $g_\mu$ -2 discrepancy  
for  $\epsilon^2 \approx 3-5 \times 10^{-6}$  &  $m_{Z_d} \approx 20-50 \text{ MeV}$  (see figure)

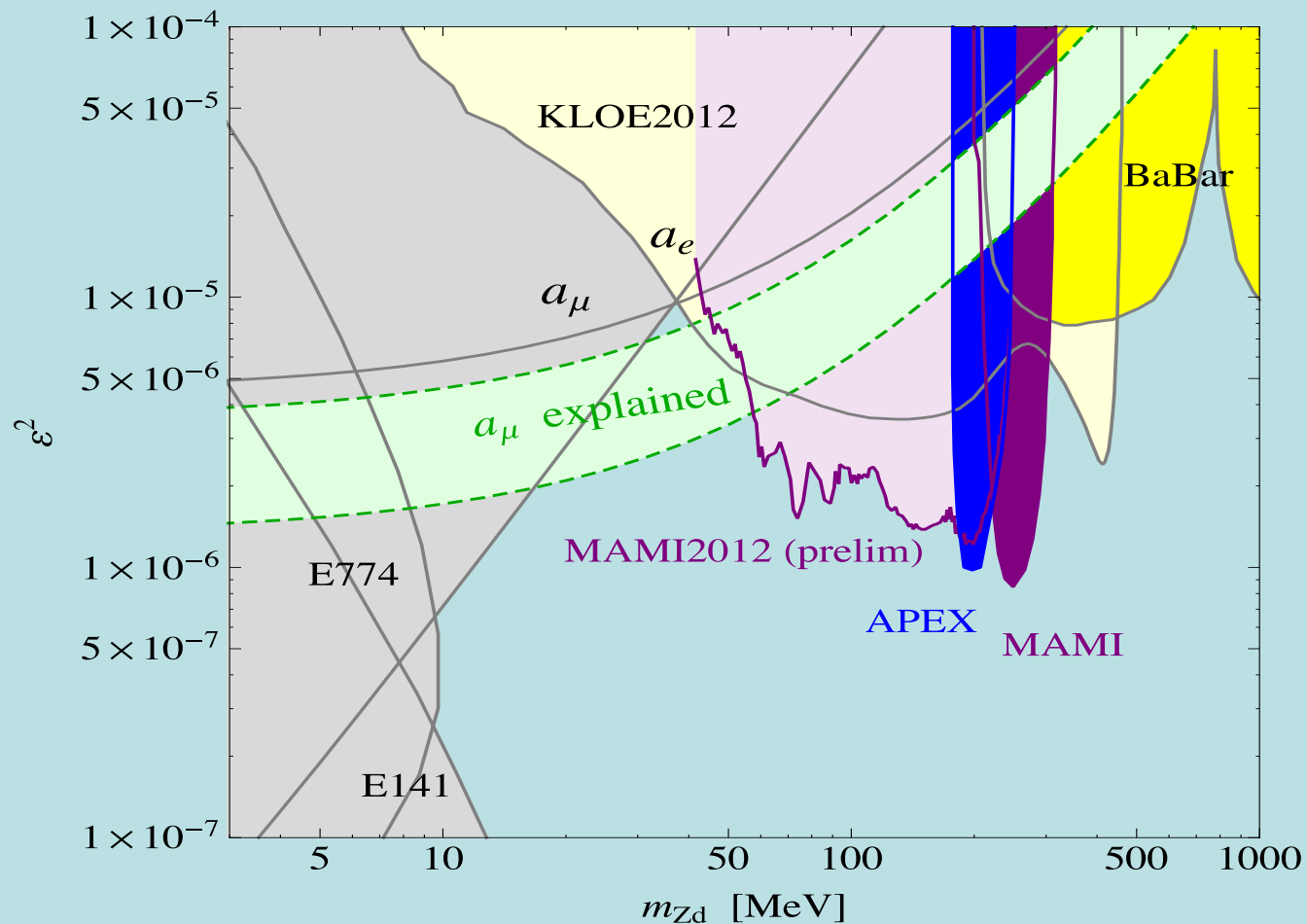




# Dark Photon Exclusion Early 2012



Recent Updates  $\rightarrow$  20 MeV-50 MeV Left  
2013 COSY  $\pi^0 \rightarrow \gamma Z_d \rightarrow e^+e^-$  Not Shown



