



Spettroscopia Adronica

Diego Bettoni
Anno Accademico 2012-2013

Outline

- Introduction To QCD
- Theories and Models
 - Effective Field Theories
 - Lattice QCD
- Hadron Configurations
- Antiproton-proton Annihilations
- Experimental Results
 - Hybrids
 - Glueballs
 - Multiquarks
 - $D_{(s)}$ systems

Introduzione alla QCD

QCD (Quantum ChromoDynamics)

La QCD è la teoria dei quark, gluoni e delle loro interazioni.

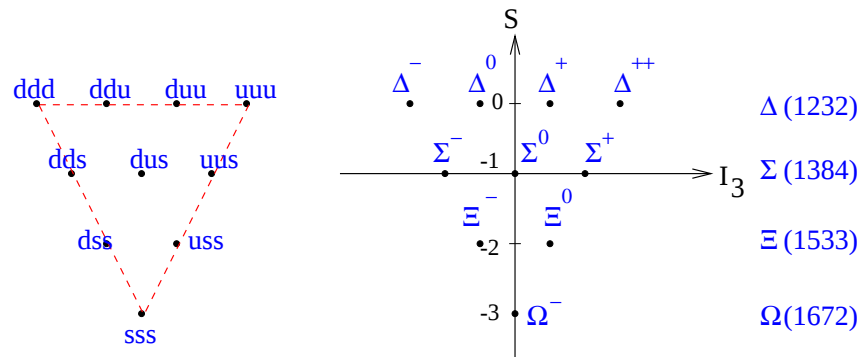
Fa parte del Modello Standard. E' una teoria di campo quantistica con una lagrangiana semplice ed elegante che si basa interamente sulla invarianza per trasformazioni di un gruppo di gauge locale, $SU(3)_{\text{colore}}$.

Gli adroni sono composti da quark. Le forze tra quark all'interno degli adroni sono più semplici delle forze tra adroni, nello stesso modo in cui le interazioni coulombiane all'interno di un atomo sono più semplici delle interazioni interatomiche.

I quark si presentano in sei flavor (u, d, s, c, b, t). Simmetria $SU(3)_{\text{flavor}}$ (approssimata).

Simmetria di colore $SU(3)_{\text{colore}}$ esatta.

Il Decupletto Barionico



- Hanno **spin-parità** $J^P = \frac{3}{2}^+$
- La **funzione d'onda è simmetrica** rispetto allo scambio di una qualsiasi coppia di quark.
- Si trovano in **onda s**, hanno **spin paralleli**, quindi anche le funzioni d'onda spaziale e di spin sono simmetriche.

Principio di Pauli ? La soluzione sta nel fatto che i quark hanno un ulteriore grado di libertà interno, il **colore**, che può assumere i 3 valori **R, G, B**. I quark formano il tripletto fondamentale di una simmetria SU(3) di colore.

Gli adroni sono **neutri** dal punto di vista del colore, cioè appartengono a una rappresentazione di **singoletto di SU(3) di colore**. In questo modo la funzione d'onda è antisimmetrica.

$$(qqq)_{c.s.} = \sqrt{\frac{1}{6}}(RGB - RBG + BRG - BGR + GBR - GRB)$$

Il colore

Per uno stato di tre quark scriviamo la funzione d'onda come

$$\psi_{3q} = \psi_{spazio} \psi_{spin} \psi_{flavor} \psi_{colore}$$

il prodotto delle prime tre funzioni d'onda è simmetrico per lo scambio di due quark, per cui richiediamo che la parte di colore sia antisimmetrica

$$\psi^{\alpha} \quad (\alpha = 1, 2, 3)$$

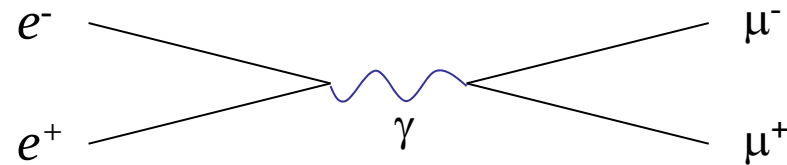
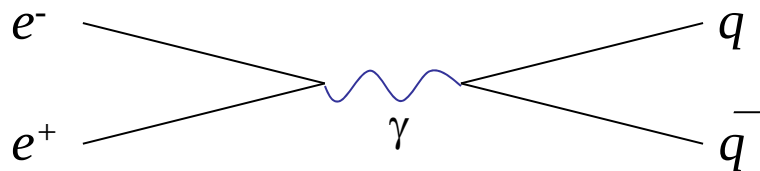
$$\psi_{colore} = \varepsilon_{\alpha\beta\gamma} \psi^{\alpha} \psi^{\beta} \psi^{\gamma}$$

- Ogni flavor esiste in tre colori, che si trasformano tra di loro sotto $SU(3)_{colore}$. (rappresentazione 3_c).
- Tutti gli adroni osservati sono singoletti di colore. (rappresentazione 1_c)

Il processo $e^+e^- \rightarrow \text{adroni}$

La produzione di adroni in annichilazione e^+e^- avviene per adronizzazione delle coppie $q \bar{q}$ prodotte nel processo $e^+e^- \rightarrow q \bar{q}$.

La sezione d'urto totale si dunque collegare a quella per $e^+e^- \rightarrow \mu^+\mu^-$.



$$\sigma(e^+e^- \rightarrow \mu^+\mu^-) = \frac{4\pi}{3} \frac{\alpha^2}{s}$$

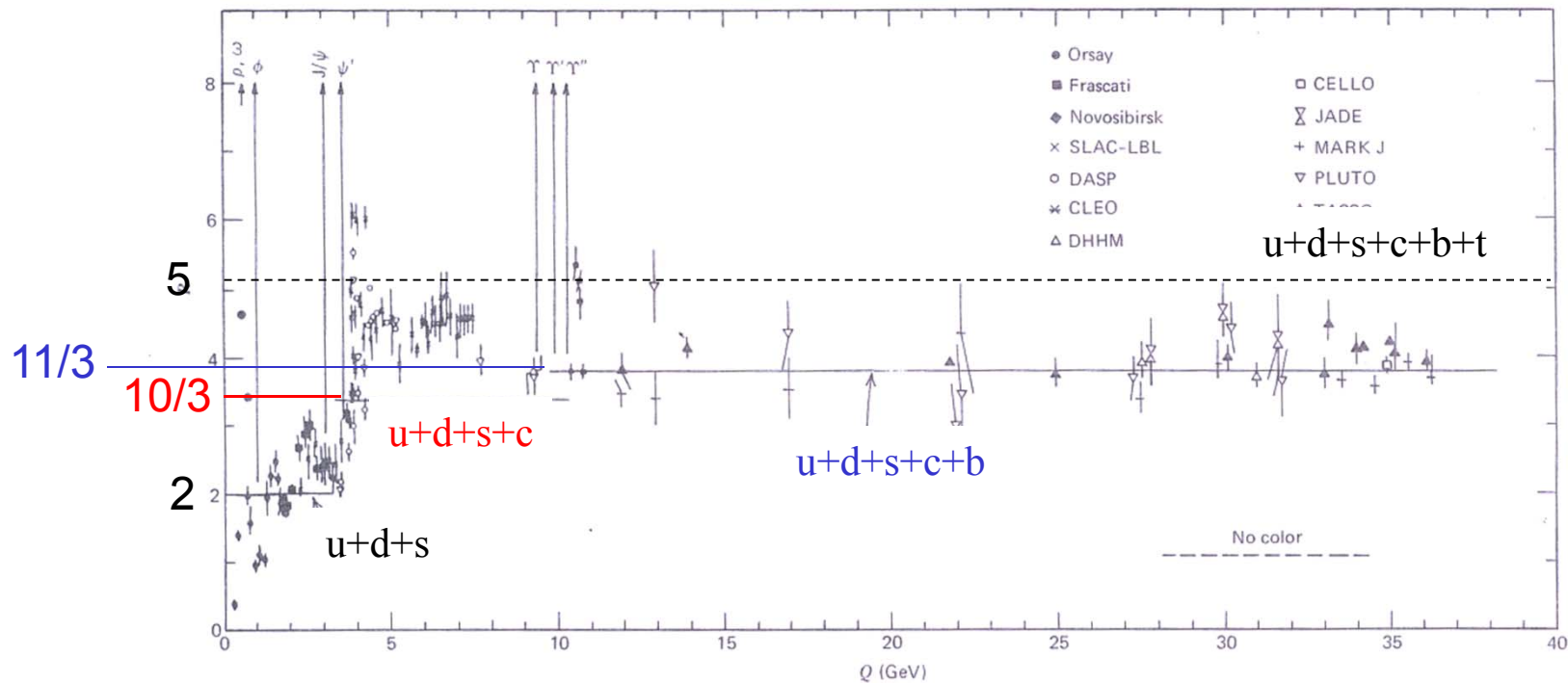
$$\sigma(e^+e^- \rightarrow q\bar{q}) = 3e_q^2 \sigma(e^+e^- \rightarrow \mu^+\mu^-)$$

$\downarrow$
 colore

$$e_q = \begin{cases} -\frac{1}{3} & q = d, s, b \\ +\frac{2}{3} & q = u, c, t \end{cases}$$

$$\sigma(e^+e^- \rightarrow \text{adroni}) = \sum_q 3e_q^2 \sigma(e^+e^- \rightarrow \mu^+\mu^-)$$

$$R \equiv \frac{\sigma(e^+e^- \rightarrow \text{adroni})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)} = 3 \sum_q e_q^2$$



All'aumentare dell'energia, il rapporto R aumenta ogni volta che si supera la soglia per produrre un nuovo flavour. La misura di R conferma anche che i quark si presentano in tre colori.

correzioni di QCD

$$R = 3 \sum_q e_q^2 \left(1 + \frac{\alpha_s(Q^2)}{\pi} \right)$$

Alla simmetria di colore $SU(3)_c$ è associata l'invarianza delle leggi della fisica sotto la trasformazione globale non abeliana di fase:

$$\psi' = e^{i\alpha_j \lambda_j / 2} \psi \quad (j = 1, \dots, 8)$$

La trasformazione locale di fase genera una teoria dinamica che necessita dell'introduzione di **8 bosoni vettoriali** di gauge (perchè ci sono 8 generatori in $SU(3)$) che mediano le forze tra quark. Questi quanti dell'interazione forte sono chiamati **gluoni** e appartengono alla rappresentazione di **ottetto di $SU(3)_c$** (8_c). La simmetria di colore è esatta per cui i gluoni hanno **massa nulla**.

Questa **teoria di gauge non abeliana** è la QCD.

La natura non abeliana della teoria la rende asintoticamente libera, cioè le interazioni tra quark tendono (logaritmicamente) a zero a piccole distanze.

La Lagrangiana della QCD

I fermioni elementari della QCD, i quark, appaiono in sei flavor e sono raggruppati in un campo $\psi(x) = (u(x), d(x), s(x), c(x), b(x), t(x))^T$ dove $u(x)$, $d(x)$ etc sono spinori di Dirac a 4 componenti.

La Lagrangiana della QCD è data da:

$$\mathcal{L}_{QCD} = \bar{\psi} \left(i \gamma_\mu \mathcal{D}^\mu - m \right) \psi - \frac{1}{4} G_{\mu\nu}^j G_j^{\mu\nu}$$

con la derivata covariante:

$$\mathcal{D}_\mu = \partial_\mu - ig \sum_{j=1}^8 \frac{\lambda_j}{2} \mathcal{A}_\mu^j(x)$$

e il tensore del campo gluonico:

$$G_{\mu\nu}^i(x) = \partial_\mu \mathcal{A}_\nu^i(x) - \partial_\nu \mathcal{A}_\mu^i(x) + gf_{ijk} \mathcal{A}_\mu^j(x) \mathcal{A}_\nu^k(x)$$

λ_j Matrici di Gell-Mann

f_{ijk} Costanti di Struttura

$\mathcal{A}_\mu^j$ Gluoni

La rinormalizzazione della teoria introduce una scala di energia: la costante di accoppiamento g diventa una “running coupling constant”, cioè dipende dalla scala di energia μ alla quale viene valutata.

Definendo $\alpha_s(\mu) = g^2(\mu)/4\pi$ si ha

$$\alpha_s(\mu) = \frac{4\pi}{\beta_0 \ln(\mu^2 / \Lambda^2)}$$

con $\beta_0 = 11 - 2N_f / 3$

N_f è il numero di flavor di quark.

Il parametro di scala Λ viene determinato empiricamente. Si ottiene

$\Lambda = 0.2 \text{ GeV}$ per $N_f = 4$.

La costante di accoppiamento diminuisce all'aumentare dell'energia: a scale $\mu \gg 1 \text{ GeV}$ l'interazione diventa debole e la QCD si può

trattare perturbativamente (**libertà asintotica**). $\alpha_s(M_Z) = 0.1176 \pm 0.0020$

A basse energie α_s diventa dell'ordine di 1 e si entra nel regime detto QCD non perturbativa.

Quarks

Light quarks

$$m_q \ll \Lambda_{\text{QCD}}$$

$q=u, d, s$

Heavy quarks

$$m_Q \gg \Lambda_{\text{QCD}}$$

$Q=c, b, t$

$$m_u = 1.5 \div 4.0 \text{ MeV}$$

$$m_d = 4 \div 8 \text{ MeV}$$

$$m_s = 80 \div 130 \text{ MeV}$$

“current quark masses” $\overline{\text{MS}}$ at scale 2 GeV

$$m_c = 1.15 \div 1.35 \text{ GeV}$$

$$m_b = 4.1 \div 4.4 \text{ GeV}$$

$$m_t = 174.3 \pm 5.1 \text{ GeV}$$

“running masses” in $\overline{\text{MS}}$ scheme

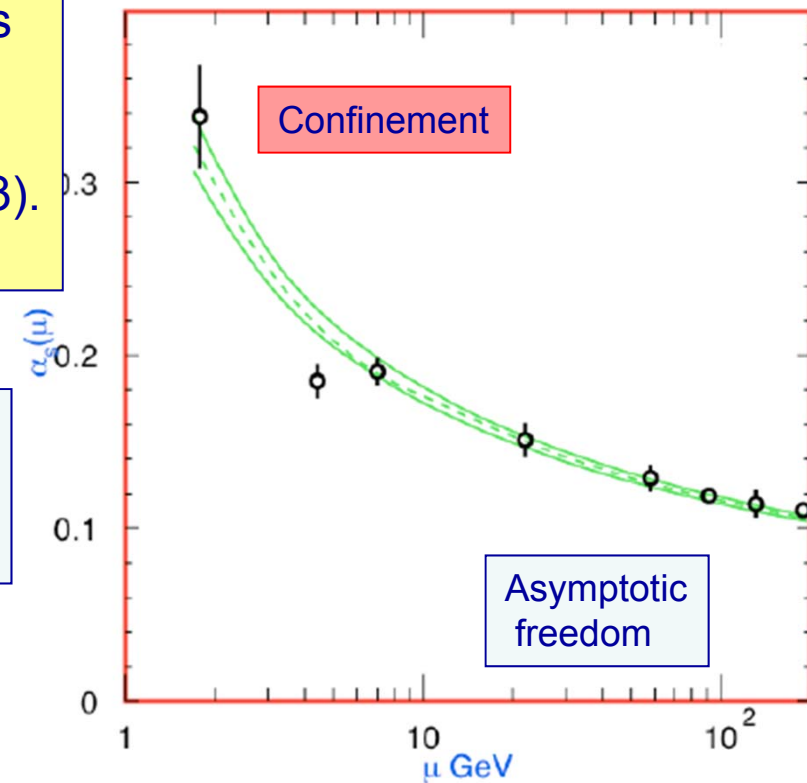
Hadrons containing heavy quarks have masses of order m_Q rather than of the order Λ_{QCD} .

QCD

The modern theory of the strong interactions is Quantum Chromodynamics (QCD), the quantum field theory of quarks and gluons based on the non abelian gauge group SU(3). It is part of the Standard Model.

At high energies, where the strong coupling constant α_s becomes small and perturbation theory applies, QCD is well tested.

In the low-energy regime, however, QCD becomes a strongly coupled theory, many aspects of which are not understood.



Regimi Asintotici

Ci sono due situazioni limite nelle quali la QCD è accessibile con approssimazioni controllate:

- Ad **alte energie** (piccole distanze < 0.1 fm) l'interazione diventa più debole e si entra nel regime perturbativo (**Libertà Asintotica**).
- A **basse energie** (grandi distanze > 1 fm) la QCD è caratterizzata dal **confinamento** e un vuoto non banale. Il confinamento implica la rottura spontanea di una simmetria che è esatta nel limite di massa nulla per i quark: **la simmetria chirale**. Questa rottura spontanea di simmetria a sua volta implica l'esistenza di tre bosoni di Goldstone pseudoscalari, identificati con i tre mesoni π nel limite di due flavor. Con tre flavor si generalizza all'ottetto pseudoscalare.

I due regimi vengono combinati a dare il potenziale:

$$V(r) = -\frac{4}{3} \frac{\alpha_s}{r} + \sigma r$$

Simmetria Chirale

Nel limite di massa zero per i quark, la Lagrangiana della QCD ha una simmetria globale legata alla chiralità conservata di particelle di massa zero e spin $\frac{1}{2}$.

Con due flavor ($N_f=2$):

$$\psi(x) = \begin{pmatrix} u(x) \\ d(x) \end{pmatrix} \quad \psi_{R,L} = \frac{1}{2}(1 \pm \gamma_5)\psi$$
$$\psi_R \rightarrow \exp\left[i\theta_R^a \frac{\tau_a}{2}\right]\psi_R \quad \psi_L \rightarrow \exp\left[i\theta_L^a \frac{\tau_a}{2}\right]\psi_L$$

Queste trasformazioni lasciano $\mathcal{L}_{\text{QCD}}$ invariata nel limite $m=0$: le componenti RH e LH dei quark non si mescolano.

$$SU(2)_R \times SU(2)_L$$

Simmetria Chirale della QCD

Sei correnti di Noether conservate:

$$J_{R,a}^\mu = \bar{\psi}_R \gamma_\mu (\tau_a / 2) \psi_R \quad J_{L,a}^\mu = \bar{\psi}_L \gamma_\mu (\tau_a / 2) \psi_L$$

$$\partial_\mu J_R^\mu = \partial_\mu J_L^\mu = 0$$

Corrente Vettoriale: $V_a^\mu = J_{R,a}^\mu + J_{L,a}^\mu = \bar{\psi} \gamma^\mu \frac{\tau_a}{2} \psi$

Corrente Assiale: $A_a^\mu = J_{R,a}^\mu - J_{L,a}^\mu = \bar{\psi} \gamma^\mu \gamma_5 \frac{\tau_a}{2} \psi$

Le cariche corrispondenti sono generatori di $SU(2) \times SU(2)$:

$$Q_a^V = \int d^3x \psi^\dagger(x) \frac{\tau_a}{2} \psi(x) \quad Q_a^A = \int d^3x \psi^\dagger(x) \gamma_5 \frac{\tau_a}{2} \psi(x)$$

Nella misura in cui si può considerare piccola la massa del quark strano ha senso generalizzare la simmetria chirale a 3 flavor $N_f=3$. In questo caso le 3 matrici di Pauli τ_a vengono sostituite dalle 8 matrici di Gell-Mann λ_a .

Rottura Spontanea della Simmetria Chirale

C'è evidenza dalla spettroscopia adronica che la **simmetria chirale** nel limite $m=0$ sia **rotta spontaneamente**. Per motivi dinamici lo stato di vuoto è **simmetrico solo sotto il sottogruppo $SU(2)_V$ generato dalla carica vettoriale Q^V** . Questa è la ben nota simmetria di isospin (per $N_f=2$) o simmetria di flavor (per $N_f=3$). Infatti se la simmetria non fosse rotta ci sarebbero dei doppietti di parità e i mesoni vettoriali ($J^P=1^-$) sarebbero degeneri con quelli assiali ($J^P=1^+$), mentre per esempio $M(\rho) = 0.77$ GeV e $M(a_1) = 1.23$ GeV. La simmetria chirale è rotta spontaneamente e si riduce a quella di isospin:

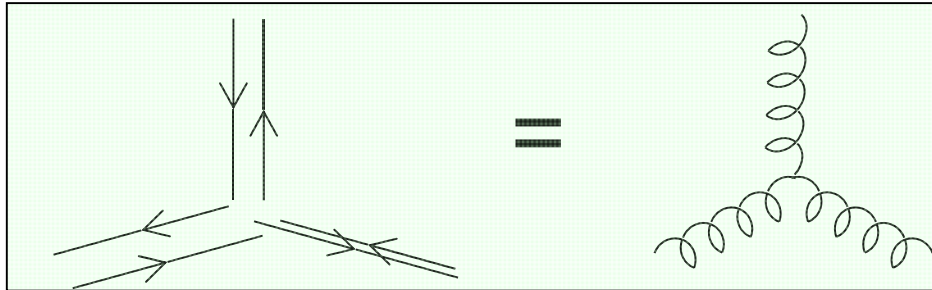
$$SU(2)_R \times SU(2)_L \rightarrow SU(2)_V$$

I bosoni di Goldstone sono i 3 π nel caso di due flavor e gli otto membri dell'ottetto mesonico nel caso di tre flavor.