#### 4.) *Muonic Hydrogen Lamb Shift*

In an effort to precisely determine  $r_p$

New PSI  $\mu p$  atomic Lamb shift experiment

$$\Delta E(2P_{3/2}-2S_{1/2})=209.9779(49)-5.2262r_p^2+0.0347r_p^3 \text{ meV}$$

*R. Pohl, A. Antognini et al. Nature July 2010*

*Very Elegant!*

Stop  $\mu^-$  in Hydrogen, About 1% populate 2S (1 $\mu$ sec)

Excite resonance with laser to 2P\1S

$\mu p$  atomic Lamb Shift very sensitive to  $r_p$

$(m_\mu/m_e)^3 = 8 \times 10^6$  enhancement

Proton Finite Size  $\approx -2\%$

*20ppm experiment*

*12years in the making (1998-2010)*

$$\Delta E(2P_{3/2}-2S_{1/2})^{\text{exp}} = 206.2949 \pm 0.0032 \text{ meV}$$

$$r_p = \underline{0.84184(67)}\text{fm} \quad (\mu\text{p atom})$$

*10x More Precise & 5 sigma below ep value!*

$$r_p \simeq \underline{0.8768(69)}\text{fm} \quad (\text{ep atom})$$

Confirmation from ep scattering

$$r_p \simeq \underline{0.879(8)}\text{fm} \quad (\text{Recent Mainz})$$

$$r_p \simeq \underline{0.875(10)}\text{fm} \quad (\text{Recent JLAB})$$

***Current Electron Average:  $r_p = \underline{0.8772(46)}\text{fm}$***

***8 sigma below  $\mu\text{p atom}$ !***

Atomic ep Theory? Rydberg Constant( $R_\infty$ ) (Off by  $5\sigma$ ?)

**$R_\infty$  known to 13 significant figures!**

$$=1.0973731568527(73)\times 10^7\text{m}^{-1}$$

”One of the Two most accurately measured fundamental physical constants”.

***Could  $R_\infty$  really be wrong?***

***also***

***What about ep scattering? Wrong!***

**Perhaps the most likely solution**



***$\mu$ p atomic theory or experiment wrong?***

Proton Polarizability? QED Corrections ( $\gamma\gamma$ )?

$\mu$ p Experiment? (seems solid)

Follow up Experimental & Theoretical Work  
appear to confirm original results!

***Can all three  $r_p$  determinations be correct?***

2 out of 3 correct?...

# ***New “Light” Vector or Scalar Boson?***

Light Vector Boson with coupling  $e'$

$$e'^2/4\pi = \alpha' \ll \alpha = 1/137$$

New Vector Boson Interaction Shifts Atomic Spectrum  
in a way that mimics a proton charge radius

(Based on calculation by A. Czarnecki)

$$\Delta r_p / r_p \sim -2\alpha' / \alpha^3 (1 + m_V / \alpha m_\mu)^2$$

Experiment  $\rightarrow \Delta r_p / r_p \sim -4\%$

**example  $\alpha' = 2.5 \times 10^{-6} \alpha$ ,  $m_V \leq 1 \text{ MeV}$  works**

(Heavier  $m_V$  requires larger coupling)

Can it be the “Dark Photon”?

Light gauge boson from Dark Matter Sector  
that mixes with the photon (small coupling)

# “New Physics” & The $g_\mu-2$ Discrepancy

$$a_\mu = (g_\mu - 2)/2$$

$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 286(63)(49) \times 10^{-11} \quad (3.6\sigma!)$$

What about light vector boson with  $m_{Z_d} < m_\mu$ ?

$$\begin{aligned} \Delta a_\mu &\sim \alpha' / 2\pi \quad \text{like Schwinger term} \\ &= 2.9 \times 10^{-9} \rightarrow \alpha' \sim 2.5 \times 10^{-6} \alpha \end{aligned}$$

**Dark Photon = natural solution to  $g_\mu-2$  Discrepancy**

So, a light vector boson with mass  $O(1\text{MeV})$   
and  $\alpha' \sim 2.5 \times 10^{-6} \alpha$  coupling for  $\mu p$  and  $\mu\mu$   
solves both proton size puzzle &  $g_\mu-2$

***Can it be the Dark Photon?***

**No!** O(1MeV) dark photon would also reduce  $r_p$  in ep atom

***(Observation of Czarnecki & Pospelov)***

and should have led to  $g_e$ -2 discrepancy

$$\Delta a_e = |a_e^{\text{exp}} - a_e^{\text{SM}}| < 10^{-11}!$$

**Possible Solution: violate e- $\mu$  Universality**

Egs Gauge B-3L $_{\mu}$  or B-3/2(L $_{\mu}$ +L $_{\tau}$ )... (Lee & Ma)

Anomaly Free, couples to baryons, **not electrons**

**So, a light  $m_V \sim \text{MeV}$  &  $\alpha' \sim 2.5 \times 10^{-6} \alpha$  alleviates both  $r_p$  and  $a_{\mu}$  problems if it doesn't couple (directly) to electrons!**

**What about neutrino physics? ( $\nu_{\mu}$  vs  $\nu_e$ ) Matter effect!**

3  $r_p$  determinations: ep atom, ep scattering,  $\mu p$  atom  
something likely wrong but which one(s)?

**Rydberg Constant Vulnerable**

*What if it shifts by 5 sigma?*

*but ep remains a problem?*

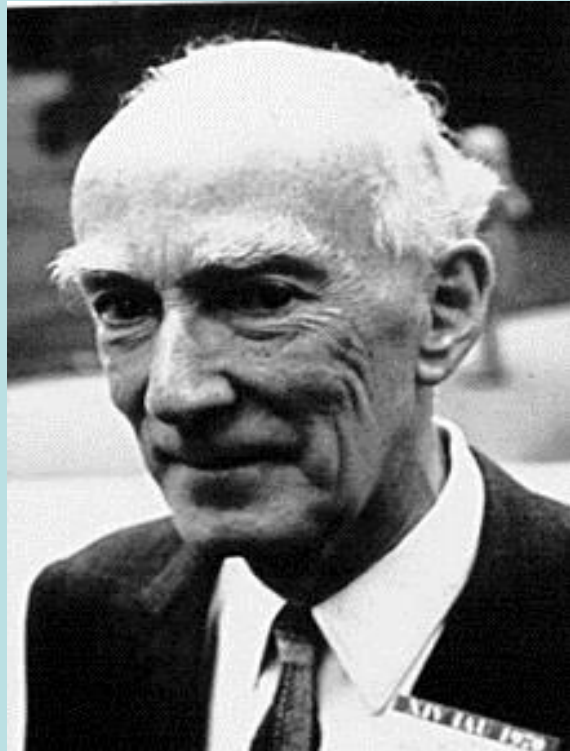
Then  $m_V \sim \text{MeV}$  &  $\alpha' \sim 2.5 \times 10^{-6} \alpha$  solves both  $r_p$  &  $a_\mu$   
discrepancies. **Other constraints?**  $a_e$ ? ...