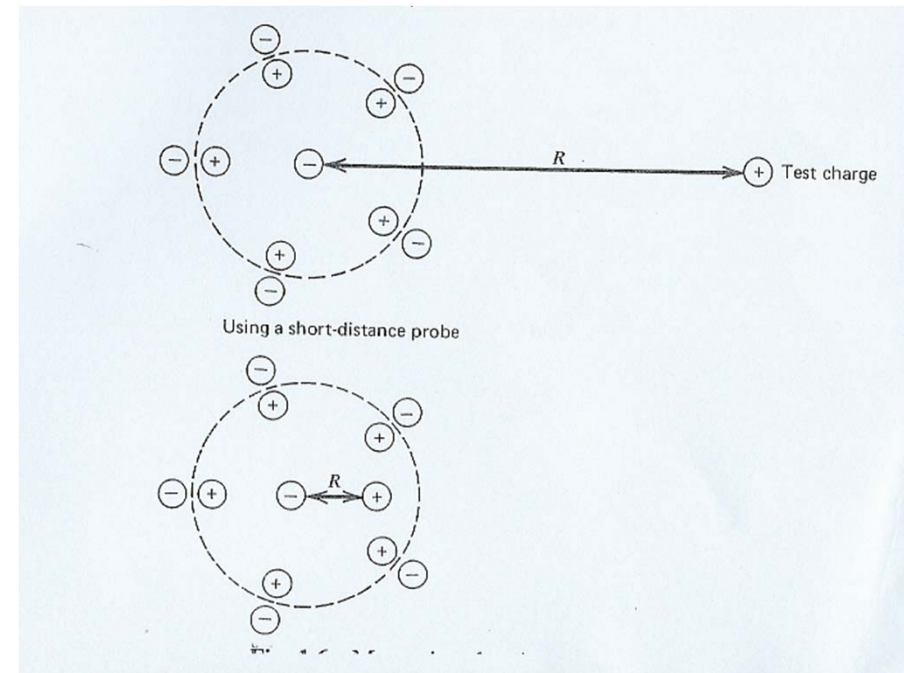
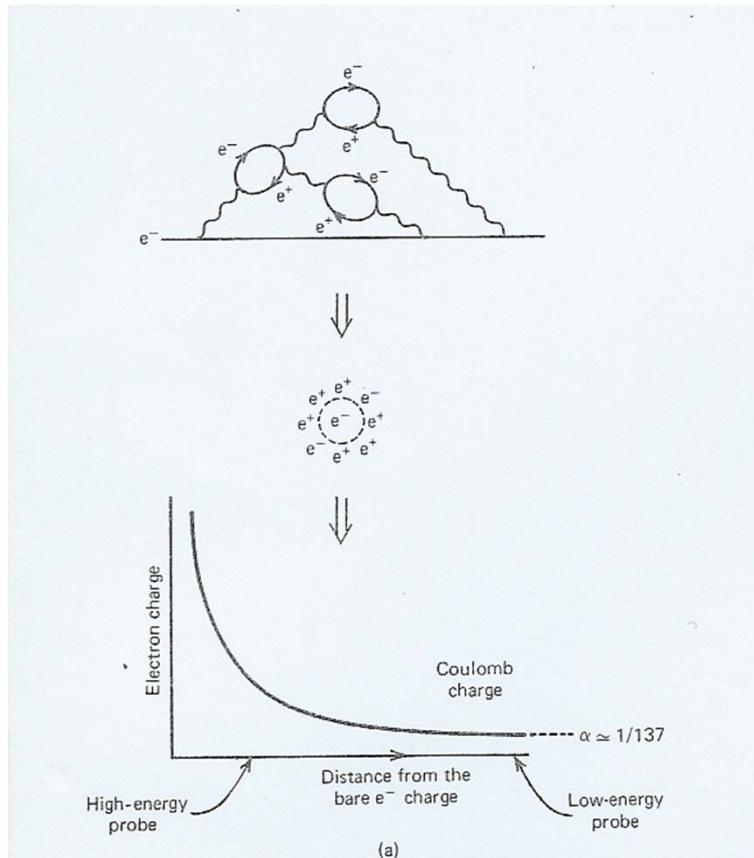
QCD Properties

- Poincaré, P, T and C invariant.
- Non abelian gauge theory $\Rightarrow$ physical spectrum consists of color singlet states only.
- The QCD effective coupling constant $\alpha_s(q)$ decreases as the momentum transfer scale increases (asymptotic freedom)
 $\Rightarrow$ perturbative calculations at high energies.
- Intrinsic scale at low energies Λ_{QCD} , main contribution to hadron masses. At $q \sim 1/\Lambda_{\text{QCD}}$, $\alpha_s(q) \sim 1$ and perturbation theory cannot be used.
- Flavor conservation.

Il fatto che i gluoni abbiano carica di colore implica l'esistenza di un accoppiamento diretto fra gluoni, per il quale non esiste l'analogo in QED.

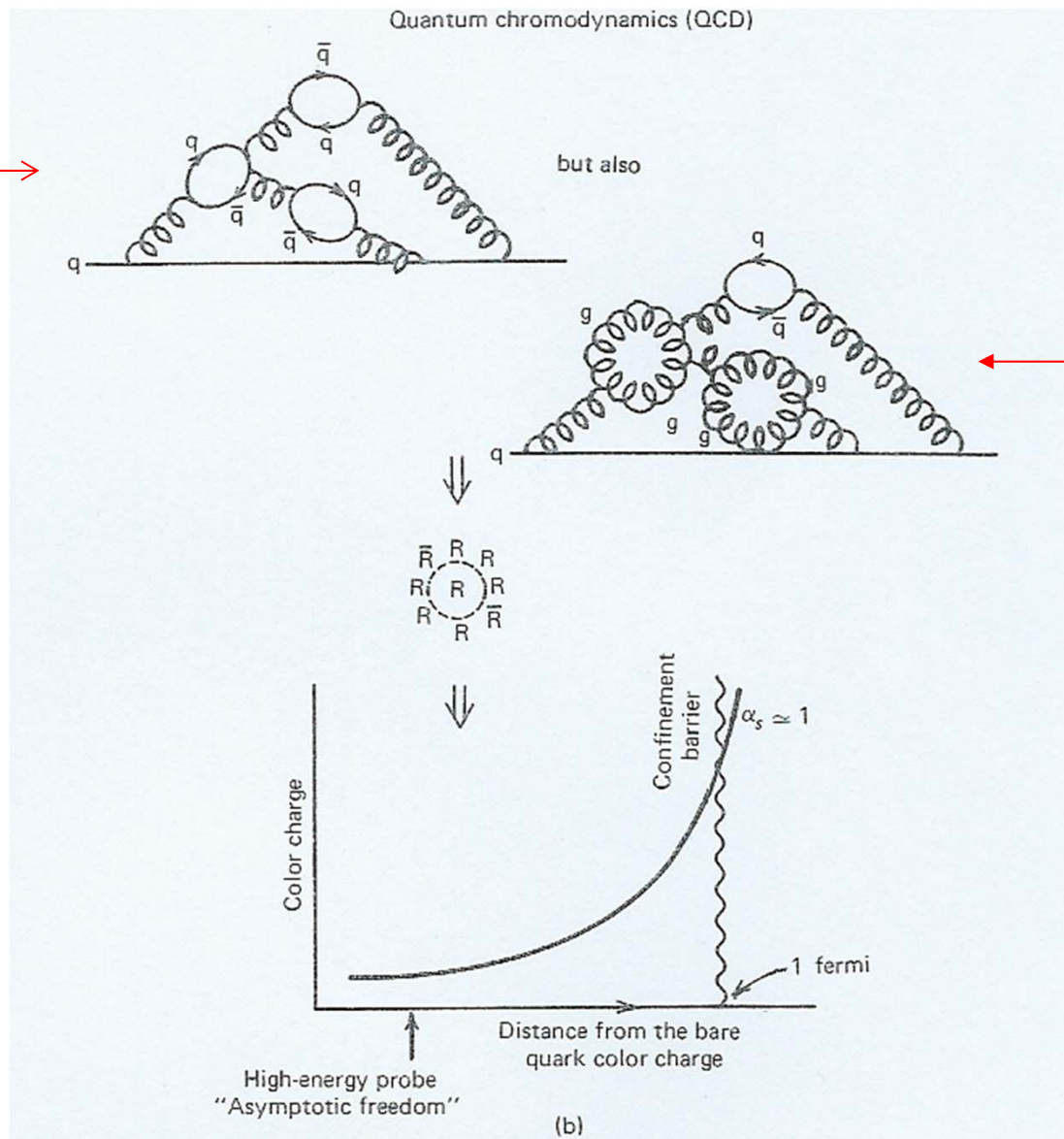


Questo fatto ha delle implicazioni importantissime sulla schermatura di carica in QED e QCD e sull'andamento asintotico delle due interazioni.



Schermatura di carica in QCD e andamento di α_s

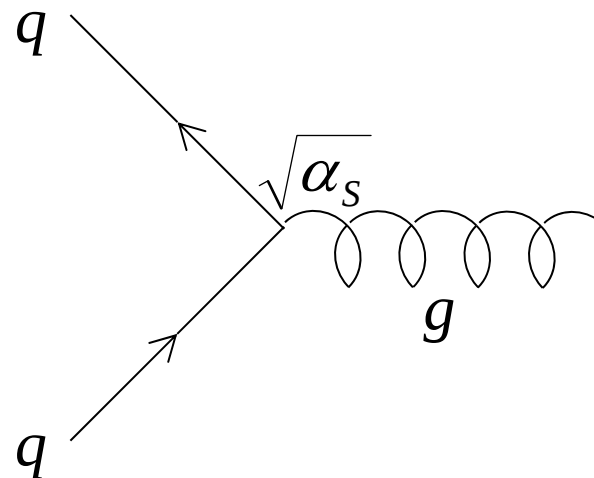
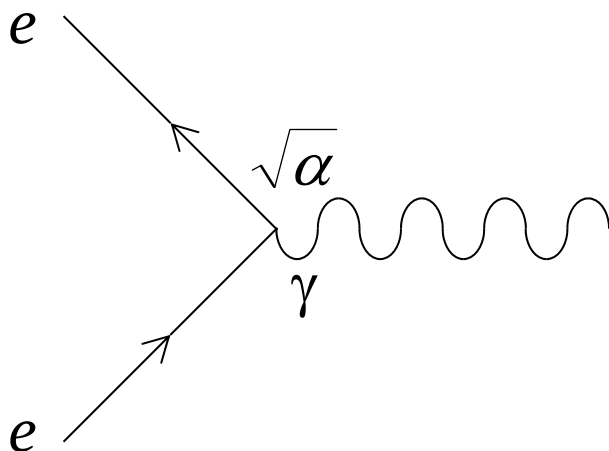
QED
analog



gluon
self coupling
in QCD

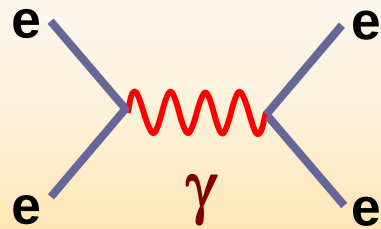
Le proprietà essenziali della QCD si possono riassumere nei seguenti punti:

- I quark hanno una carica di colore (oltre alla carica elettrica) che può assumere 6 valori: R, G, B, $\bar{R}$, $\bar{B}$, $\bar{G}$.
- Il colore viene scambiato da 8 gluoni “bi-colorati”.
- Le interazioni quark-quark si possono calcolare usando le regole di QED, con l'introduzione di un fattore di colore e la sostituzione $\sqrt{\alpha} \rightarrow \sqrt{\alpha_s}$ a ogni vertice.



- I gluoni possiedono carica di colore e possono interagire direttamente tra di loro.
- A piccole distanze α_s è sufficientemente piccola da rendere possibile il calcolo perturbativo (libertà asintotica).

QED vs QCD



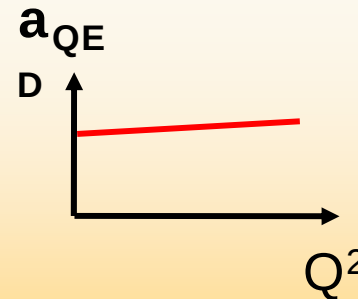
Leptons (e, μ , τ)
couple to
electric charge

Photon
carries
no charge

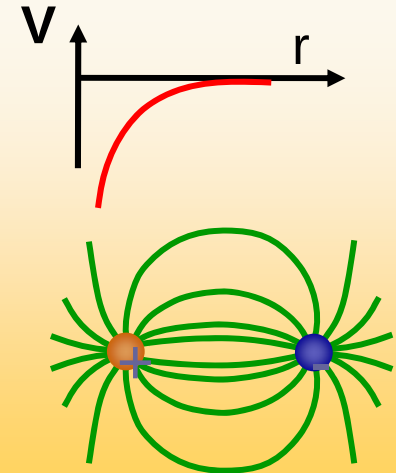
$$m_e = 0.5 \text{ MeV}$$

$$m_p = 938 \text{ MeV}$$

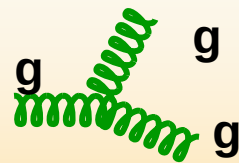
$$E_b = 13 \text{ eV}$$



$$\alpha_{QED}(Q^2 = 0) = \frac{1}{137}$$



Quarks
(u, d, s, c, b, t)
couple to
3 **Colourcharges**



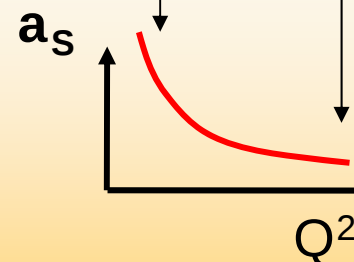
$$m_u \approx 3 \text{ MeV}$$

$$m_d \approx 6 \text{ MeV}$$

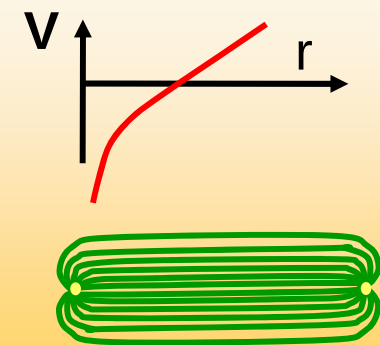
$$M_p = 938 \text{ MeV}$$

Confinement

Asymptotic
freedom



$$\alpha_S(Q^2 = M_Z^2) \approx 0.12$$



„String“

Física Adronica

Introduction

Hadron physics is the study of strong interacting hadronic matter in all its manifestations, and the understanding of its properties in terms of the underlying fundamental theory, **Quantum Chromodynamics or QCD**.

- QCD extremely successful at high energies.
- However it is the long-distance, low-energy regime which governs the bulk of strong interactions (e.g. it determines the properties of the light-hadron spectrum). It requires understanding of non-perturbative QCD.
- At low energies $SU(3)_F$ (flavor) symmetry reasonably successful.

Where is the missing link ?

Experimental exploration of the **full spectrum of states** composed of quarks, antiquarks and gluons is required to understand the structure and dynamics of hadrons.

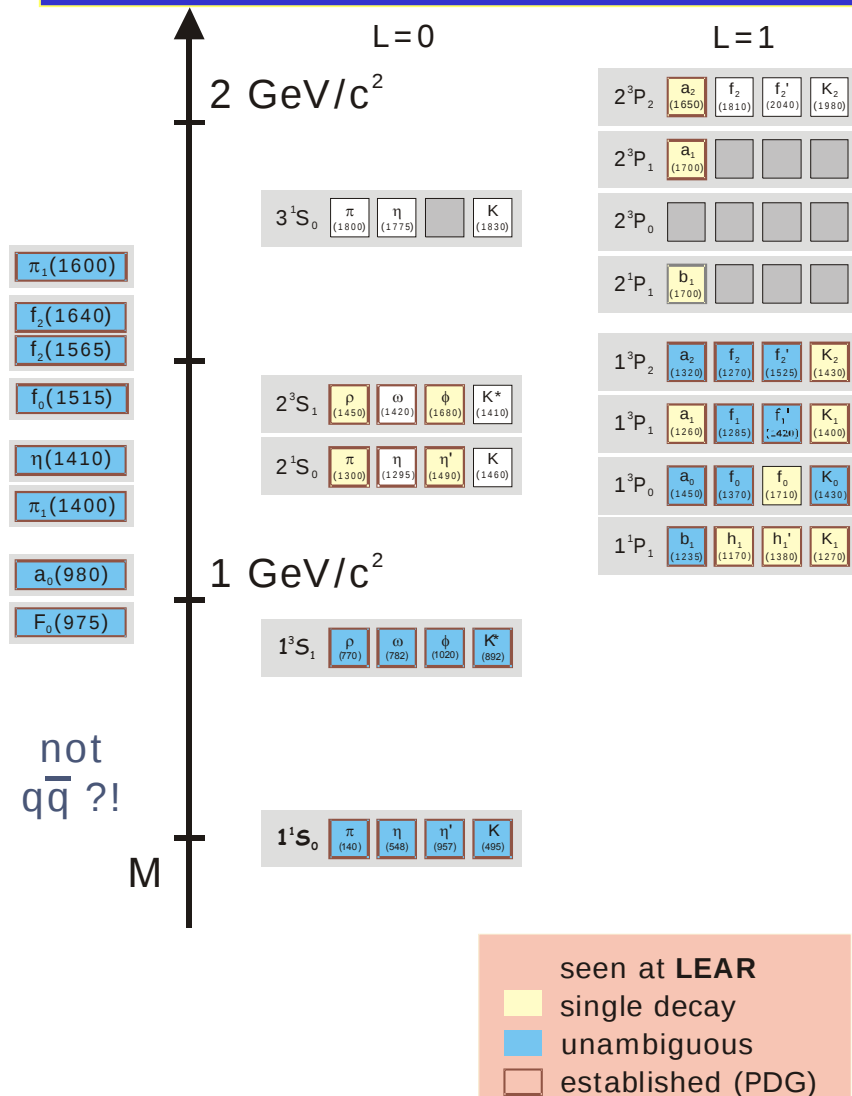
QCD is also an essential ingredient of the Standard Model and it is the incalculable strong matrix element which limit our reach for physics beyond the standard model.

- supersymmetric neutralino and dark matter puzzle.
- muon $g-2$.
- origin of CP violation.

Two main approaches for the study of hadronic matter:

- **Static**: mass, magnetic moments, spin, parity etc.
Spectroscopy and search for exotic states.
- **Dynamic**: study of the intrinsic properties of constituents inside hadrons (DIS, Transversity, GPD's etc.).