**Precision QED remains interesting & timely**

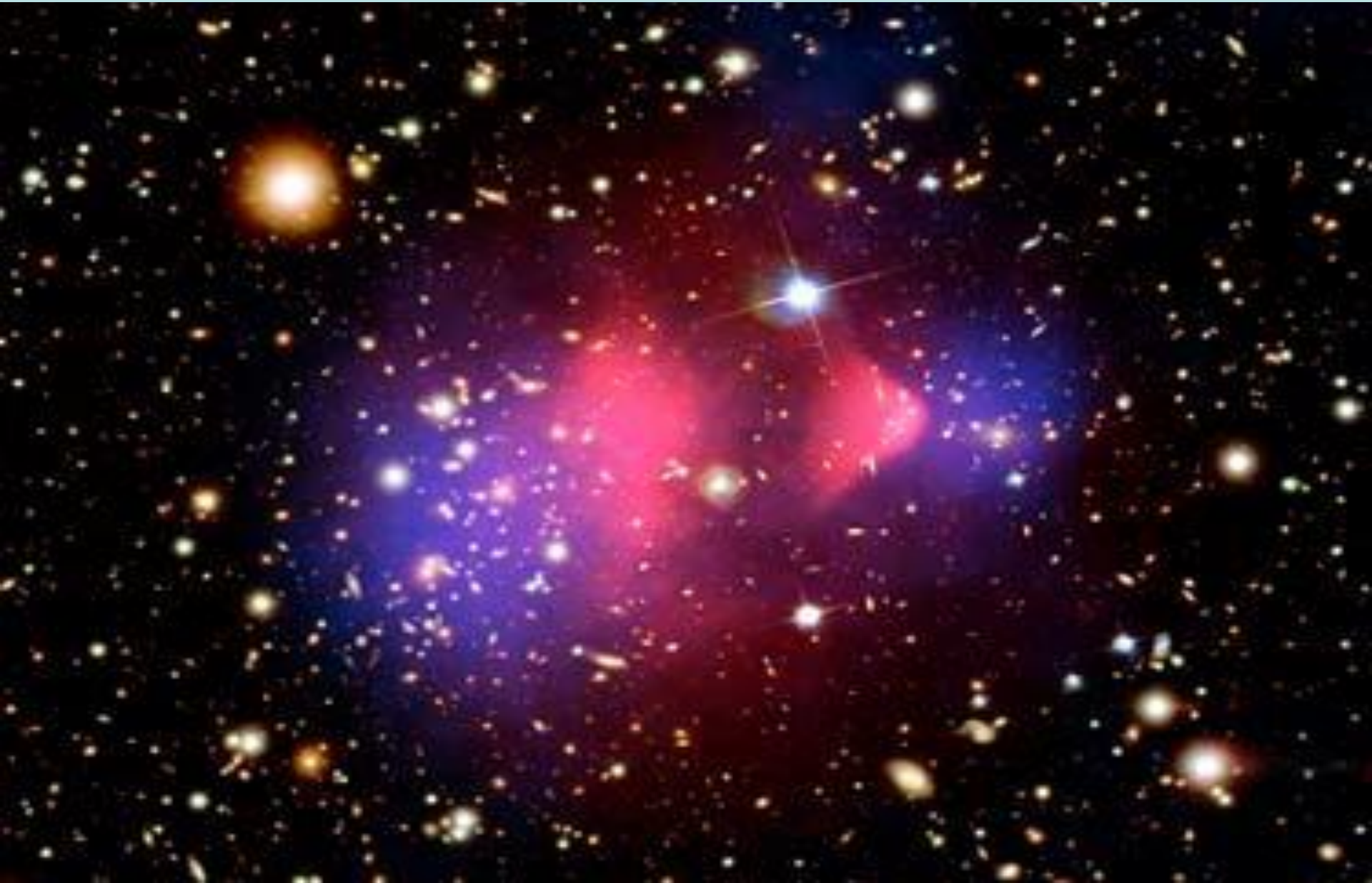
*Stay Tuned For Future Developments*

(About the same time antiparticles were being discovered) 1932-33's Astronomers start to see "Dark Matter" Evidence!

## Jan Ort & Fritz Zwicky



# *Bullet Galaxy Cluster*



# *What is the Dark Matter?*

Light Matter-Ordinary Particles (Galaxies, Stars, Us)

= 3-4% Of Universe (many varieties)

Dark Matter = 22% Of Universe – Gravitational Interactions

Dark Energy = 75% Of Universe – Cosmological Constant

*Is dark matter a single **stable** new elementary particle?*

*How Heavy is it? Spin (0,1/2,1,3/2)?*

*Does it interact only gravitationally?*

*Does it have antiparticle partner(s)? (Asymmetry?)*

Are there many species of dark particles (most unstable)

Does Dark Matter have gauge interactions? Dark Charge?



# *The Hunt For Dark Particles*

- Underground Searches for Dark Matter Particles (WIMPS)

## *Conflicting Experimental Results*

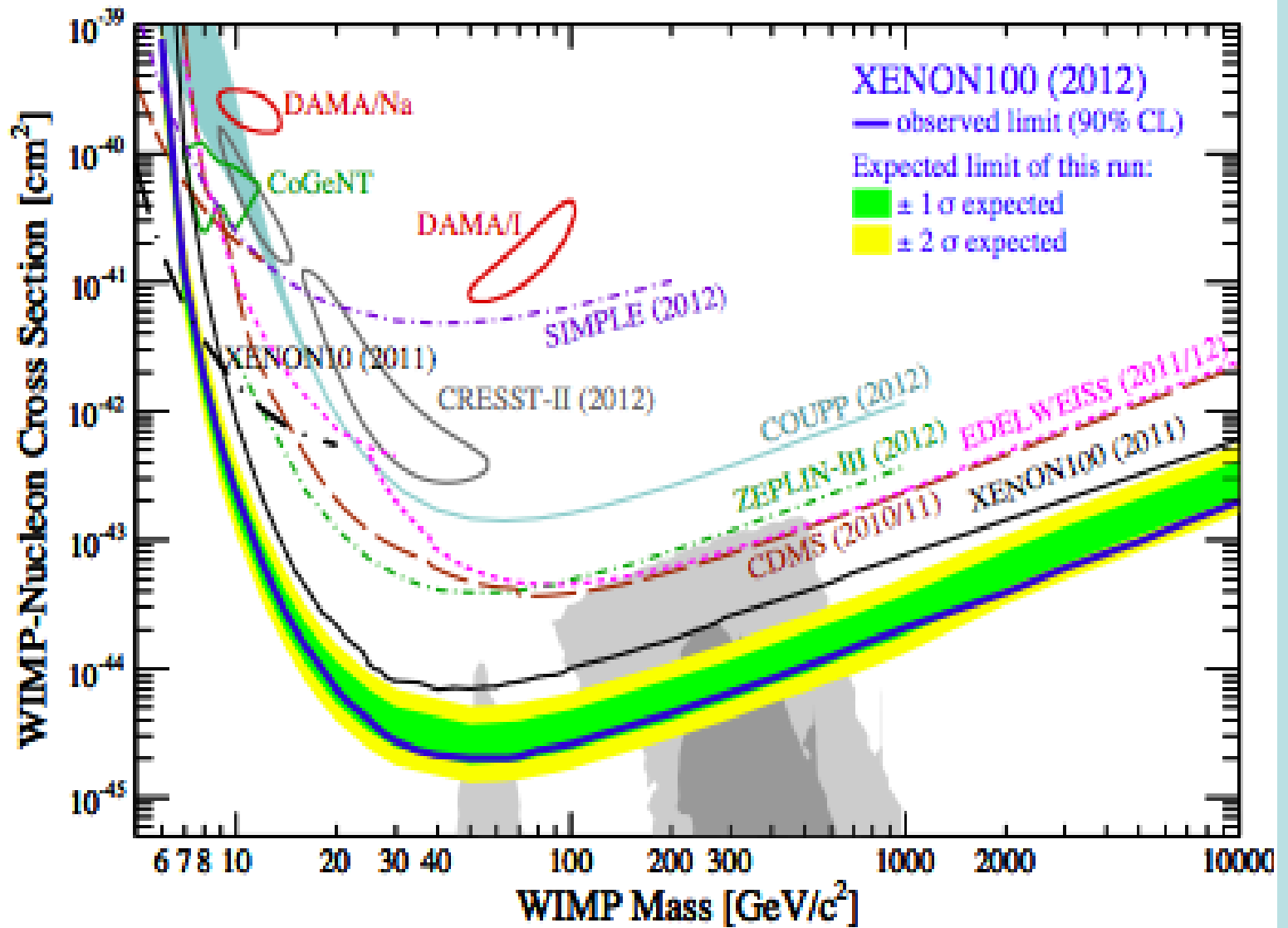
Astrophysics - Possible Hints of Dark Particle Annihilations

LHC (Supersymmetry – Other?) No direct detection yet

## *The Dark Photon – A Possible Portal to Dark Matter*

What if dark particles interact weakly with one another via a new massive but relatively “light”  $\gamma_d$  (Dark Photon) ?