Meson Spectrum after LEAR



• The LEAR Era with the experiments

– @ CERN

- Asterix/Obelix
- Crystal Barrel
- Jetset/PS185
- WA102/Gams

– @ BNL

- E818/E852

– @ FNAL

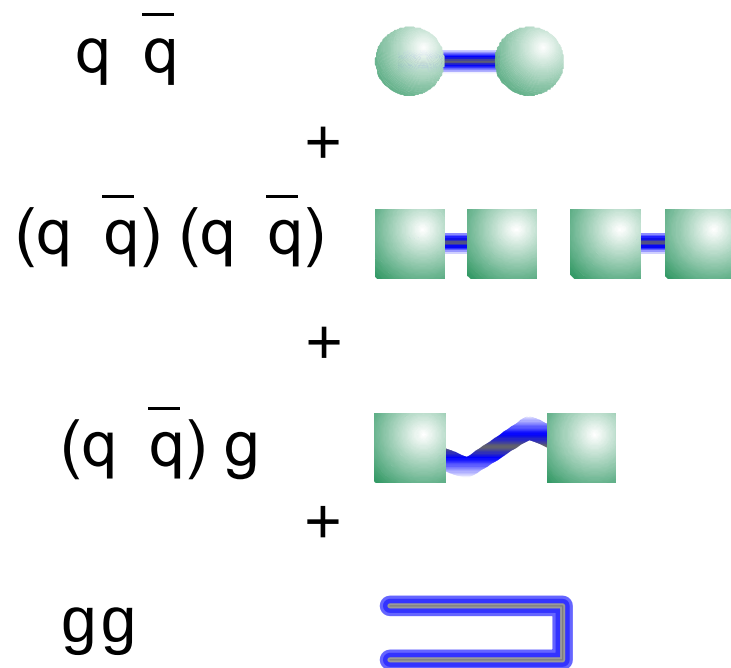
- E760/E835

– @ Serpukhov

- VES/Gams

produced **impressive results** with high statistics and high resolution

Hadrons are very complicated

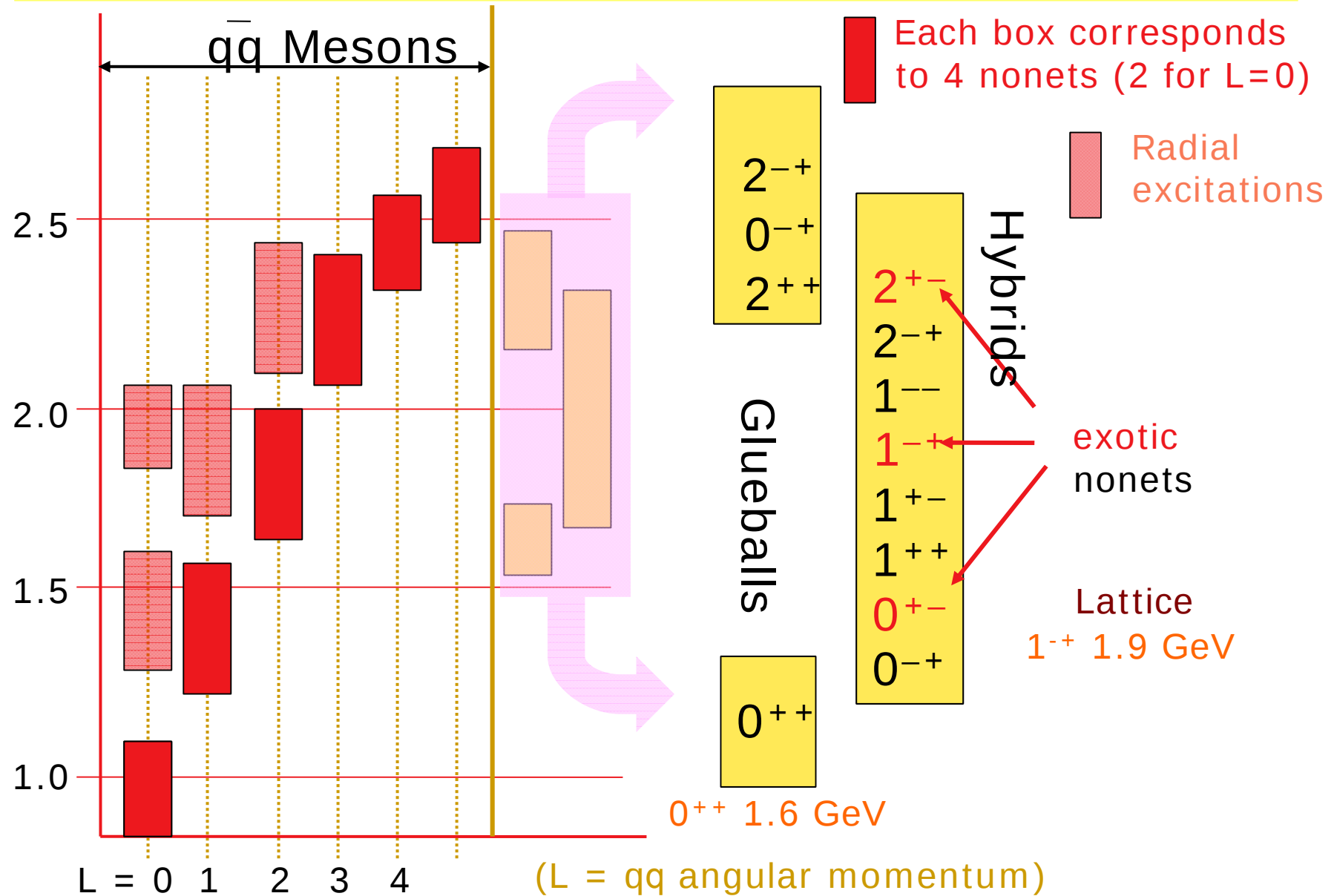


- Quark models usually account for $q \bar{q}$ states

- Other color neutral configurations with same quantum numbers can (and will mix)

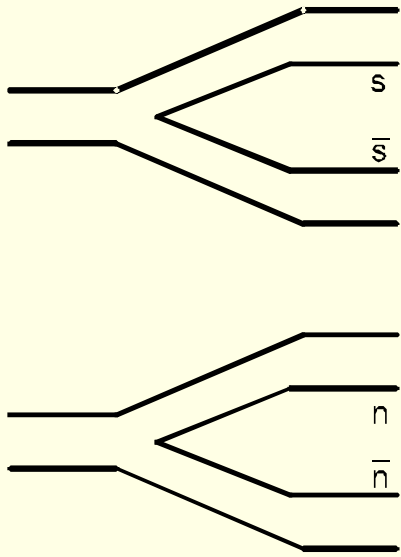
- Decoupling only possible for
 - narrow states
 - vanishing leading qq term

Light Meson Spectrum



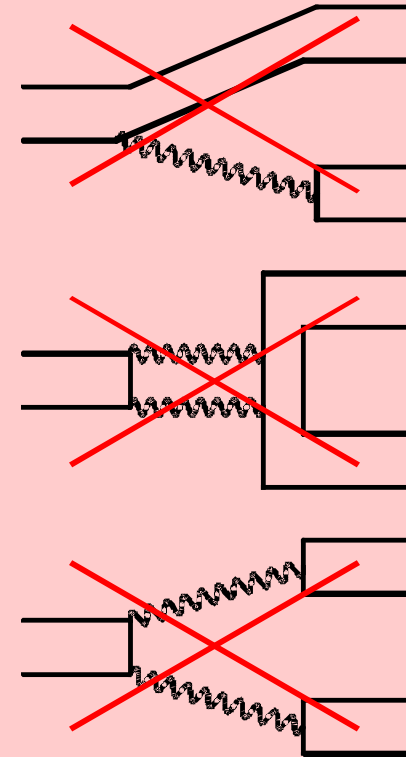
Meson Decay in the $SU(3)_F$ Picture

allowed

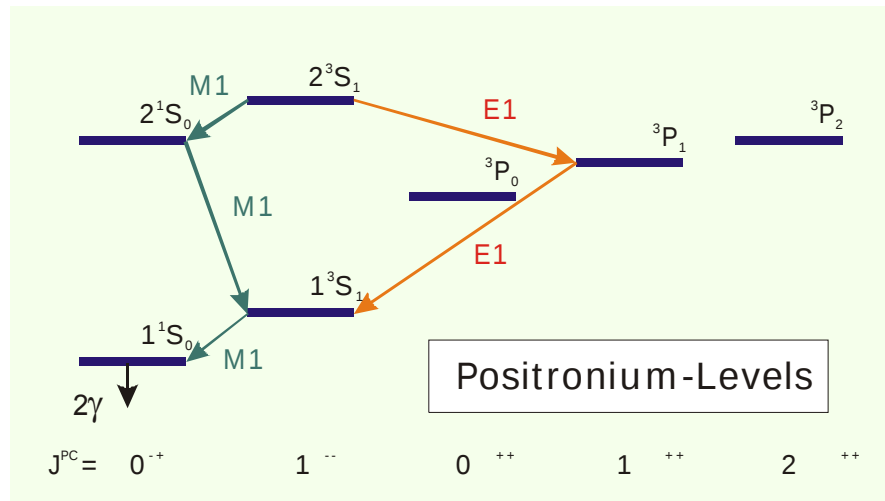


- Zweig-Rule
- Quark-antiquark-Production from the (3P_0 -)Vacuum
- But !
no hard gluons !

forbidden



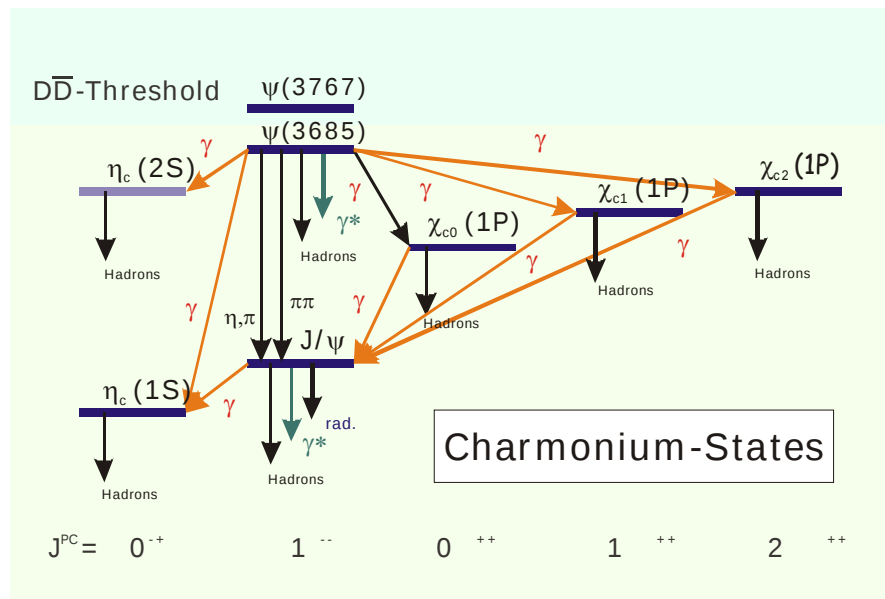
QED and QCD Bound States



Electrodynamic and Chromodynamic spectrum look alike (not to scale)

- for infinite quark masses

A Coulomb-like Potential seems to be a good approach



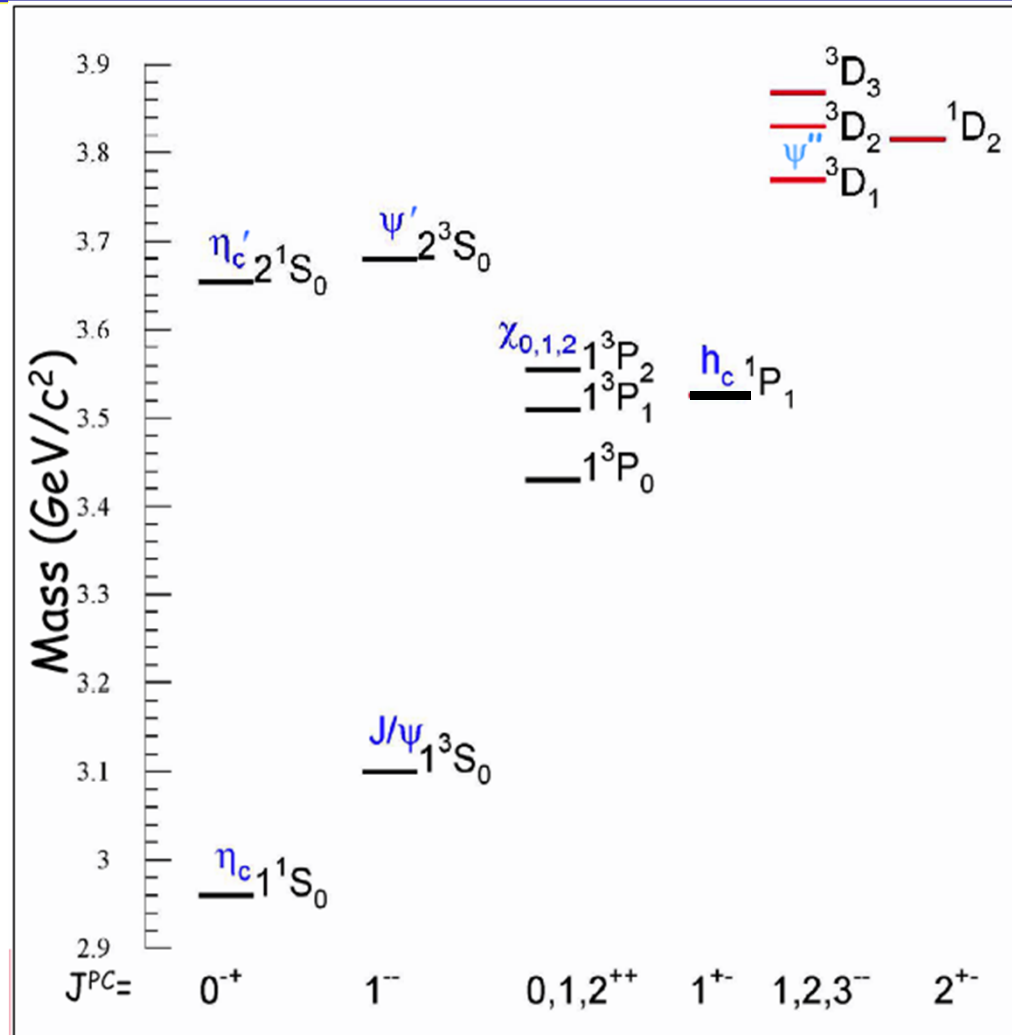
In addition one has to treat the confinement with a linearly rising potential

- confirmed by LQCD

Charmonium Physics

Open questions

- Precise measurement of mass and width for $\eta_c(2^1S_0)$ and $h_c(1^1P_1)$.
- States above threshold: D, 2P, ...
- Radiative decays
- Exclusive channels
 - helicity violation
 - 12 % rule
 - ...



Effective Field Theories (EFT)

A non-relativistic bound state is characterized by at least three scales:

- mass m (*hard*)
- momentum transfer mv (*soft*)
- kinetic energy of the $q \bar{q}$ pair in the CMS $E \sim p^2/m \sim mv^2$ (*ultrasoft*)

Hierarchy of scales $\Rightarrow$ substitute QCD with simpler, but equivalent, **Effective Field Theory (EFT)**, i.e. a quantum field theory with the following properties:

- It contains the **relevant degrees of freedom** to describe phenomena which occur in a certain **limited range of energies and momenta**.
- It contains an **intrinsic energy scale Λ** that sets the limit of applicability of the EFT.

Effective Field Theories (EFT)

- **Heavy Quark Effective Theory (HQET)** describes systems with one heavy quark ($q \bar{Q}, Q \bar{q}$), characterized by scales m and Λ_{QCD} . Integrate m out and build expansion in Λ_{QCD}/m .
- **Non Relativistic QCD (NRQCD)** describes bound states of two heavy quarks ($Q \bar{Q}$). Integrate out only m and leaves lower scales as dynamical degrees of freedom.

Lattice QCD (LQCD)

The interaction is discretized on a 3 (Space) + 1 (Time) dim. Lattice

e.g. $\partial_t \phi \rightarrow [\phi(t+a) - \phi(t-a)]/2a$.

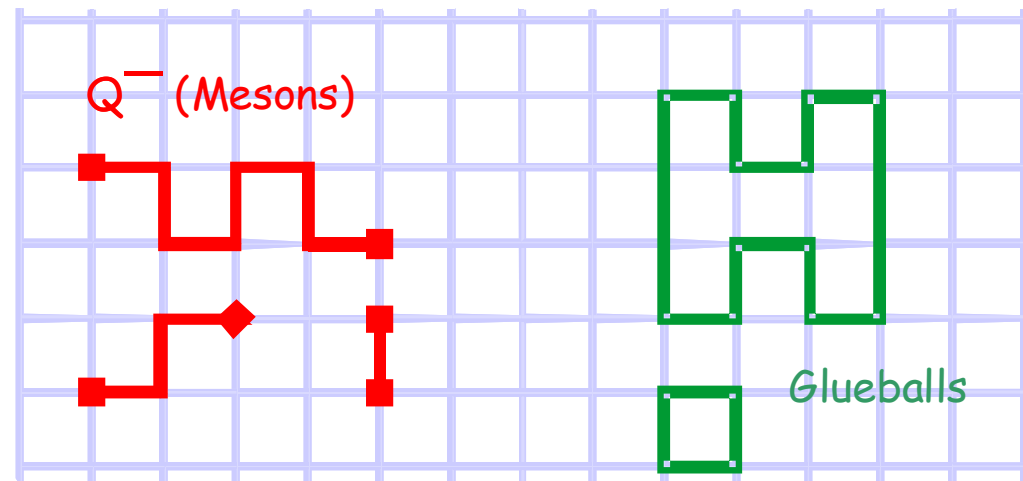
Continuum results obtained by $a \rightarrow 0$.

LQCD formulated in Euclidean space-time.

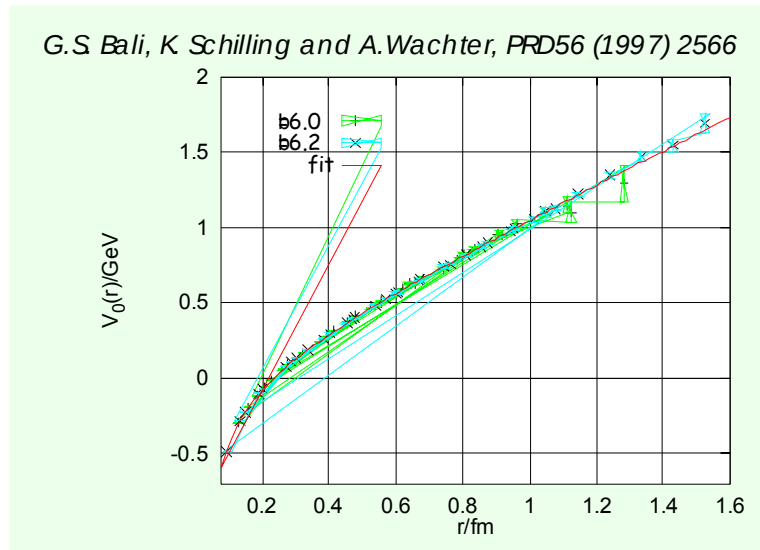
LQCD is a *first principles approach*: only parameters inherent to QCD, i.e.

α_s and the quark masses. These n_f+1 parameters are fixed by matching n_f+1 low-energy quantities to their experimental values.

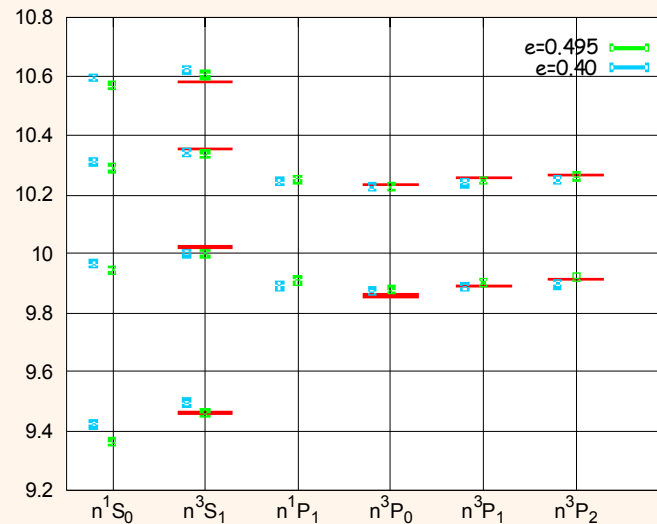
Observables are calculated taking their expectation values in the path integral approach $\Rightarrow$ take average of all possible “configurations” of gauge fields.