***Can we find evidence for such a particle?***



# Astrophysics: Hints of Dark Particle Annihilations

## Light or Heavy Dark Matter Particles?

**Positron ( $e^+$ ) Excesses at high energies(?)**

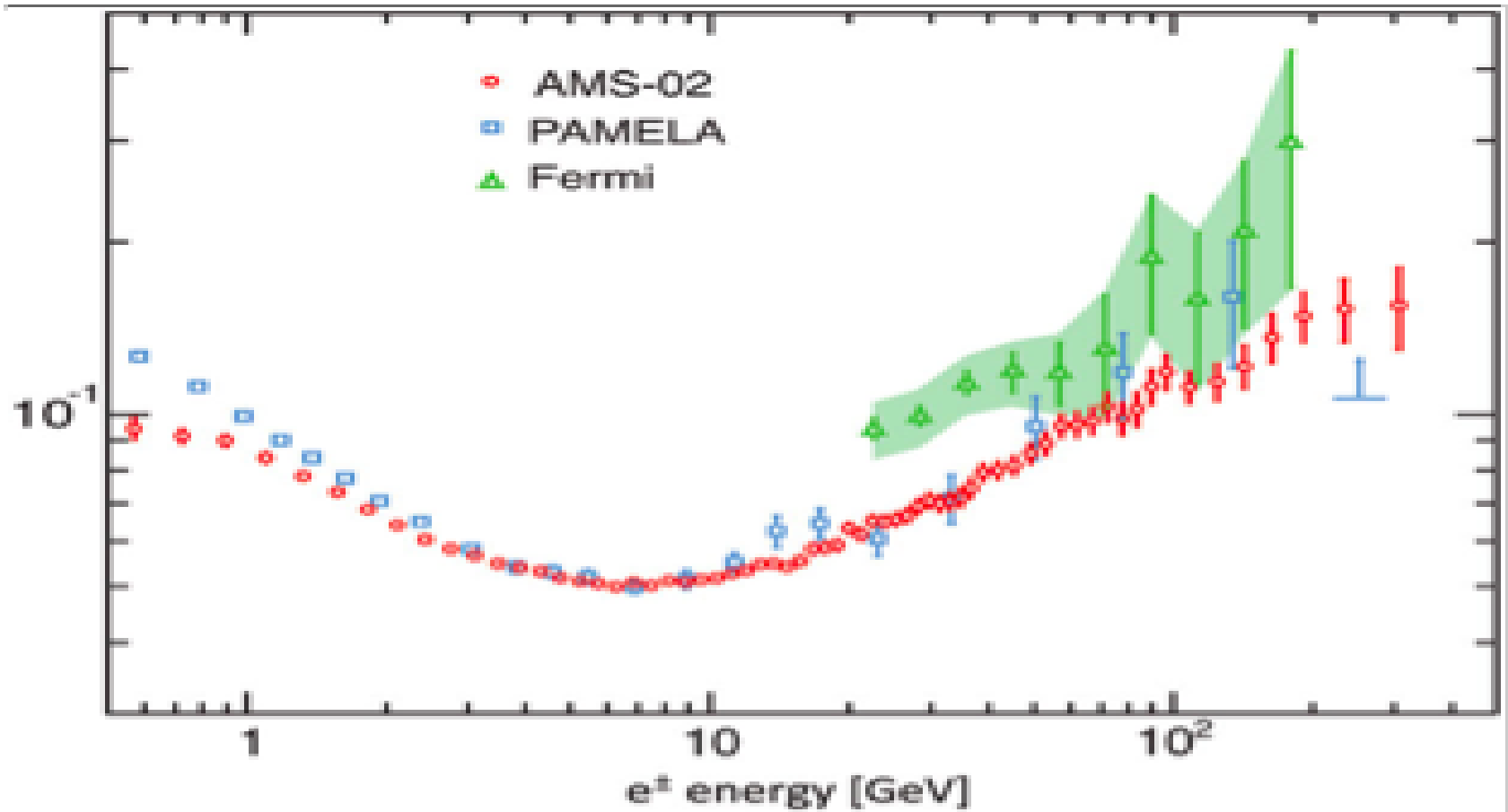
Pamela, Fermi, AMS (Heavy Dark Matter) > TeV? (Unlikely Interpretation?)

Fermi  $\gamma$ -ray Excess from Galactic Center

**Light  $\sim 10$  GeV Dark matter annihilations ( $\rightarrow e^+e^-, \mu^+\mu^-, \tau^+\tau^-$ )**

Both Interesting Effects

Interpretations?



positron fraction as measured by the AMS (red circles) from 1 to 350 GeV. (Courtesy: *Phys. Rev. Lett.* **110** 141102)

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# $\gamma_d$ coupling to our particle world

- **Very Weak < 0.0001x electromagnetism**

Nevertheless, produce in electron scattering

detect  $\gamma_d \rightarrow e^+e^-$

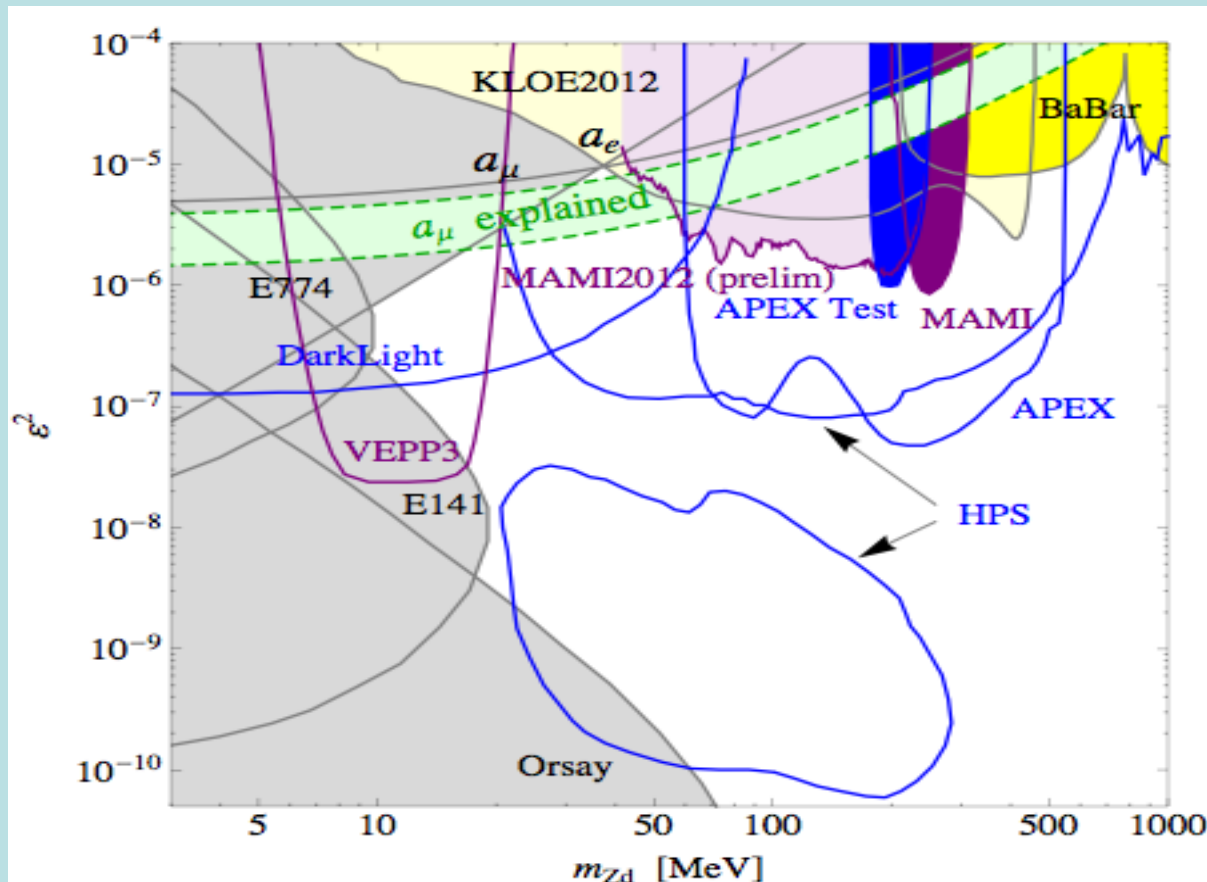
Experiments at JLAB and MAMI (Mainz) in Progress

More planned for the future

So far, no direct signal – but much territory needs to be explored

# Current Bounds & Future Dark Photon Sensitivity

Assumes  $\text{Br}(Z_d \rightarrow e^+e^-) = 1$  What if  $Z_d \rightarrow$  missing energy?



# Meanwhile

**1950 Purcell & Ramsey Speculate P may be violated**

**Begin search for neutron edm**

**T (CP) violation also needed for edms!**

**P & T Violation \ EDMs for all particles with spin**

**CKM CP Violation \ unobservably small edms**

**EDMs: Window to Early Universe CP Violation!**

**“New Physics” Source of CP Violation Needed!**

**Supersymmetry Leading Candidate**

**(Not observed at LHC yet! Some Tension!)**

# Great Future Expectations

- $d_n \rightarrow 10^{-27} - 10^{-28}$  e-cm Neutron Spallation/Reactor Sources
- $d_e \rightarrow 10^{-29}$  e-cm or better!
- $d_p$  &  $d_D \rightarrow 10^{-28} - 10^{-29}$  e-cm Storage Ring Proposal (BNL/COSY)

Pave the way for a **new generation** of storage ring experiments  $d_p$ ,  $d_D$ ,  $d(^3\text{He})$ ,  $d(\text{radioactive nuclei})$ ,  $d_\mu$

Several orders of magnitude improvement expected



# Vector-like Heavy Leptons Dark Variant Example - Davoudiasl, Lee & WJM

- Example: A Possible Dark Sector

Two Left Handed Doublets  $(N_i^0, E_i^-)_L$   $i=1,2$

Two Right-Handed Doublets  $(N_i^0, E_i^-)_R$

Dark Charges  $\pm 1$

Four Left Handed Singlets  $N_{jL}, E_{jL}$   $j=3,4$

Four Right Handed Singlets  $N_{jR}, E_{jR}$

Dark Charges  $\pm 1$

Gauge Invariant Mass Terms + Higgs Couplings  $\rightarrow$  Mixing

All interactions vector-like under  $SU(2)_L \times U(1)_Y \times U(1)_d$

4 Charged & 3 Neutral Leptons Unstable

**Lightest Neutral: Potential Stable Dark Matter?**

## $a_f$ vs $d_f$ (very roughly)

- Two loop Higgs contribution:  $a_\mu(H) \approx \text{few} \times 10^{-11}$   
 $a_e(H) \approx 5 \times 10^{-16}$