The $b \bar{b}$ Spectrum from LQCD



G.S. Bali, K. Schilling and A. Wachter, hep-ph/9611226

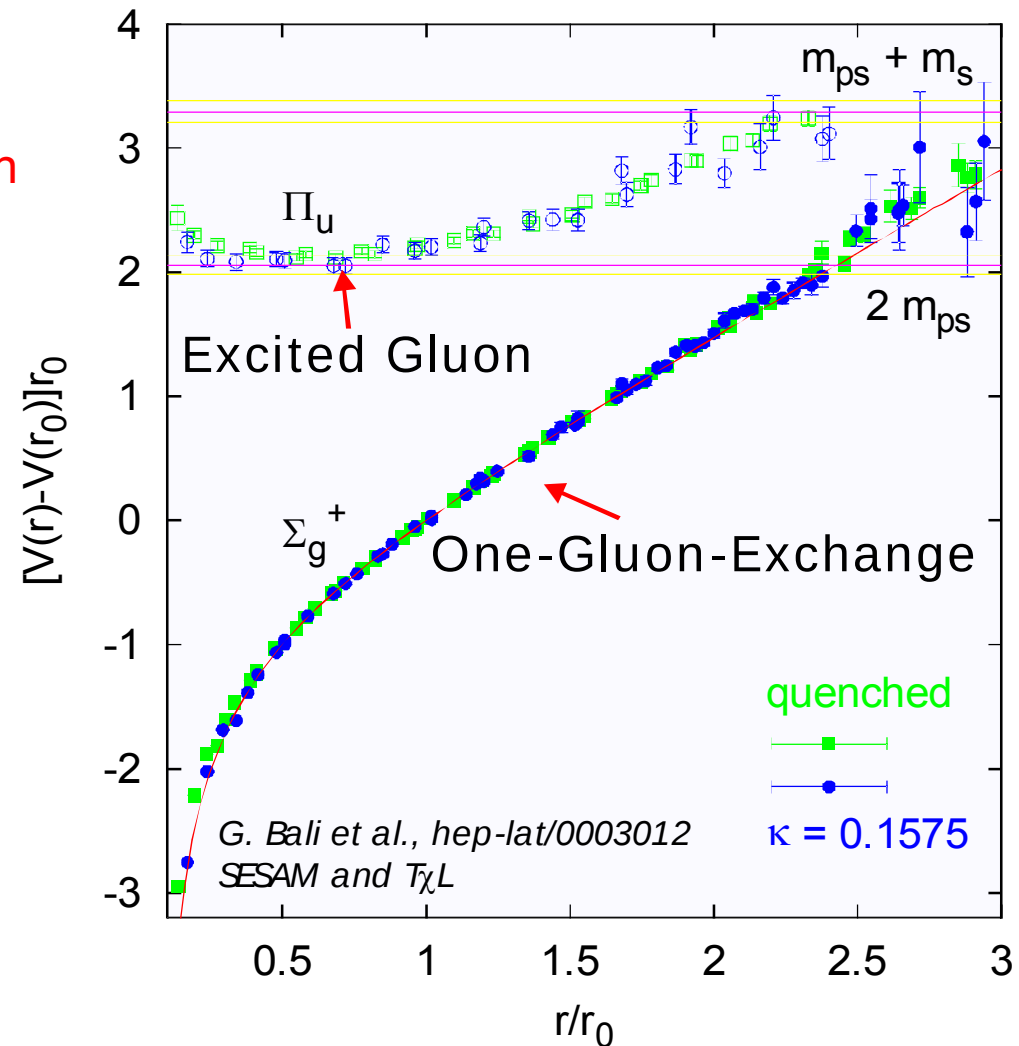


The static potential derived from LQCD confirms the
Coulomb + Confinement Ansatz

Quenched vs Unquenched LQCD

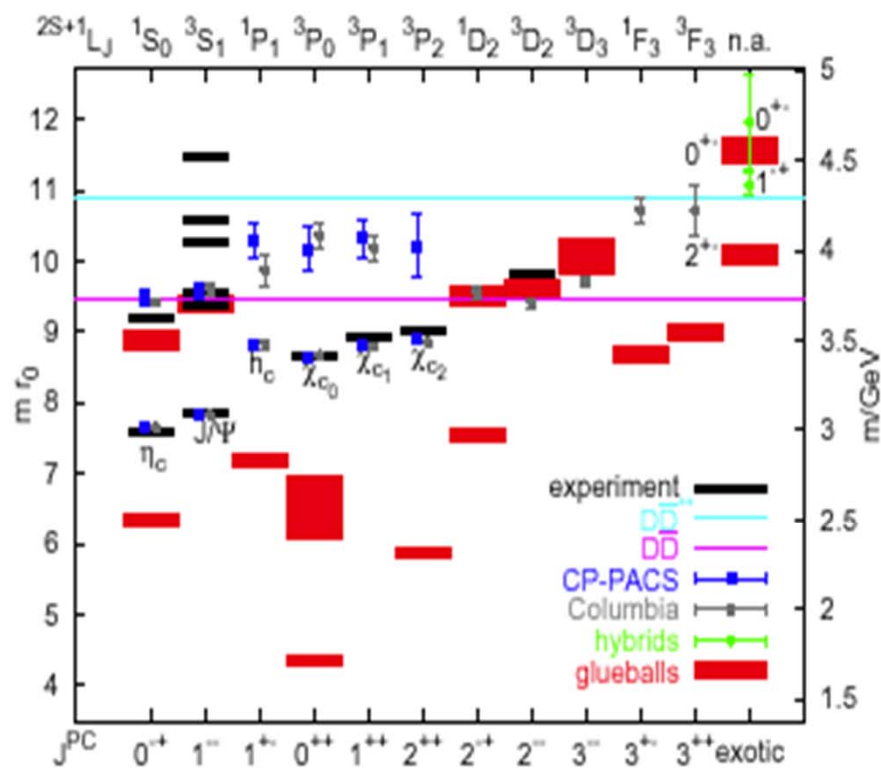
In the **quenched approximation** sea quarks are neglected.

$$V(r) = -\frac{4}{3} \frac{\alpha_s}{r} + \sigma r$$



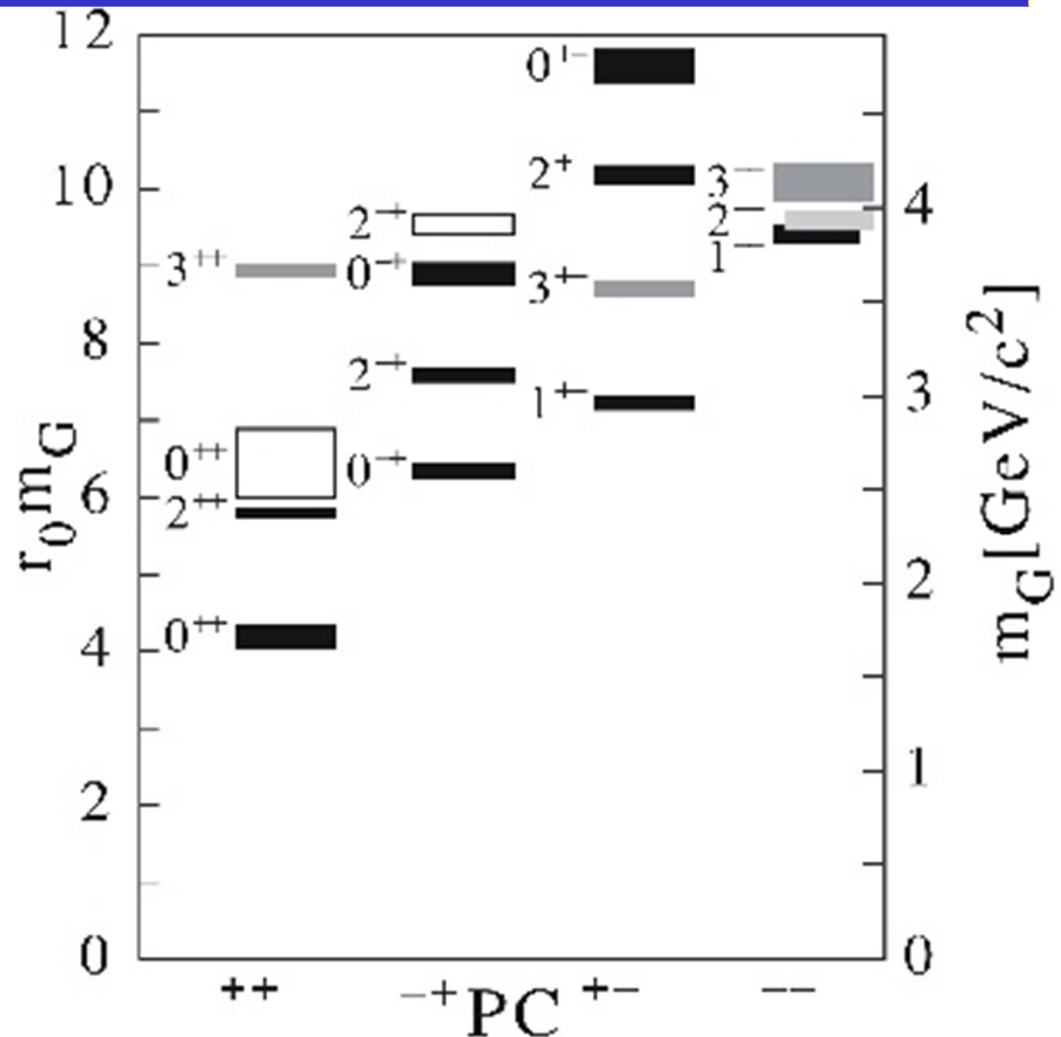
Quenched Charmonium Spectrum

J^{PC}	state	CP-PACS	Columbia	QCD-TARO	experiment	glueballs
0^{-+}	η_c	3013 (1)	3014 (4)	3010 (4)	2980(1)	2500(40)
	η_c'	3739(46)	3707(20)		3654(10)	3500(60)
1^{--}	J/ψ	3085 (1)	3084 (4)	3087 (4)	3097	
	$\psi(2S)$	3777(40)	3780(43)		3686	3700(50)
1^{+-}	h_c	3474(10)	3474(20)	3528(25)	$m[1^3P]=3525$	2830(30)
	h_c'	4053(95)	3886(92)		—	
0^{++}	χ_{c0}	3408	3413(10)	3474(15)	3415(1)	1720(30)
	χ_{c1}	4008(122)	4080(75)		—	2540(120)
1^{++}	χ_{c1}	3472 (9)	3462(15)	3524(16)	3511	
	χ_{c2}	4067(105)	4010(70)		—	
2^{++}	χ_{c2}	3503(24)	3488(11)		3556	2300(25)
	χ_{c3}	4030(180)			—	
2^{-+}	1^3D_2		3763(22)		—	2975(30)
					—	3740(40)
2^{--}	1^3D_2		3704(33)		$X(3872) ???$	3780(40)
3^{--}	1^3D_3		3822(25)		—	3960(90)
3^{+-}	1^3F_3		4224(74)		—	3410(40)
3^{++}	1^3F_3		4222(140)		—	3540(40)
0^{+-}	H_0		4714(260)		—	4560(70)
1^{-+}	H_1		4366(64)		—	
2^{+-}	H_2		4845(220)		—	3980(50)



Glueballs

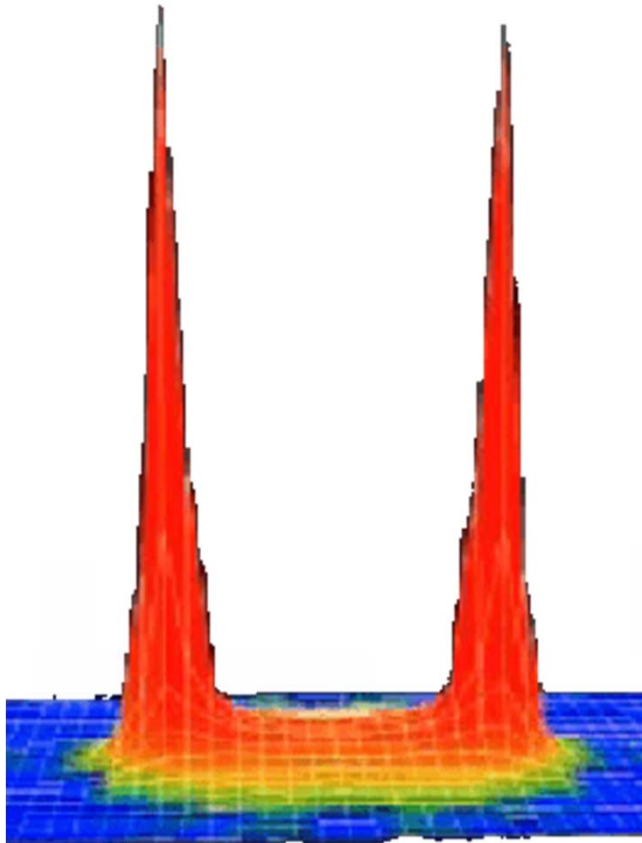
- Glueballs are the **excitation of the QCD vacuum**
 - Comparably easy to calculate
 - Lots of improvements in the last decade
 - Mainly due to
 - anisotropic lattices
 - improved actions



Morningstar und Peardon, PRD60 (1999) 034509
 Morningstar und Peardon, PRD56 (1997) 4043

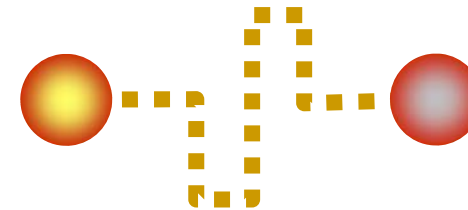
Fluxtube

The gluon field between the quark and the antiquark is like a flux of glue.
Actual states are discrete configurations.
Decays are due to flux breaking.



~ Simplified Lattice Approach

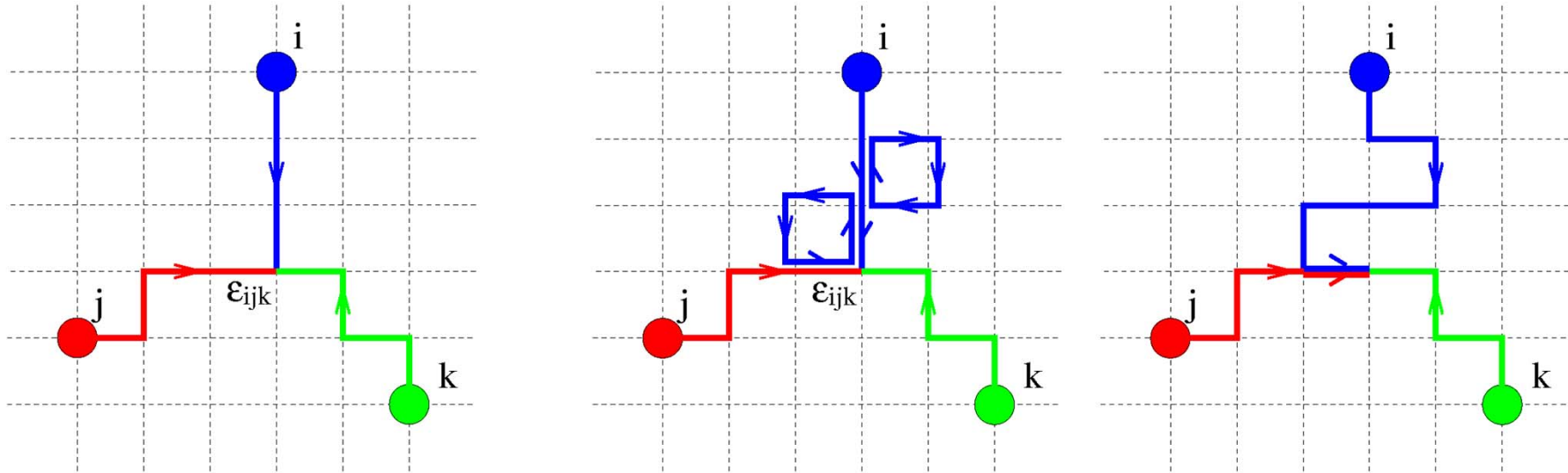
Meson



Hybrid

Flux (excited Gluon)
carries angular momentum

Example: Baryons in the Fluxtube Model



Basic idea is to reduce the amount of computing time by integrating over the whole color flux between source and drain

The excitation energy is then related to the averaged flux length for a sample of configurations

Definition of Hadron Configurations

$SU(3)_c$ symmetry tells us that

$$(3i+n)q \ (3j+n) \ \bar{q} \ (k)g$$

is colour neutral

$$i=1, j=n=k=0$$

baryon

$$i=j=k=0, n=1$$

meson

$$i=j=n=0, k>1$$

glueball

$$i=j=0, n=1, k>1$$

meson hybrid

$$i=1, j=n=0, k>1$$

baryon hybrid

$$i=n=1, j=k=0$$

pentaquark

$$i=j=k=0, n=2$$

four-quark

$$i=j=k=0, n=3 \text{ or } i=j=1, n=k=0$$

baryonium

Classification (Close and Lipkin)

Exotics of the first kind

External quantum numbers unambiguously incompatible with assignment to baryons or mesons

B=1 - baryonlike

- $Q > 2, Q < -1, S < -3, S > 0, I > 3/2, \dots$

B=0 - mesonlike

- $|Q| > 1, I > 1, |S| > 2, |C| > 2, |S-C| > 1, \dots$

Classification (Close and Lipkin)

Exotics of the **second kind**

Combination of quantum numbers not allowed for leading Fock-term

Only possible for $B=0$

- $J^{PC} = 0^{--}, 0^{+-}, 1^{-+}, 2^{+-}, \dots$
- cannot be formed by any unexcited qq-System

Classification (Close and Lipkin)

Exotics of the **third kind** – **Crypto-Exotics**

Internal exotic structure

- like gluonic excitations
- like N-quarks

but no model free signature

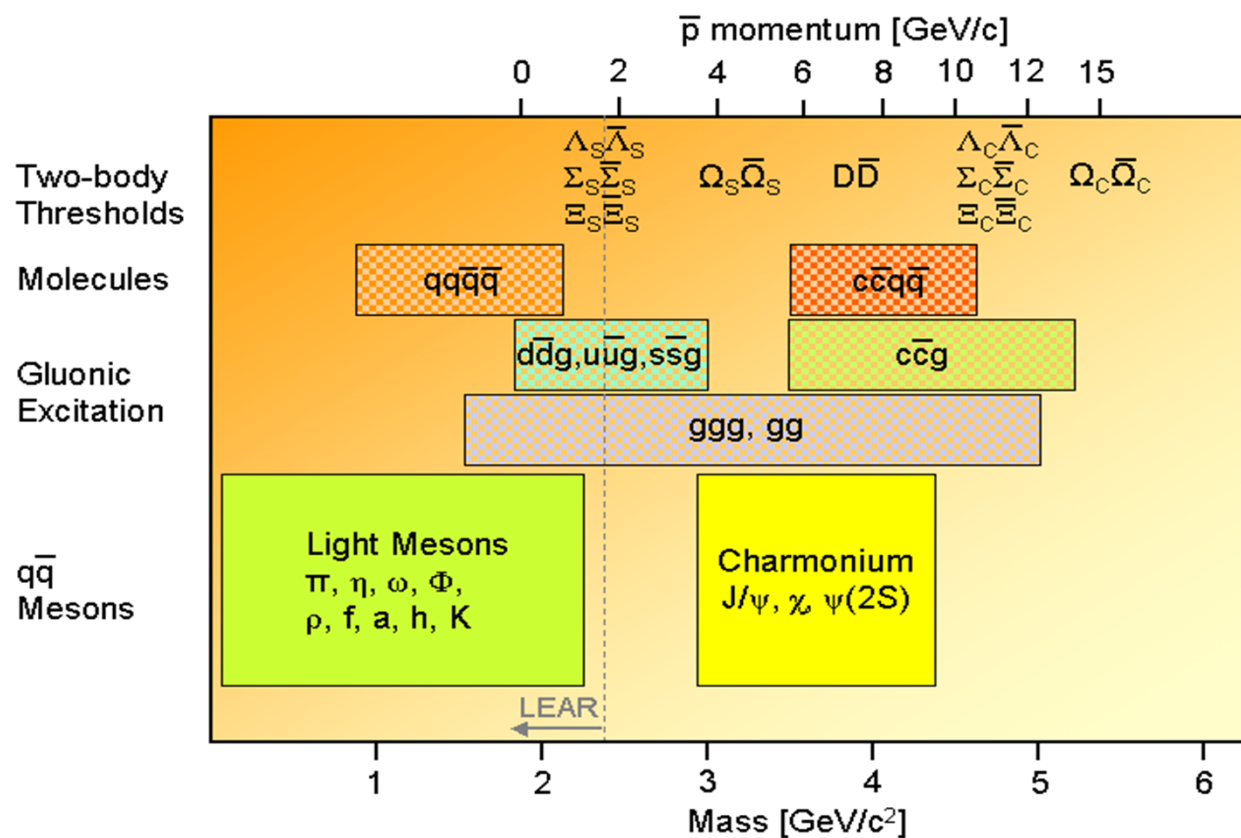
approach:

- overpopulation of hadron multiplets
- unexpected masses and decay properties
- a well understood conventional meson picture is mandatory

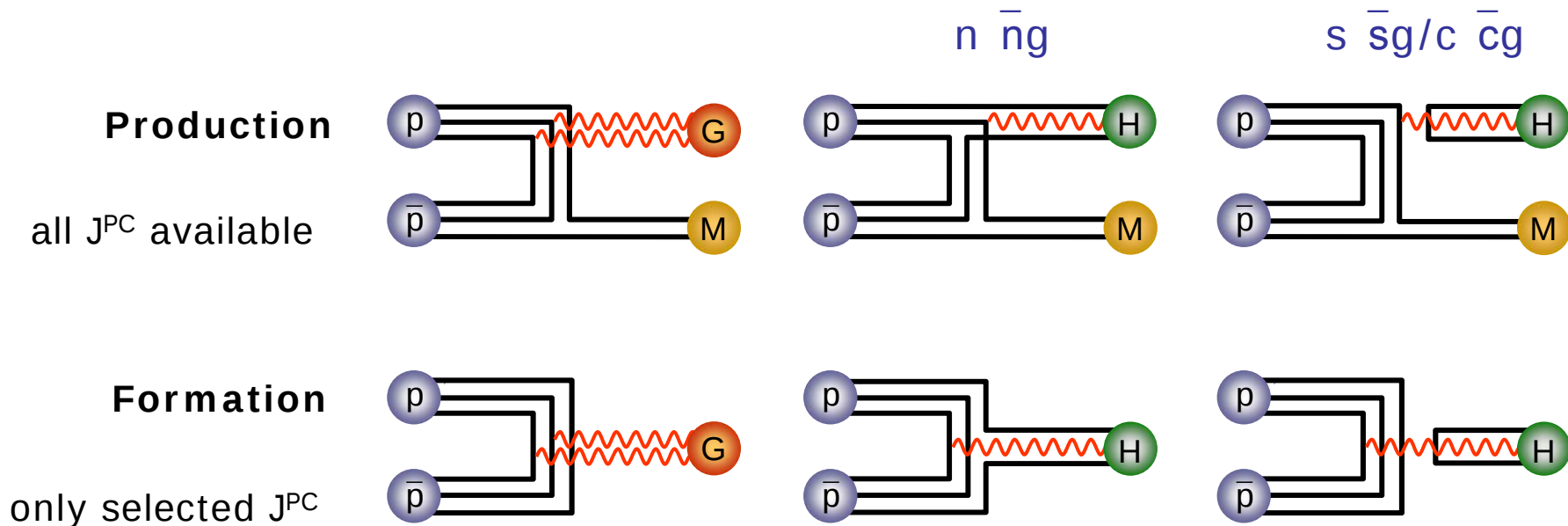
Antiproton-Proton Annihilation in Flight

- Annihilation in flight
 - scattering process: no well defined initial state
 - maximum angular momentum rises with energy
- Advantages
 - larger phase space
 - formation experiments
- Disadvantages
 - many waves due to large phase space
 - many waves interfere with each other

Hadronic Systems



Exotic Production/Formation in $\bar{p}p$ Annihilation



Gluon rich process creates gluonic excitation in a direct way

- $c \bar{c}$ requires the quarks to annihilate (no rearrangement)
- yield comparable to charmonium production
- even at low momenta large exotic content has been proven
- Exotic quantum numbers can only be achieved in production mode

$D_{(s)}$ systems

Charm (c) + Light Quark (u,d,s)

H-Atom of QCD

Annihilation of the charm quantum number

D-Mesons have no strong decay

only (electro-)weak decays possible

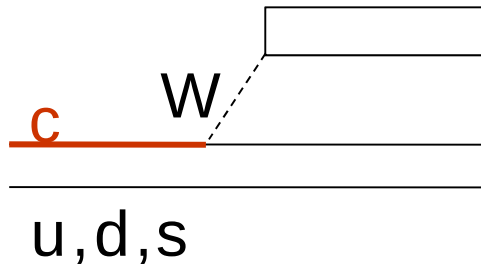
Long lifetime $c\tau \sim 100\text{-}300\mu\text{m}$

Many decays to light mesons

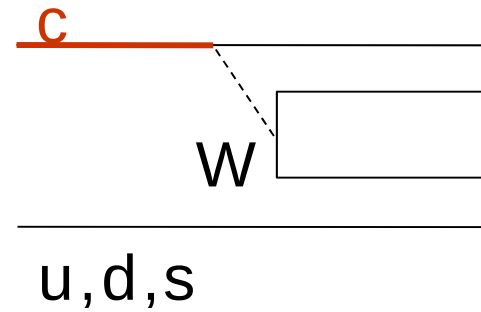
clean Spin-Parity $J^{PC}=0^{-+}$ for spectroscopy

$D_{(s)}$ Decays

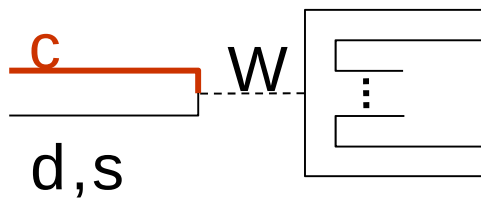
W-Emission (external)



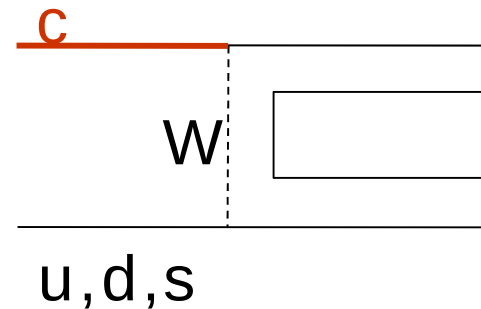
W-Emission (internal)



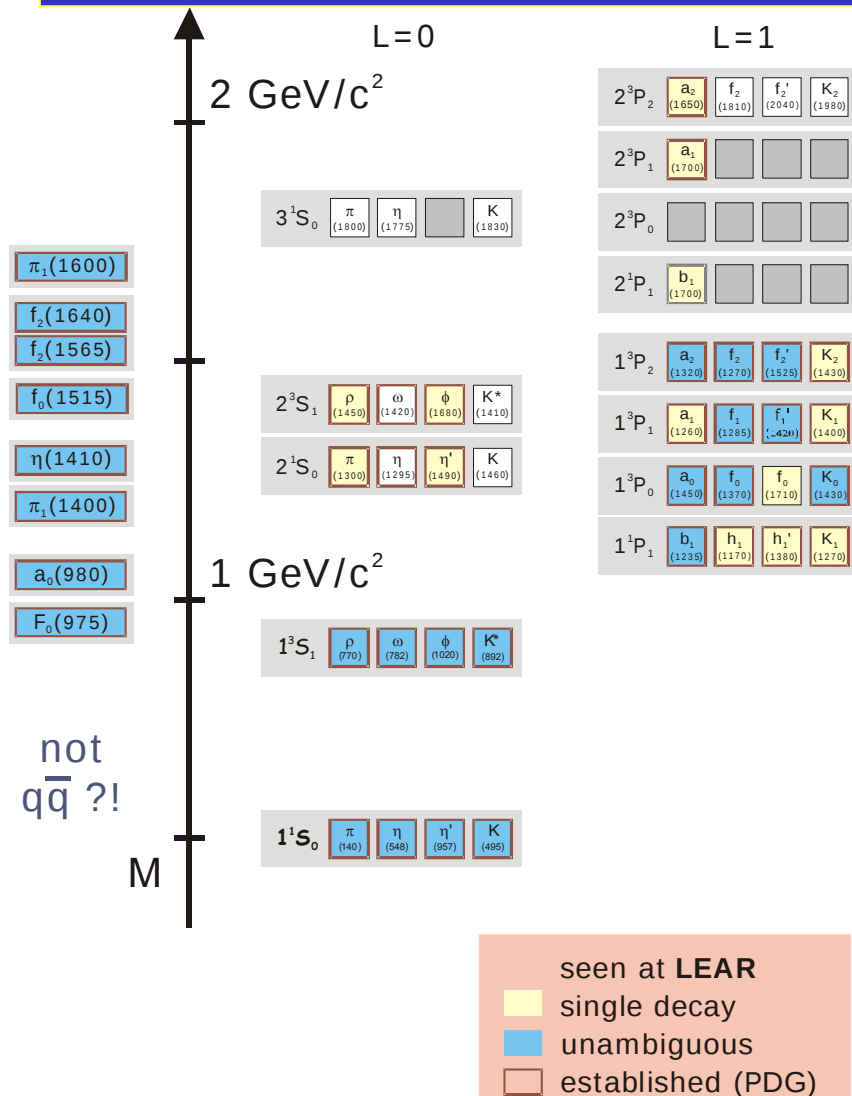
W-Annihilation



W-Exchange



Meson Spectrum after LEAR



• The LEAR Era with the experiments

– @ CERN

- Asterix/Obelix
- Crystal Barrel
- Jetset/PS185
- WA102/Gams

– @ BNL

- E818/E852

– @ FNAL

- E760/E835

– @ Serpukhov

- VES/Gams

produced **impressive results** with high statistics and high resolution

Hybrids

- Light hybrids
 - Predictions
 - Candidates
- Charmonium hybrids
 - Predictions

Simplest Hybrids

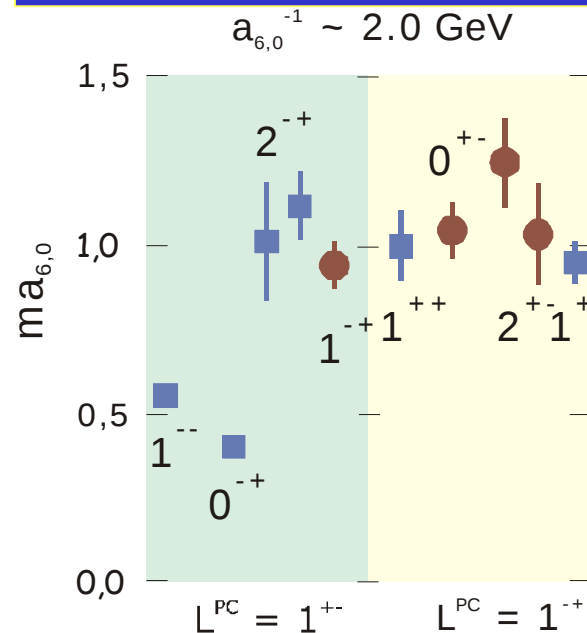
S-Wave+Gluon $(qq)_8g$ with $()_8$ =coloured

1S_0 $\uparrow\downarrow$ 3S_1 $\uparrow\uparrow$

combined with a 1^+ or 1^- gluon

Gluon	1^- (TM)	1^+ (TE)
$^1S_0, 0^{-+}$	1^{++}	1^{--}
$^3S_1, 1^{--}$	0^{+-} 1^{+-} 2^{+-}	0^{-+} 1^{-+} 2^{-+}

Light Hybrid LQCD Predictions



UKQCD '96/'97, quenched QCD

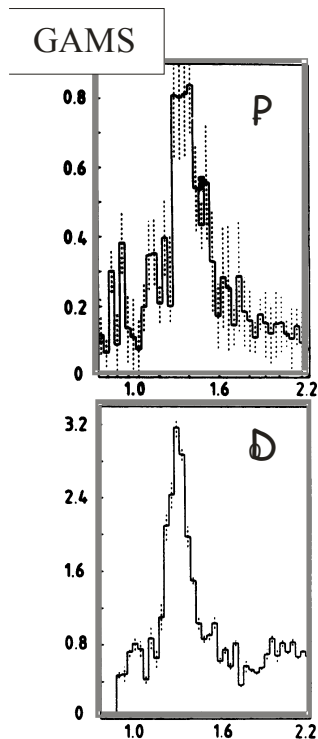
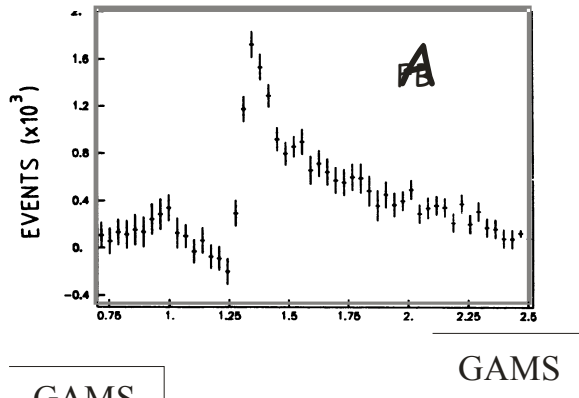
masses $\sim 2 \text{ GeV}/c^2$ comparable to masses from the fluxtube-model but:
LQCD predicts

a light vector ($\sim 1,2 \text{ GeV}/c^2$)

and a pseudoscalar ($< 1 \text{ GeV}/c^2$)

Group	$m(1^{+-})$	Ref
UKQCD ,97	1.87	Lacock et al, PLB401,308
MILC ,97	1.97	Bernard et al, PRD56 7039
MILC 99	2.11	Bernard et al, NPB 73,264
Lacock & Schilling	1,9	NPB73,261

$\pi_1(1400)$ - History



1988 GAMS published strong FB-asymmetry in the reaction

□ $\rightarrow \pi^- p \rightarrow \pi^0 \eta n$

verifies Apel et al. and called **M(1405)**

1991 GAMS: PWA ambiguous,

□ $\rightarrow$ 8 solutions

□ $\rightarrow$ not all support $\pi\eta$ P-wave

1992 KEK-E179:

□ $\rightarrow$ all solutions need an exotic wave
but acceptance unclear

1994 CB: PS-197

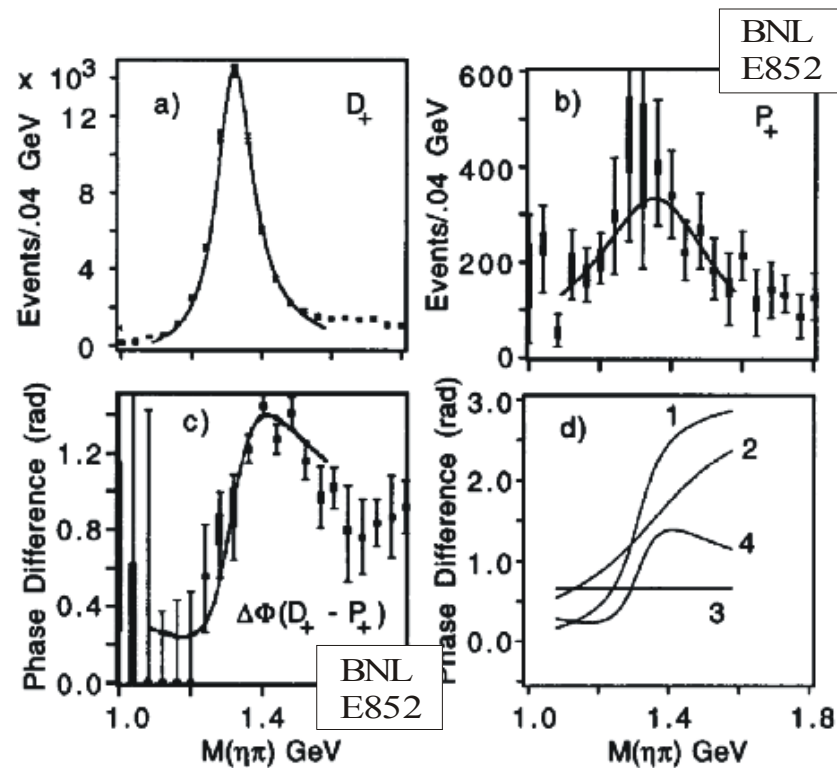
□ $\rightarrow \pi\eta$ -P-Wave in $\pi\pi\eta$

□ $\rightarrow$ large Width

□ $\rightarrow$ Resonance? questionable

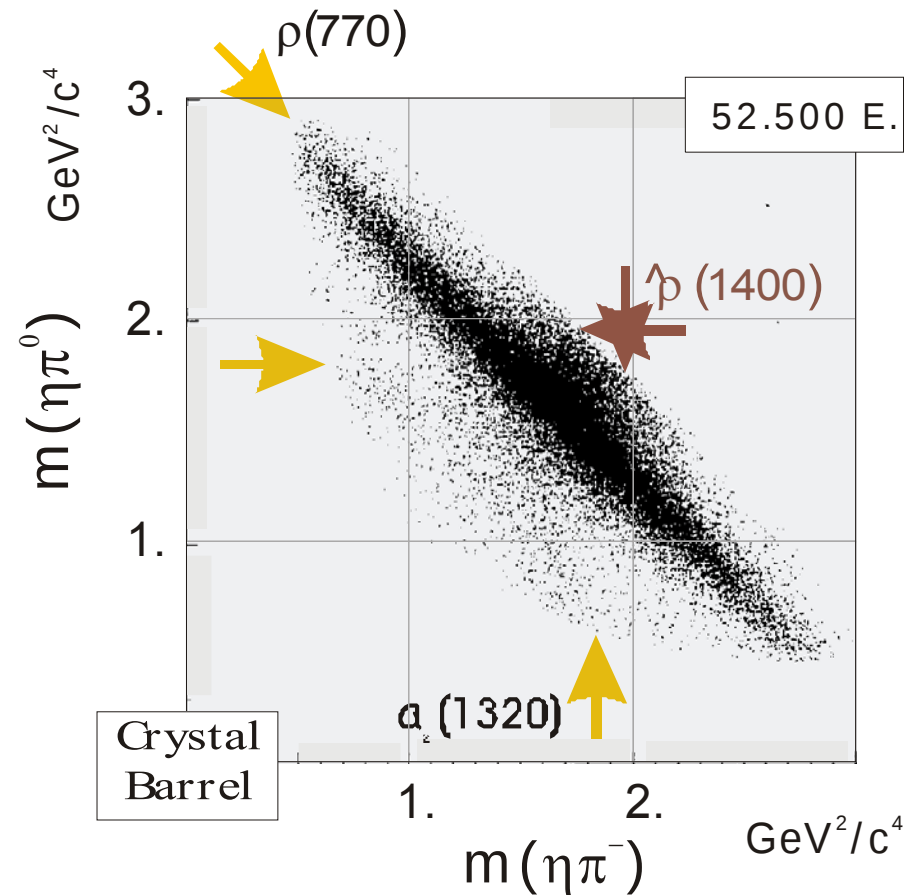
$\pi_1(1400)$ – E852 and Crystal Barrel

$\pi^- p \rightarrow \pi^- \eta p$ (and $\rightarrow \pi^0 \eta n$)



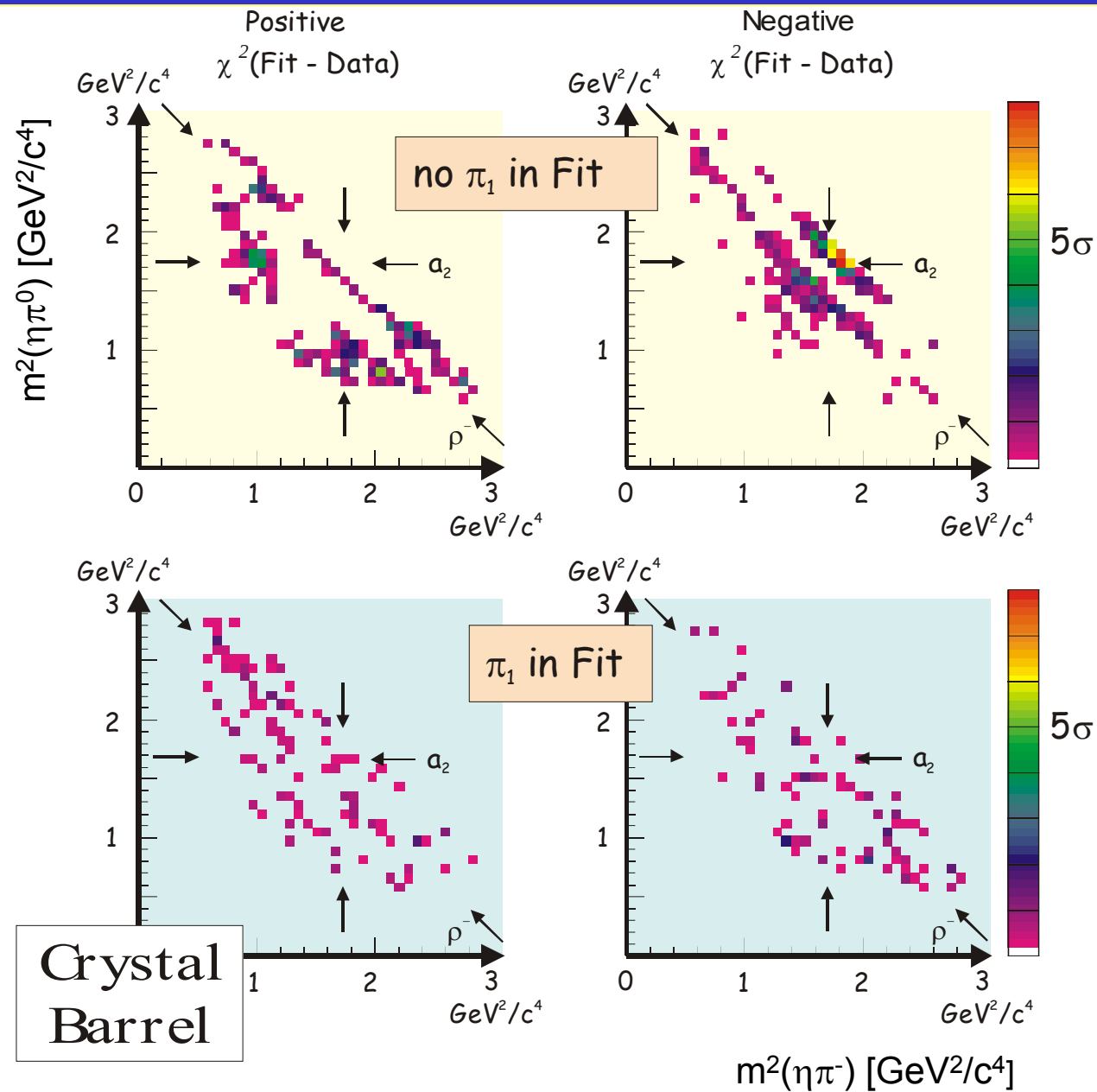
$\pi\eta$ peak @ $1.4 \text{ GeV}/c^2$
 phasemotion at a_2 tail visible

$\bar{p}d \rightarrow \pi^- \pi^0 \eta p$ @ Rest in liq.D2



Advantage: $I=1$
 and no Scalars

$\pi_1(1400)$ – Proof of Exotic Wave (CB)

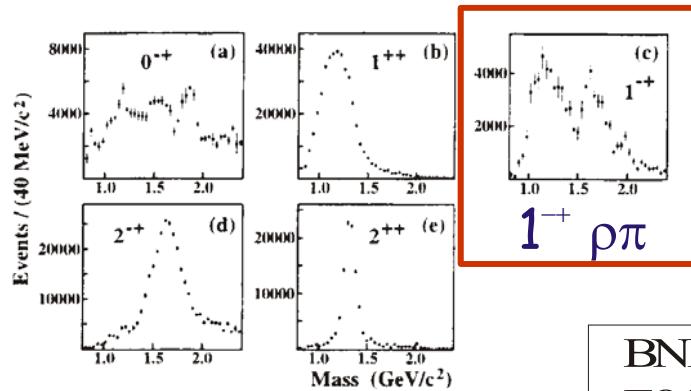


$\pi_1(1400)$ Summary

Exp	Year	Mass	Width	Channel
GAMS	1988	1406 ± 20	189 ± 20	$\pi^0 \eta$
E179	1993	1323 ± 5	143 ± 13	$\pi^- \eta$
VES	1993	~ 1300	~ 300	$\pi^- \eta$
	1997	~ 1300	> 500	$\pi^- \eta$
CB	1994	$1200-1600$	$400-1000$	$\pi^0 \eta$
	1998	1360 ± 25	220 ± 90	$\pi^0 \eta$
E852	1997	$1370 \pm 16^{+50}_{-30}$	$385 \pm 40^{+65}_{-105}$	$\pi^- \eta$
CB	1998	$1400 \pm 20 \pm 20$	$310 \pm 50^{+50}_{-30}$	$\pi^0 \eta \quad \pi^- \eta$

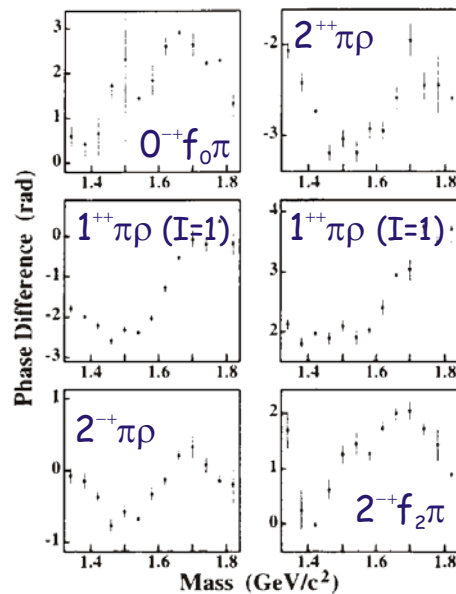
Exotic wave is evident

$\pi_1(1600)$



BNL
E852

$\phi(X-1^+)$



$\pi^- p \rightarrow \pi^- \rho^0 p \rightarrow \pi^- \pi^- \pi^+ p$ (E852)
shows a clear resonance in the 1^-
wave around $1600 \text{ MeV}/c^2$

Also observed by the VES
collaboration in the $\rho\pi$, $\eta'\pi$ and
 $b_1(1235)\pi$ channels.