**Unobservably Small!**

Two Loop Higgs contribution:  $d_e(H) \approx 10^{-26} \sin\phi$  e-cm  
 $|d_n(H)| \approx |d_p(H)| \approx 3 \times 10^{-26} \sin\phi$  e-cm

Already  $d_e$  bound implies  $\sin\phi \leq 0.1$  (smaller?)

**CP violation in  $H(\bar{\nu}\nu)$**   $\sin^2\phi \leq 0.01$

***Unlikely to be observable, but edm experiments can  
Explore down to  $\sin\phi \approx O(10^{-3})$ ! Unique!***

# Anomalous Dipole Moments

fermion	$a_f^{\text{exp}}$	$ d_f(e/2m_f)^{\text{exp}} $
e	0.00115965218073(28)	$<1 \times 10^{-16}$
$\mu$	0.00116592089(63)	$<3 \times 10^{-6}$
p	1.792158142(28)	$<3 \times 10^{-12}$ ( $d_{\text{Hg}}$ )
n	-1.9130427(5)	$<1 \times 10^{-13}$

“New Physics” expected to scale as  $(m_f/\Lambda)^2$   
 $(m_\mu/m_e)^2 \approx 43000$  Muon only  $a_f$  sensitive to high  $\Lambda \sim 2\text{TeV}$ !

All  $d_f$  sensitive to “New Physics” if  $\tan\phi^{\text{NP}}$  not too small  
Nucleon edms Isovector or isoscalar? Mixed?  
Both  $d_n$  and  $d_p$  need to be measured!

## Some Dipole Moments

fermion	$a_f^{\text{exp}}$	$d_f^{\text{exp}} \times (2m_f/e)$
e	0.00115965218073(28)	$< 5 \times 10^{-17}$
$\mu$	0.00116592089(63)	$< 3 \times 10^{-6}$
p	1.792158142(28)	$< 3 \times 10^{-12}$ (from $d_{\text{Hg}}$ )
n	-1.9130427(5)	$< 1 \times 10^{-13}$

“Heavy New Physics” expected to scale as  $(m_f/\Lambda)^2$   
 $(m_\mu/m_e)^2 \approx 43000$  Muon only  $a_f$  sensitive to high  $\Lambda$ !

All  $d_f$  sensitive to “New Physics” if  $\tan\phi^{\text{NP}}$  not too small  
Nucleon edms Isovector or isoscalar? Mixed?  
Both  $d_n$  and  $d_p$  (as well as  $d_D$ ) need to be measured!

## *Future Expectations*

- $d_n \rightarrow 10^{-27}-10^{-28}$ e-cm Spallation Neutron Sources
- $d_p$  &  $d_D \rightarrow 10^{-28}-10^{-29}$ e-cm Storage Ring Proposal (BNL/COSY)  
Probes New Physics(NP) at  $(1\text{TeV}/\Lambda_{\text{NP}})^2 \tan\phi_{\text{NP}} \leq 10^{-7}$ !  
for  $\phi_{\text{NP}} \sim O(1) \rightarrow \Lambda_{\text{NP}} \sim \underline{3000\text{TeV}}$ ! (**well beyond LHC**)  
Paves the way for a **new generation** of storage ring  
experiments  $d_p$ ,  $d_D$ ,  $d(^3\text{He})$ ,  $d(\text{radioactive nuclei})$ ,  $d_\mu$
- $d_e \rightarrow 10^{-30}$ e-cm or better!
- $d_\mu \rightarrow 10^{-24}$ e-cm Storage Ring Proposal

# Baryogenesis & New Physics CP Violation

Examples of New Physics Models with potentially large CP Violation: Supersymmetry, Multi-Higgs, L-R Models, 4th Generation, Extra Dimensions...  
Dark Matter Sector...Higgs CP Violation

- Generic Manifestation - **Electric Dipole Moments**

**What is the “New Physics”?**

**Look for EDMs!**

**No Standard Model Background (too small)**