$b_1(1235)\pi$ channel confirmed by CB
in $\bar{p}p \rightarrow \omega \pi^+ \pi^- \pi^0$.

Heavy-quark hybrid mesons

- more amenable to theoretical treatment than light-quark hybrids

- early work:

- Hasenfratz, Horgan, Kuti, Richards (1983)

- Perantonis, Michael (1990)

- possible treatment like diatomic molecule

- (Born-Oppenheimer)

- slow heavy quarks $\leftrightarrow$ nuclei

- fast gluon field (and light quarks) $\leftrightarrow$ electrons

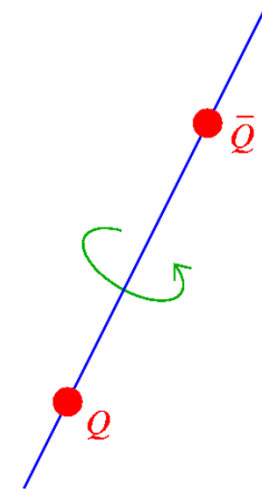
- gluons provide adiabatic potentials $V_{qq}(r)$

- gluons fully relativistic, interacting

- potentials computed in lattice simulations

- nonrelativistic quark motion described in *leading order* by solving Schrödinger equation

- conventional mesons from Σ_g^+ hybrids from Π_u, Σ_u^-



LQCD ccg 1^+ vs. cc 1^- (J/ψ)

1^+	$m(c \bar{c}g)$	Model	Group	Reference
$4390 \pm 80 \quad \pm 200$		isotropic	MILC97	PRD56(1997)7039
4317 ± 150		isotropic	MILC99	NPB93Supp(1999)264
4287		isotropic	JKM99	PRL82(1999)4400
$4369 \pm 37 \quad \pm 99$		anisotropic	ZSU02	hep-lat 0206012
$\Delta(1^+, 1^-)$	$m(c \bar{c}g) - m(c \bar{c})$			
$1340 \pm 80 \quad \pm 200$		isotropic	MILC97	PRD56(1997)7039
1220 ± 150		isotropic	MILC99	NPB93Supp(1999)264
1323 ± 130		anisotropic	CP-PACS99	PRL82(1999)4396
1190		isotropic	JKM99	PRL82(1999)4400
$1302 \pm 37 \quad \pm 99$		anisotropic	ZSU02	hep-lat 0206012

Charmed Hybrids

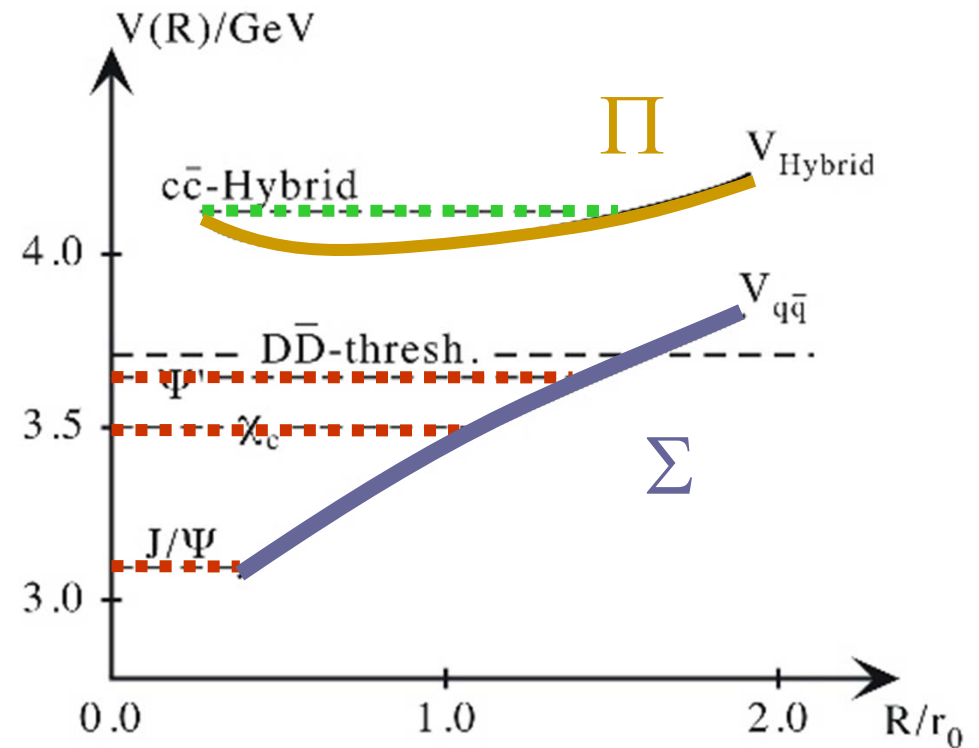
Gluonic excitations of the quark-antiquark-potential may lead to bound states

LQCD:

□ Π potential

– $m_H \sim 4.2\text{-}4.5$ GeV

Light charmed hybrids could be as narrow as $\rightarrow O(5\text{-}50$ MeV)



important $\langle r^2 \rangle$ and r_{Breakup}

Charmed Hybrid Level Scheme

$$1^{--} (0,1,2)^{-+} < 1^{++} (0,1,2)^{+-}$$

- JKM00, NPB83Suppl83(2000)304 and Manke, PRD57(1998)3829

L-Splitting

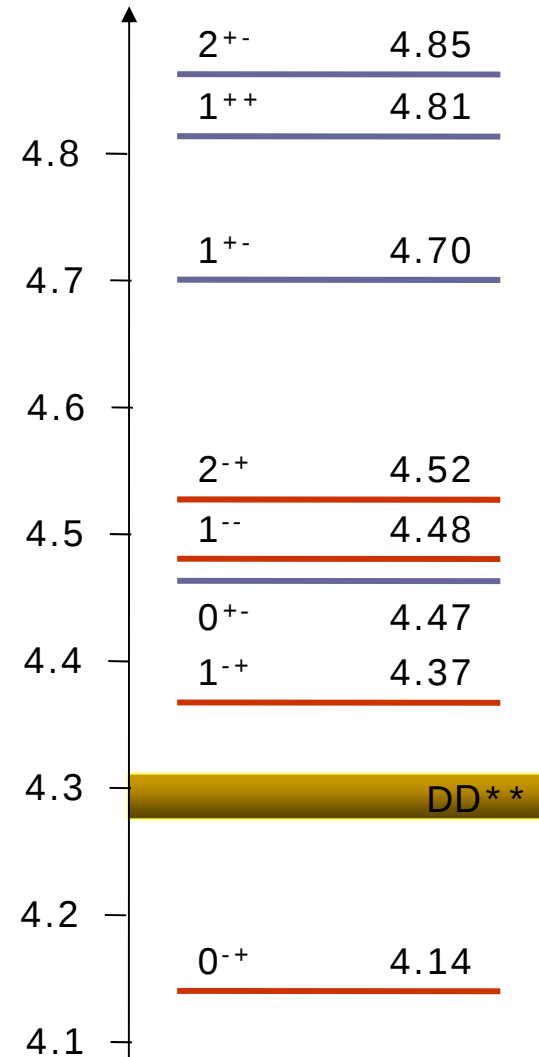
$$\square \Delta m \sim 100\text{-}250 \text{ MeV}/c^2 \text{ for } 1^{-+} \text{ to } 0^{+-}$$

S-Splittings

- Page thesis, 1995 and PRD35(1987)1668
- 4.14 (0^{-+}) to 4.52 GeV/c^2 (2^{-+})

consistent w/LQCD

- JKM, NPB86suppl(2000)397, PLB478(2000) 151



Charmed Hybrids – Decays

Fluxtube-Model predicts $DD^{**}(\text{+c.c.})$ decays

- if $m_H < 4290 \text{ MeV}/c^2$ below $DD_0(\text{+c.c.})$
- $\rightarrow \Gamma_H < 50 \text{ MeV}$

Some exotics can decay neither to DD nor to $DD^{*}(\text{+c.c.})$

- e.g.: $J^{PC}(H)=0^{+-}$
 - fluxtube forbidden: $J/\psi f_2, J/\psi(\pi\pi)_S, \eta_c h_1$
 - fluxtube allowed: $\chi_{c0}\omega, \chi_{c0}\phi, \chi_{c2}\omega, \chi_{c2}\phi, h_{1c}\eta$
- Small number of final states with small phase space
 - favours a narrow resonance
- if $DD^{*}(\text{+c.c.})$ possible $\rightarrow$ still very small phase space

But! be prepared for surprises

measure DD nor to $DD^{*}(\text{+c.c.})$ waves as well

Scalars and Glueballs

Predictions

Production Modes

Scalar States

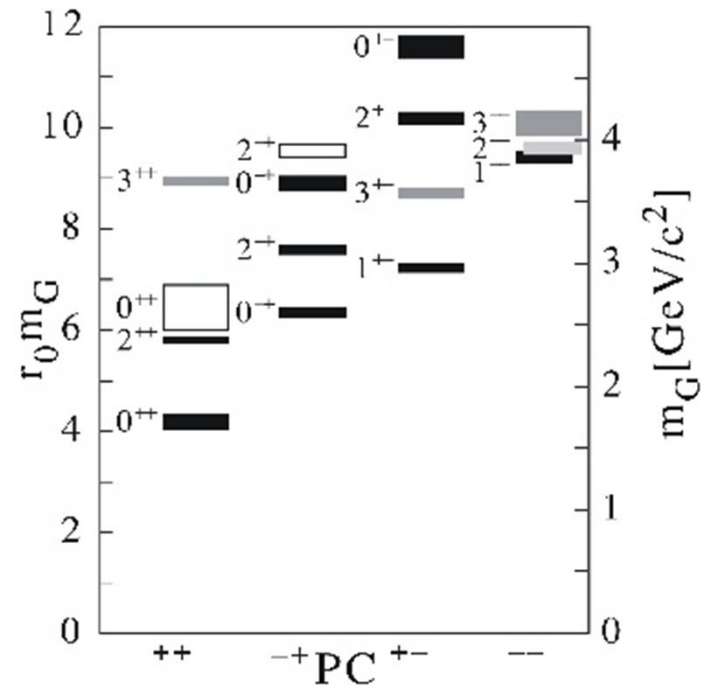
Glueballs

Detailed predictions of mass spectrum from **quenched LQCD**.

- Width of ground state ~ 100 MeV
- Several states predicted below $5 \text{ GeV}/c^2$, some exotic (**oddballs**)
- Exotic heavy glueballs:
 - $m(0^{+-}) = 4140(50)(200) \text{ MeV}$
 - $m(2^{+-}) = 4740(70)(230) \text{ MeV}$
 - **predicted narrow width**

Can be either formed directly or produced in $\bar{p}p$ annihilation.

Some predicted decay modes $\phi\phi$, $\phi\eta$, $J/\psi\eta$, $J/\psi\phi$...

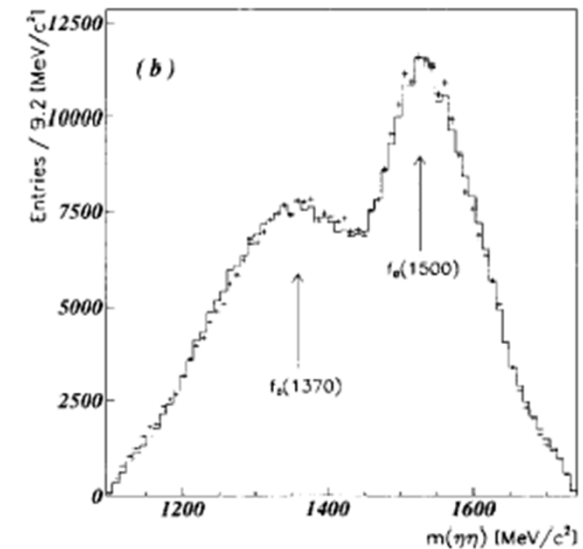


Morningstar und Peardon, PRD60 (1999) 034509
Morningstar und Peardon, PRD56 (1997) 4043

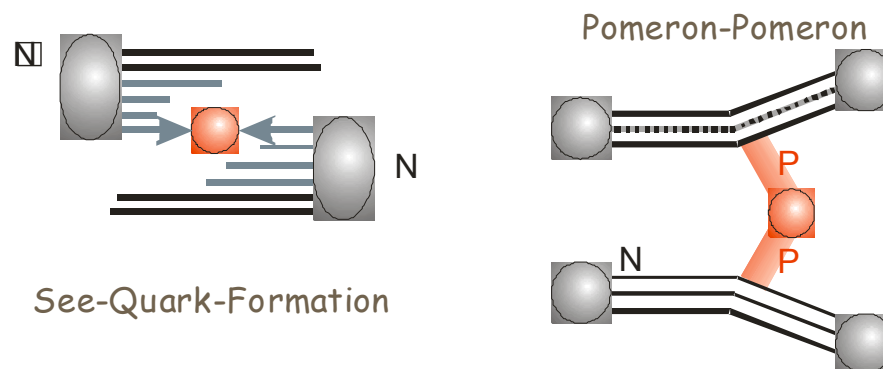
The detection of non-exotic glueballs is not trivial, as these states mix with the nearby $q\bar{q}$ states with the same quantum numbers, thus modifying the expected decay pattern.

- In 1995 through a simultaneous fit to the channels $\pi^0\eta\eta$, $\pi^0\pi^0\eta$ and $3\pi^0$ produced in $\bar{p}p$ annihilations Crystal Barrel discovered three new resonances:

- isovector $a_0(1450)$
- isoscalar $f_0(1370)$ and $f_0(1500)$

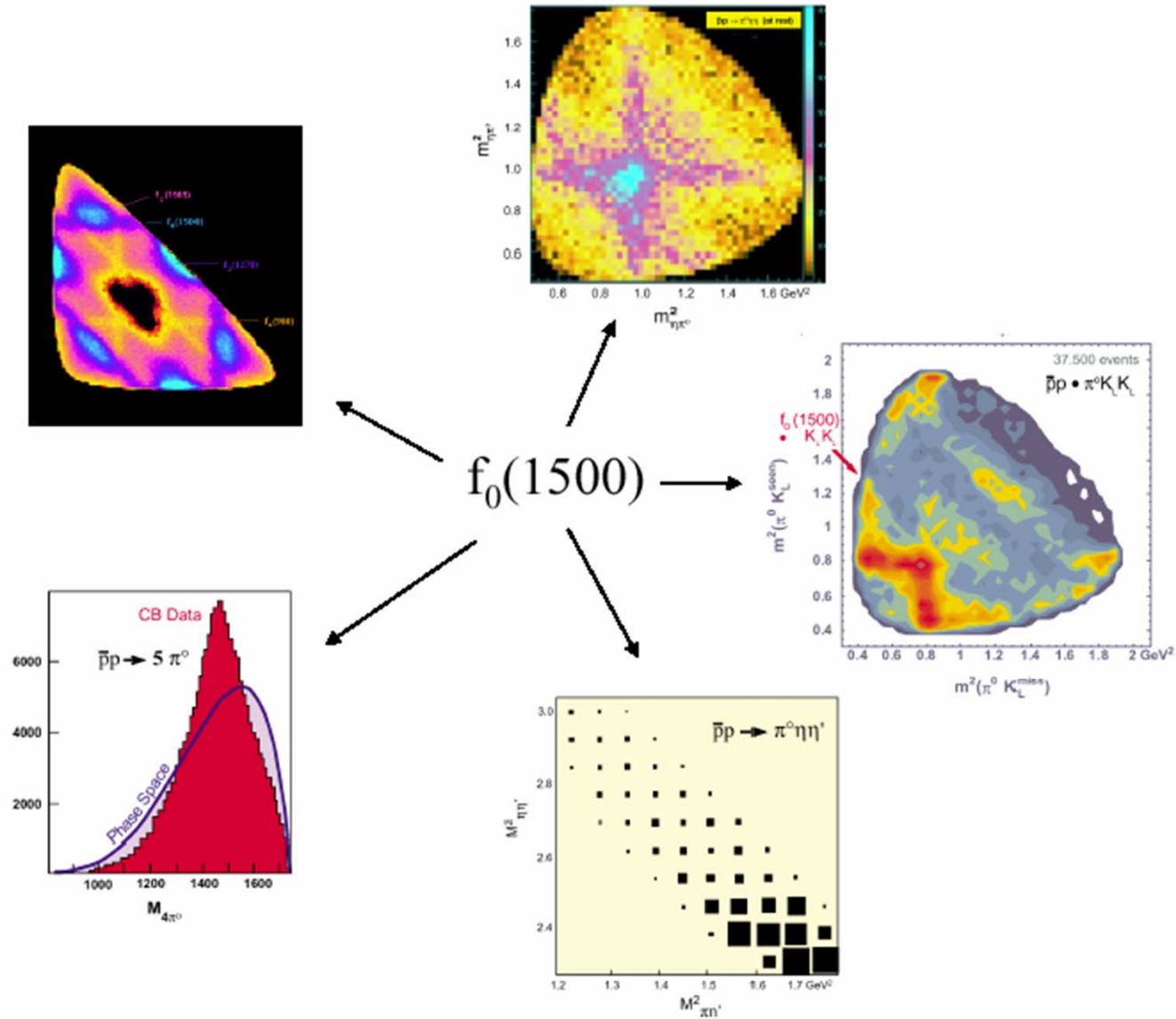


- Confirmed by OBELIX in analysis of $\pi^+\pi^-\pi^0$, $K^+K^-\pi^0$, $KK^0_S\pi$ in $\bar{p}p$ annihilation at rest.
- Confirmed by WA102 in central pp collisions at CERN.



- Crystal Barrel and OBELIX data also confirm the broad $f_0(600)$ and the narrow $f_0(980)$, neither of which are believed to be $q\bar{q}$ states.

$f_0(1500)$ Crystal Barrel data



Scalar Mesons

The PDG classification of the 0^{++} scalar mesons is tentative, because the number of states is bigger than 9.

- $a_0(980)$ and $a_0(1450)$ isovectors
- $f_0(600)$, $f_0(980)$, $f_0(1370)$, $f_0(1500)$, $f_0(1710)$ isoscalars
- $K_0^*(1430)$ and $K_0^*(1950)$ isodoublets.

BUT:

The $a_0(980)$, $f_0(600)$ and $f_0(980)$ are considered non- $q\bar{q}$ states, they are considered exotic candidates (multiquark or $K\bar{K}$ states).

It is then natural to assume that the $f_0(1370)$, $a_0(1450)$ and the strange $K_0^*(1430)$ are in the same SU(3) nonet. A higher-mass isoscalar is required as the ninth member, but we have two: $f_0(1500)$, $f_0(1710)$.

The answer is to include a glueball.

Meson-Glueball Mixing

LQCD calculations predict for the **lightest glueball a scalar** with a mass in the range **1.45 – 1.75 GeV/c²**. A combined analysis of the complete set of two-body decays of the $f_0(1370)$, $f_0(1500)$ and $f_0(1710)$ into pseudoscalar mesons determined the mixing angles and the mass m_G of the bare glueball.

$$\begin{aligned} |f_0(1710)\rangle &= 0.39|gg\rangle + 0.91|s\bar{s}\rangle + 0.14|N\bar{N}\rangle \\ |f_0(1500)\rangle &= -0.69|gg\rangle + 0.37|s\bar{s}\rangle - 0.62|N\bar{N}\rangle \\ |f_0(1370)\rangle &= 0.60|gg\rangle - 0.13|s\bar{s}\rangle - 0.79|N\bar{N}\rangle \end{aligned}$$

$$|N\bar{N}\rangle = \frac{|u\bar{u} + d\bar{d}\rangle}{\sqrt{2}}$$

$$m_G = 1440 \pm 16 \text{ MeV} / c^2$$

We have the following picture:

$a_0(1450)$, $K_0^*(1430)$, $f_0(1370)$, $f_0(1710)$ 0^{++} scalar nonet

$f_0(600)$, $f_0(980)$, $a_0(980)$ multiquark or $K \bar{K}$ states

$f_0(1500)$ scalar glueball

In this scenario it is fair to say that the lightest glueball was discovered at LEAR.

There are, however, alternative viewpoints:

$a_0(980)$, $K_0^*(1430)$, $f_0(980)$, $f_0(1500)$ $n=1$, 0^{++} scalar nonet

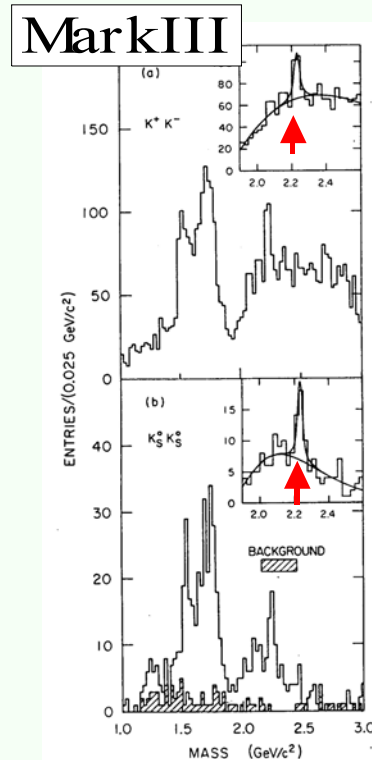
$a_0(1450)$, $K_0^*(1950)$, $f_0(1370)$, $f_0(1710)$ $n=2$, 0^{++} scalar nonet

Tensor Glueball

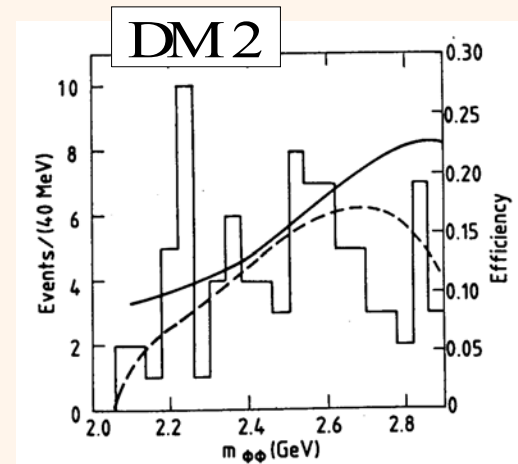
If there is a scalar glueball with a mass of $1.44 \text{ GeV}/c^2$ then LQCD predicts a **tensor glueball** with a mass around $2.0 \text{ GeV}/c^2$.

First candidate observed in 1986 in radiative J/ψ decays, named $\xi(2220)$.

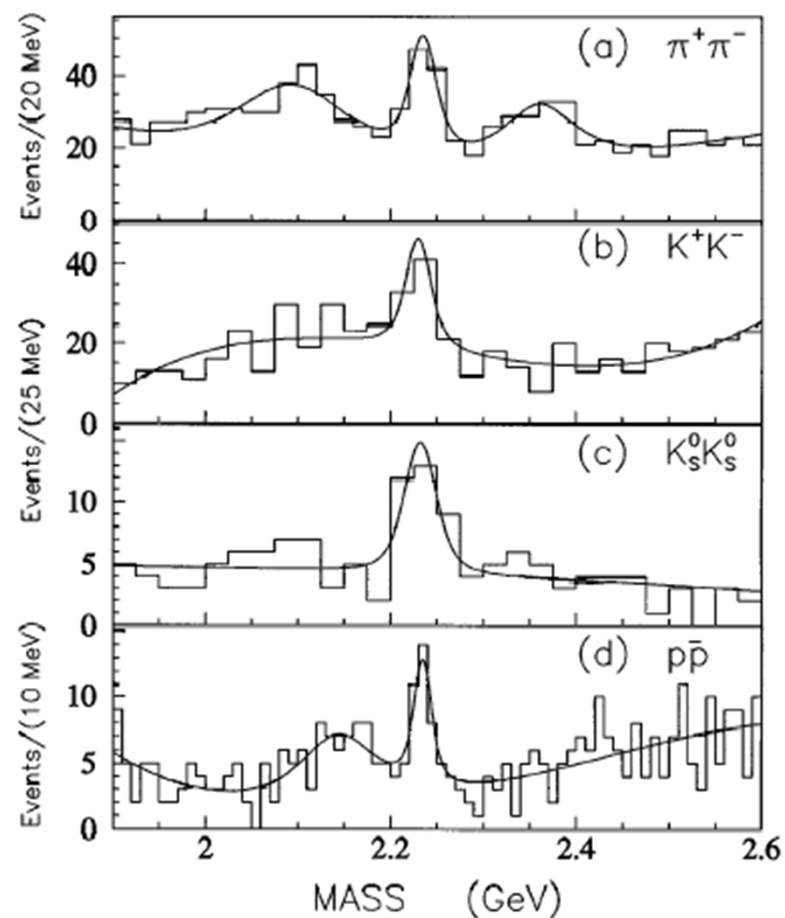
into $K\bar{K}$



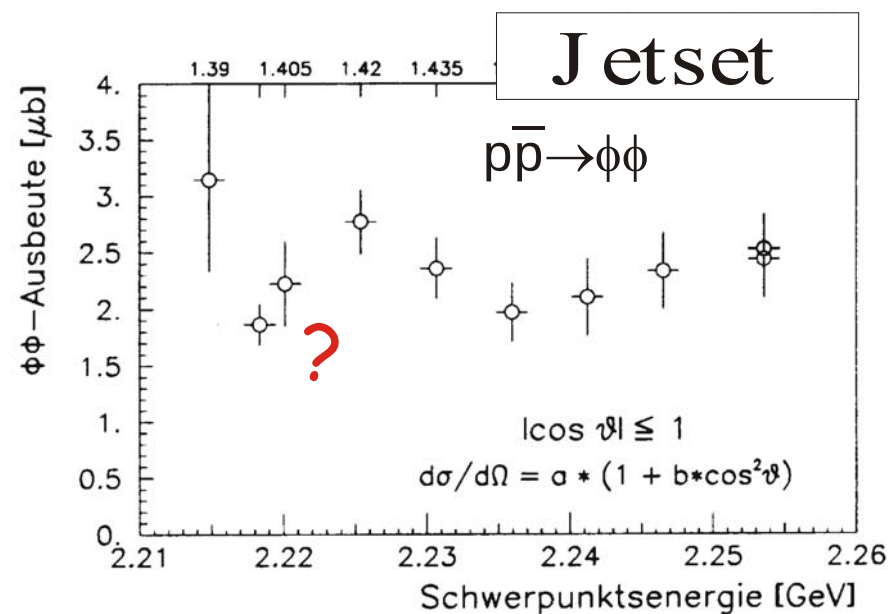
into $\phi\phi$



$\xi(2220)$ confirmed by BES



$\xi(2220)$ NOT confirmed by JETSET ...



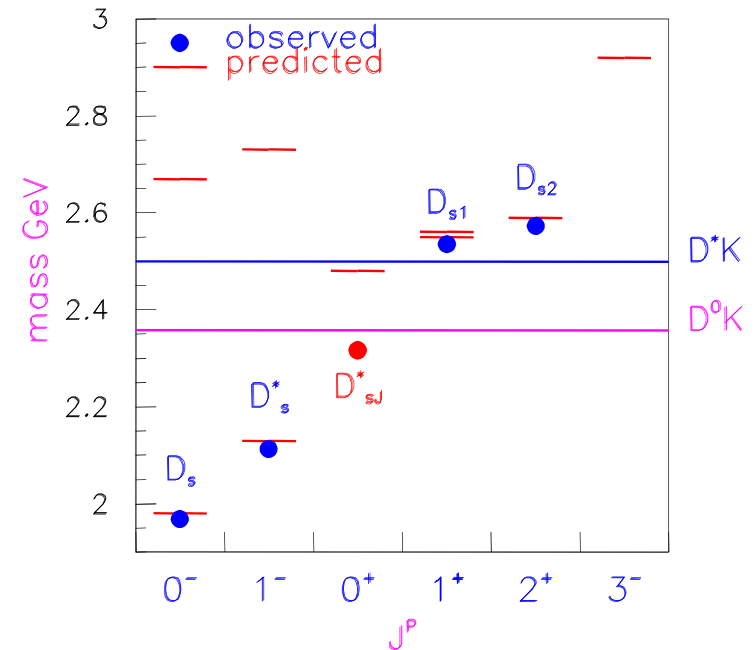
... $\xi(2220)$ NOT seen by Crystal Barrel either

Tensor Glueball situation still confused

Heavy-Light Systems

Introduction

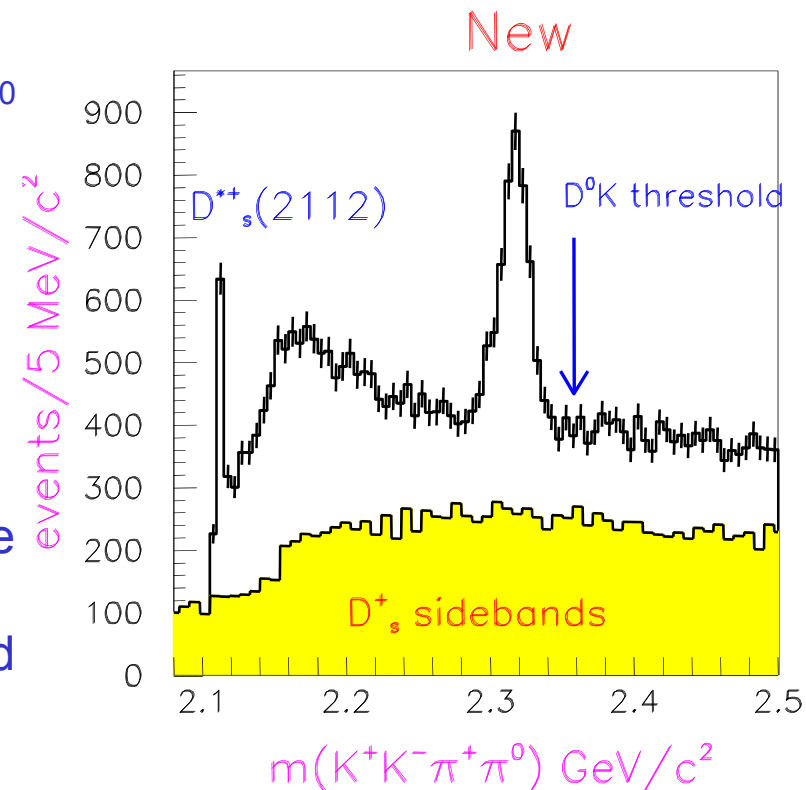
- Quark potential models are used to describe the D_s sector
 - E.g., model of Godfrey, Isgur & Kokoski
- Four experimentally observed states
 - D_s , $D_s(2112)$, $D_{s1}(2536)$, $D_{s2}(2573)$
- Some missing states
 - Two with masses ~ 2.4 to 2.6 GeV
 - Decaying to D^0K , difficult to see
- A state below D^0K threshold could be narrow
- Observation: a state at 2317 MeV, below D^0K threshold



S. Godfrey and N. Isgur, *Phys. Rev.* **D32**, 189 (1985);
 S. Godfrey and R. Kokoski, *Phys. Rev.* **D43**, 1679 (1991).
 M. Di Piero and E. Eichten, *Phys. Rev.* **D64**, 114004 (2001).

$D_S^\pm \pi^0$ Mass Spectrum for $D_S^\pm$ Signal and Sideband Regions

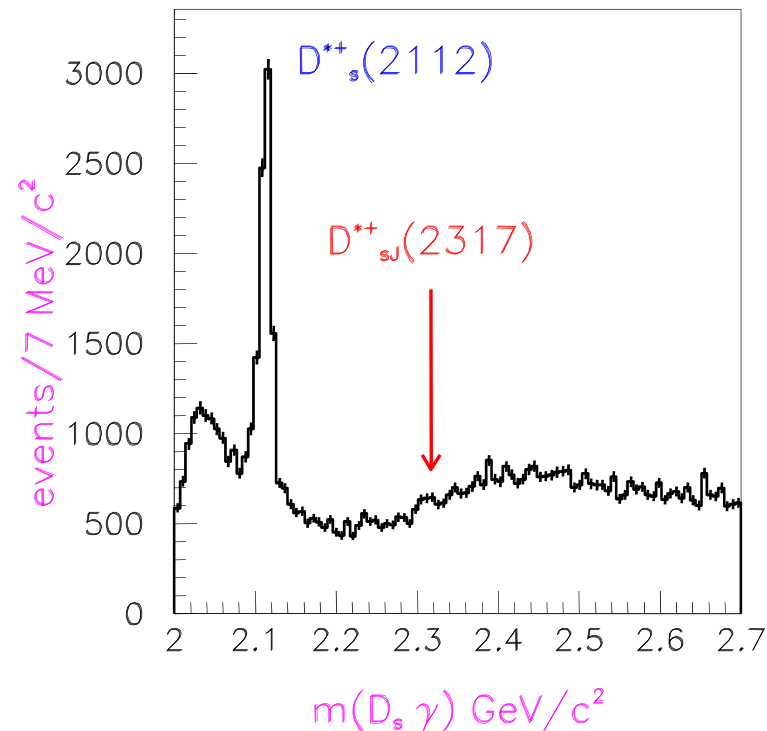
- Combine $D_S^\pm$ candidates from signal and sideband regions with π^0 candidates
 - Narrow signal seen near $2.32 \text{ GeV}/c^2$
 - ~ 2200 events
- No signal seen in sideband regions
 - Shows signal is associated with the $D_S^\pm$
 - Other checks show also associated with the π^0
- Also see known state at $2.112 \text{ GeV}/c^2$



$D_{sJ}^*(2317)^\pm$ - Other Decay Modes

- Studied decay modes
 1. $D_S^\pm \gamma$
 2. $D_S^\pm \gamma \gamma$
 3. $D_S^{*\pm}(2112) \gamma$
 4. $D_S^\pm \pi^0 \pi^0$
 5. $D_S^\pm \pi^0 \gamma$
- No significant signals seen with current statistics in first four decay modes
- Possible structure near 2.46 GeV/c^2 in $D_S^\pm \pi^0 \gamma$

Example: $D_S^\pm \gamma$



A Possible $D_{sJ}^*(2317)^\pm$ to $D_S^\pm \pi^0 \gamma$ Decay?

Small peak where

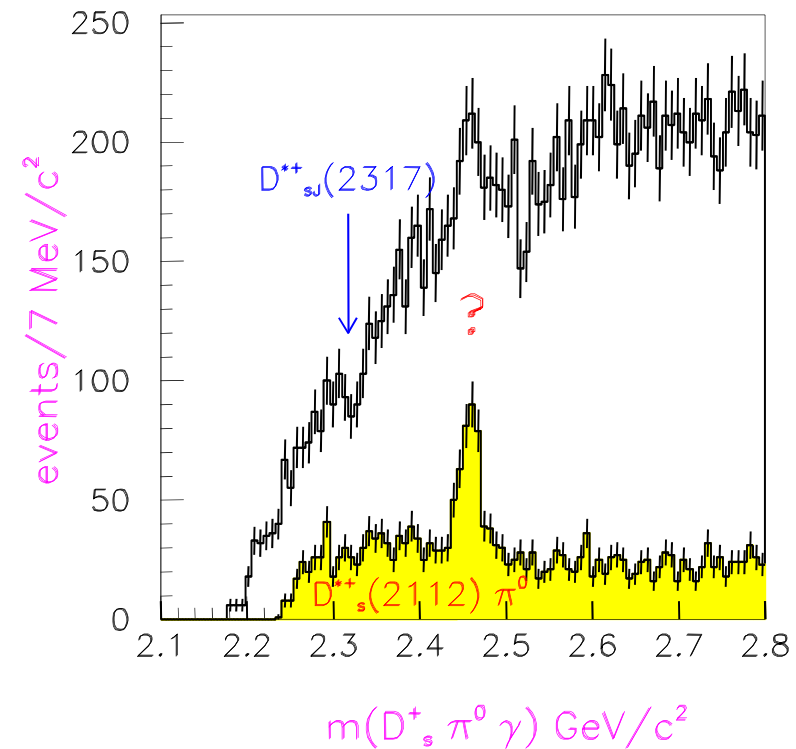
- $D_S(2112)^\pm \rightarrow D_S^\pm \gamma$ and
 $D_{sJ}(2317)^\pm \rightarrow D_S^\pm \pi^0$ overlap

A state at 2.46 GeV/c^2

- $e^+e^- \rightarrow X(2460)^\pm X_{\text{recoil}}$ with
 $\rightarrow D_S(2112)^\pm \pi^0$
- would mimic a peak in
 $D_S^\pm \pi^0$ near 2.32 GeV/c^2
- But expected width $\sim 15 \text{ MeV}$
- If decay is 100% to $D_S^\pm \pi^0$
only $\sim 1/6$ of observed peak
at 2.32 GeV/c^2 explainable

Not only source of 2.32 GeV/c^2 signal

Possible signal at 2.46 GeV/c - Requires additional detailed study



Summary

We observe a narrow signal in the inclusive $D_S^\pm \pi^0$ mass spectrum with fitted parameters

$$m = 2316.8 \pm 0.4 \text{ MeV}/c^2$$

$$\sigma = 8.6 \pm 0.4 \text{ MeV}/c^2$$

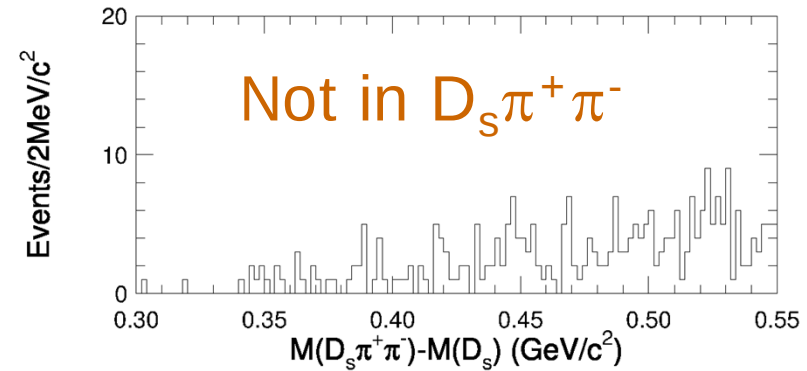
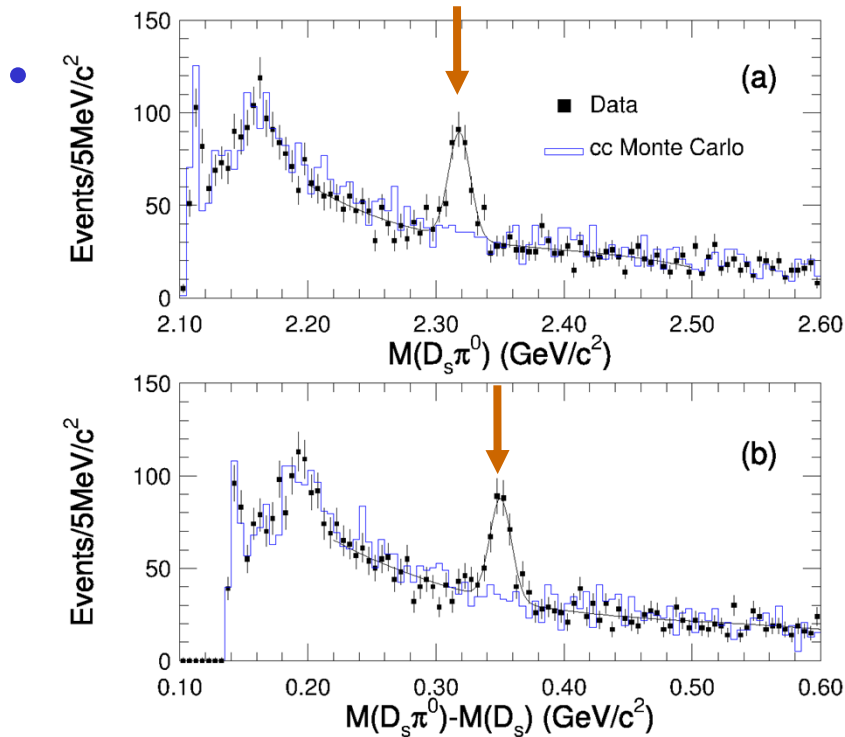
with a systematic error on the mass . 3 MeV/ c^2

- Observed width consistent with experimental resolution
- Intrinsic width small, $\Gamma < 10 \text{ MeV}$

Small peak at 2.46 GeV/ c^2 in $D_S^\pm \pi^0 \gamma$ seen, needs more study

Work in progress for $D_S^\pm \pi^\pm$ modes

CLEO Sees it Too



They use 13.5 fb⁻¹

- Signal seen in $D_s \pi^0$
- Not seen in $D_s \pi^+ \pi^-$, $D_s \gamma$, $D_{s1}(2112) \gamma$

Signal has 230^{+31}_{-29} events (» same yield/fb⁻¹ as BABAR).

Conclusions

- $D_{sJ}^*(2317)^\pm$ does not fit into existing potential model expectations
 - Godfrey & Isgur (1985), Godfrey & Kokoski (1991)
 - Below DK threshold
- Small width likely related isospin violating decay
- Could be a four-quark scalar state
 - Suggested by R.L. Jaffe, H.J. Lipkin in 1977
 - Will have similarities & differences with light-quark scalar states and charm, non-strange scalar states
 - Analogous to Belle's non-strange 2290 MeV/c² state?
- Interesting times ahead

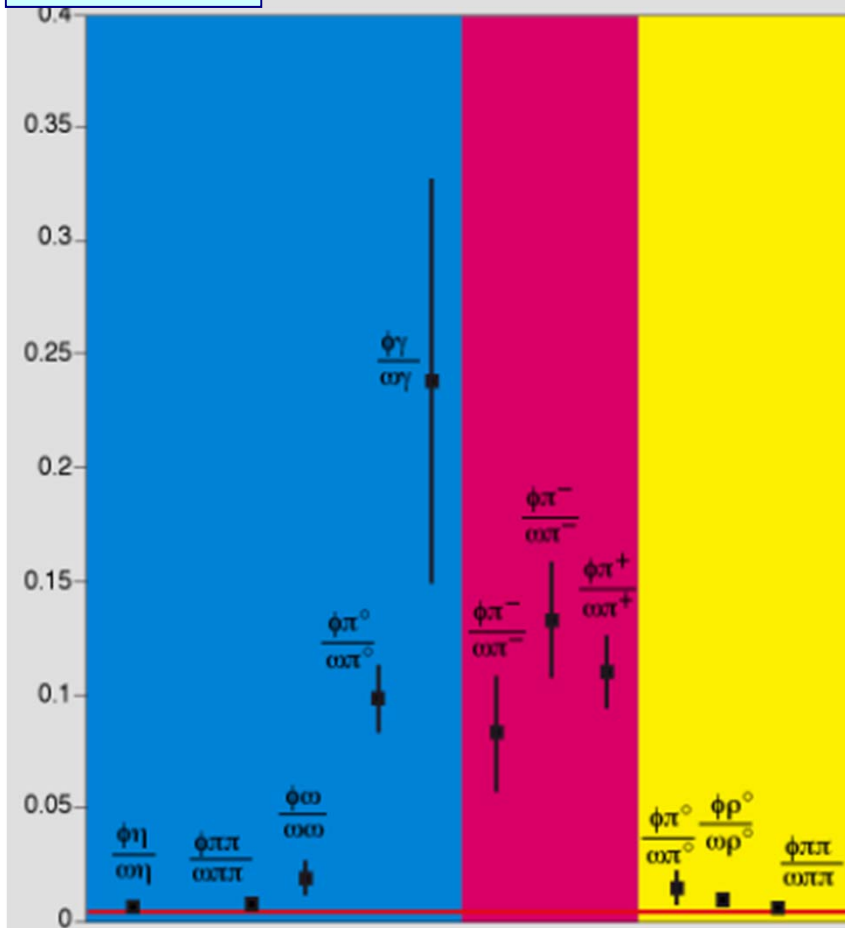
S. Godfrey and N. Isgur, *Phys. Rev.* **D32**, 189 (1985);
S. Godfrey and R. Kokoski, *Phys. Rev.* **D43**, 1679 (1991).
M. Di Pierro and E. Eichten, *Phys. Rev.* **D64**, 114004 (2001).

R.L. Jaffe, *Phys. Rev.* **D15**, 267 (1977); *Phys. Rev.* **D15**, 281 (1977).
H.J. Lipkin, *Phys. Lett.* **70B**, 113 (1977); *Phys. Lett.* **172B**, 242 (1986);
N. Isgur and H.J. Lipkin, *Phys. Lett.* **99B**, 151 (1981).

OZI Rule Violations

$$R = \frac{\sigma(\phi X)}{\sigma(\omega X)}$$

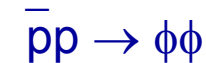
$\bar{p}$ annihilation at rest



$$R = \frac{\sigma(\phi X)}{\sigma(\omega X)} = f \cdot \tan^2(\theta_v - \theta_i)$$

Strange quark content of the nucleons.

- “Shakeout” (intrinsic $s \bar{s}$ component)
- “Rearrangement”
- The reaction



provides additional evidence for intrinsic $s \bar{s}$ pairs in nucleon.

$$\sigma(\bar{p}p \rightarrow \phi\phi) = \sigma(\bar{p}p \rightarrow \omega\omega) \tan^4(\theta_v - \theta_i)$$

Prediction ≈ 10 nb

Measurement ≈ 3700 nb

$\bar{P}$ ANDA AT GSI

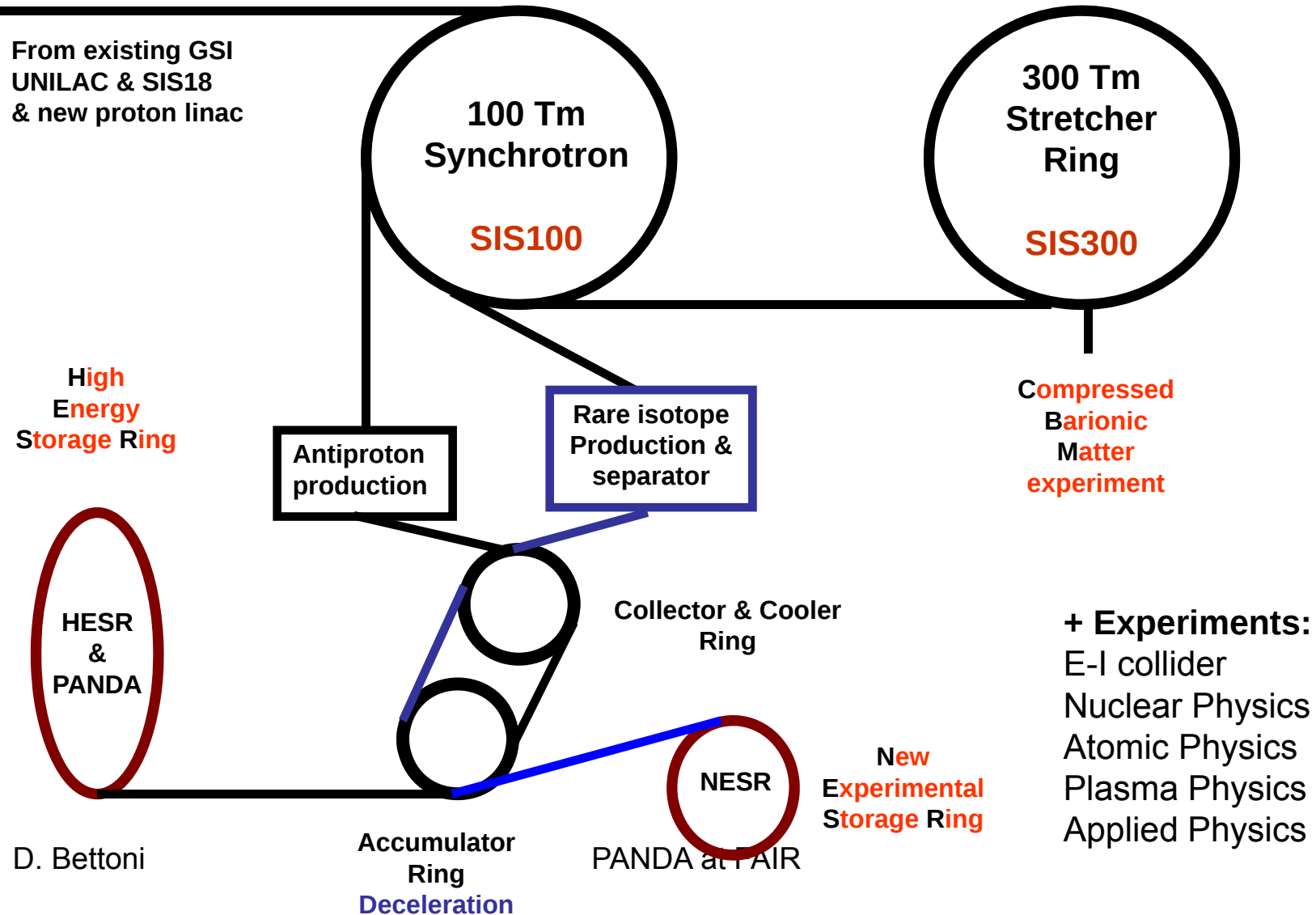
FAIR at a glance



D. Bettoni

PANDA at FAIR

The FAIR Complex



Unprecedented System Parameters at FAIR

Beam Intensity:

- primary heavy-ion beam intensity increases by $\times 100 - \times 1000$
- secondary beam intensity increases by up to $\times 10000$

Beam Energy:

- heavy-ion energy : $\times 30$

Beam Variety:

- antiprotons
- protons to uranium & radioactive ion beams

Beam Precision:

- cooled antiproton beams
- intense cooled radioactive ion beams

Beam Pulse structure:

- optimized for experiments: from dc to 50 ns

Parallel Operation:

- full accelerator performance for up to four different and independent experiments and experimental programs

High-Energy Storage Ring

- Production rate $2 \times 10^7/\text{sec}$

- $P_{\text{beam}} = 1 - 15 \text{ GeV/c}$

- $N_{\text{stored}} = 5 \times 10^{10} \bar{p}$

- Internal Target

High resolution mode

- $\delta p/p \sim 10^{-5}$ (electron cooling)

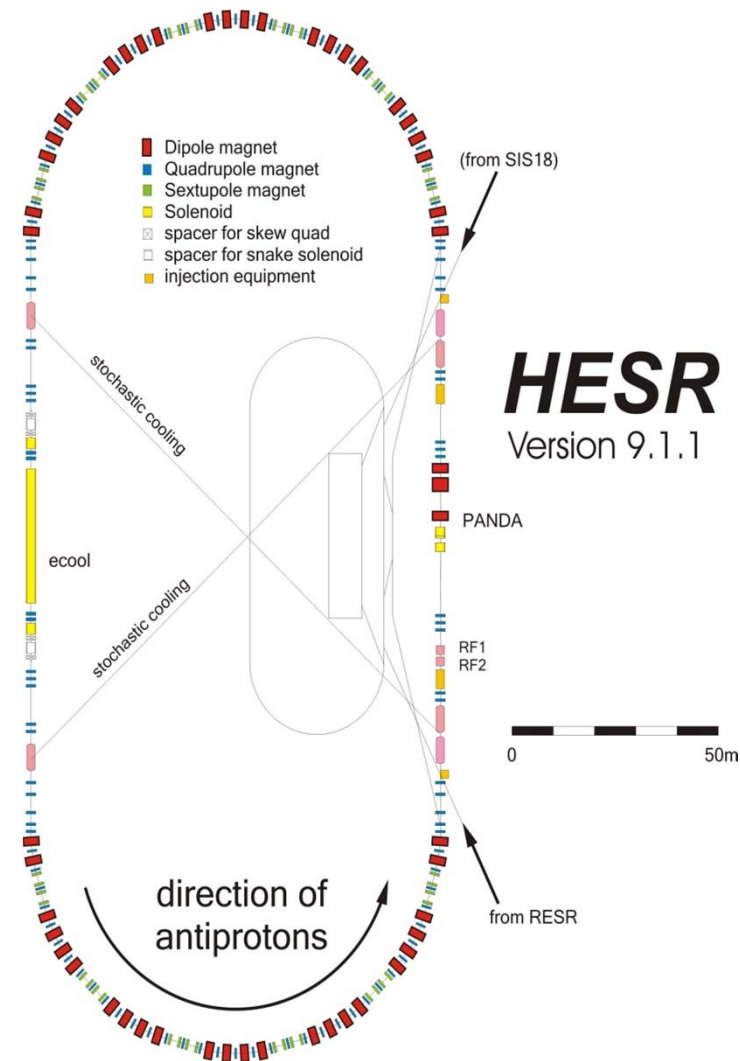
- Lumin. = $10^{31} \text{ cm}^{-2} \text{ s}^{-1}$

High luminosity mode

- Lumin. = $2 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$

- $\delta p/p \sim 10^{-4}$ (stochastic cooling)

D. Bettoni



PANDA at FAIR

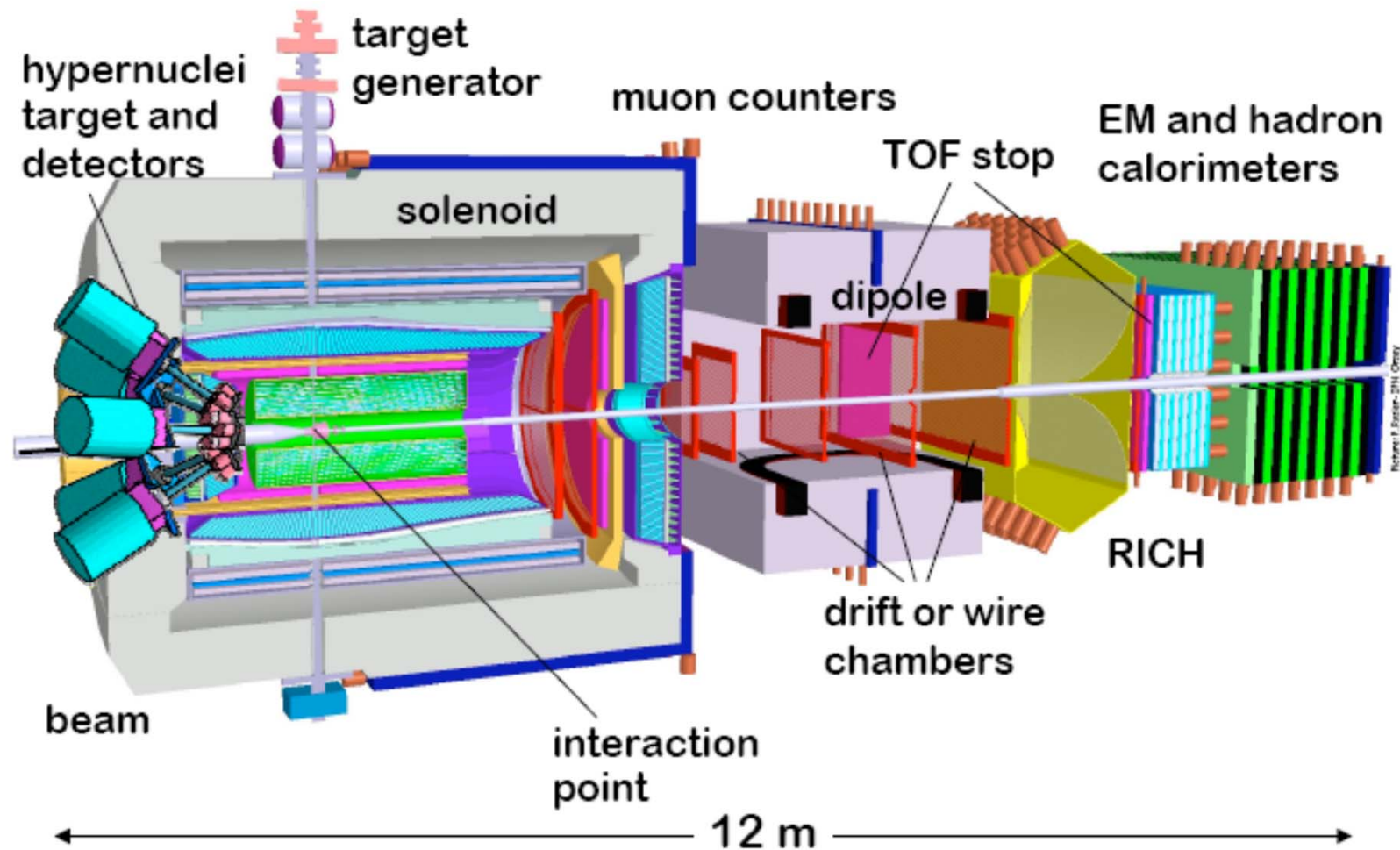
PANDA Physics Program

- **Charmonium Spectroscopy**. Precision measurement of masses, widths and branching ratios of all ($c \bar{c}$) states (hydrogen atom of QCD).
- Search for gluonic excitations (**hybrids, glueballs**) in the charmonium mass range (3-5 GeV/c²).
- Search for **modifications of meson properties in the nuclear medium**, and their possible relation to the partial restoration of chiral symmetry for light quarks.
- Precision γ -ray spectroscopy of single and double **hypernuclei**, to extract information on their structure and on the hyperon-nucleon and hyperon-hyperon interaction.
- Electromagnetic processes (DVCS, D-Y, **FF** ...) , open charm physics

The Detector

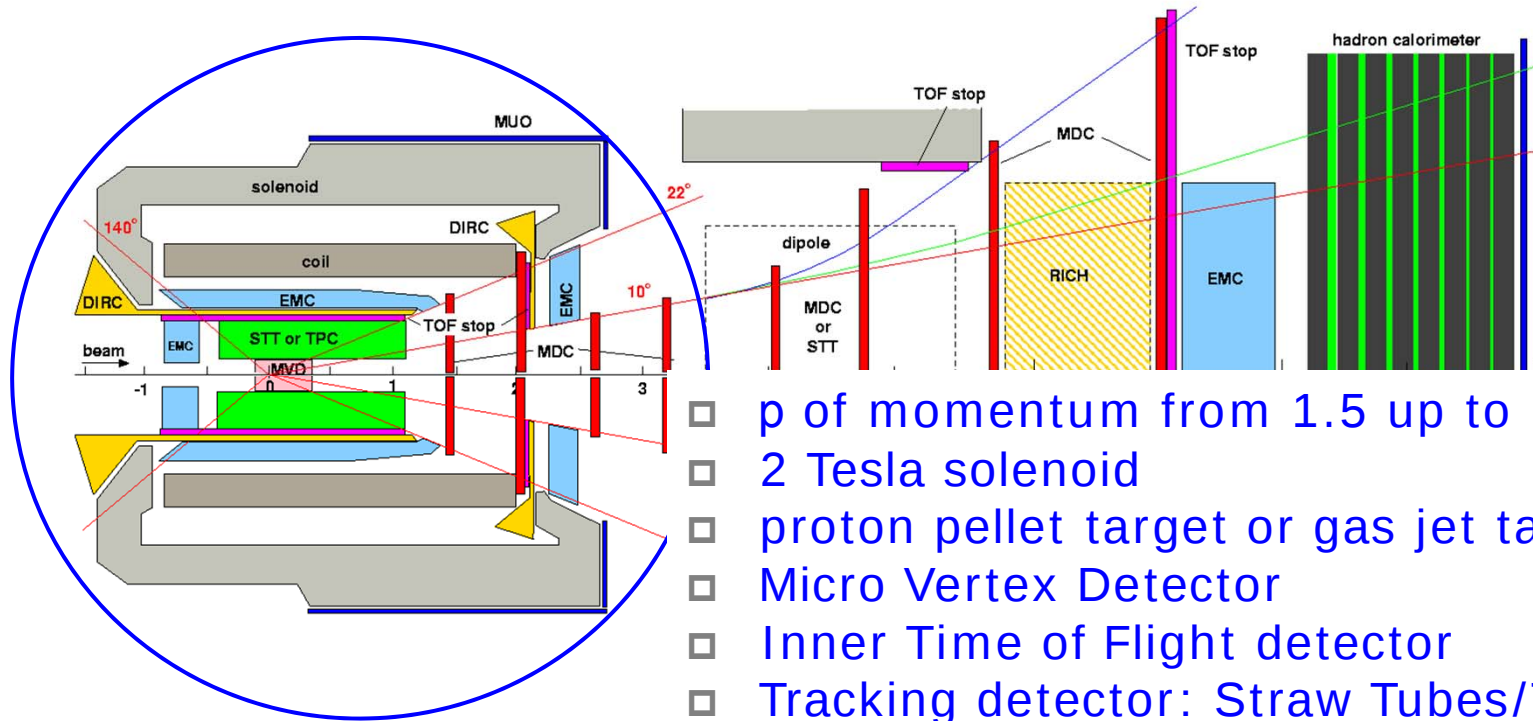
- **Detector Requirements:**
 - (Nearly) 4π solid angle coverage (partial wave analysis)
 - High-rate capability (2×10^7 annihilations/s)
 - Good PID (γ , e , μ , π , K , p)
 - Momentum resolution ($\approx 1\%$)
 - Vertex reconstruction for D , K_s^0 , Λ
 - Efficient trigger
 - Modular design
- **For Charmonium:**
 - Pointlike interaction region
 - Lepton identification
 - Excellent calorimetry
 - Energy resolution
 - Sensitivity to low-energy photons

Panda Detector



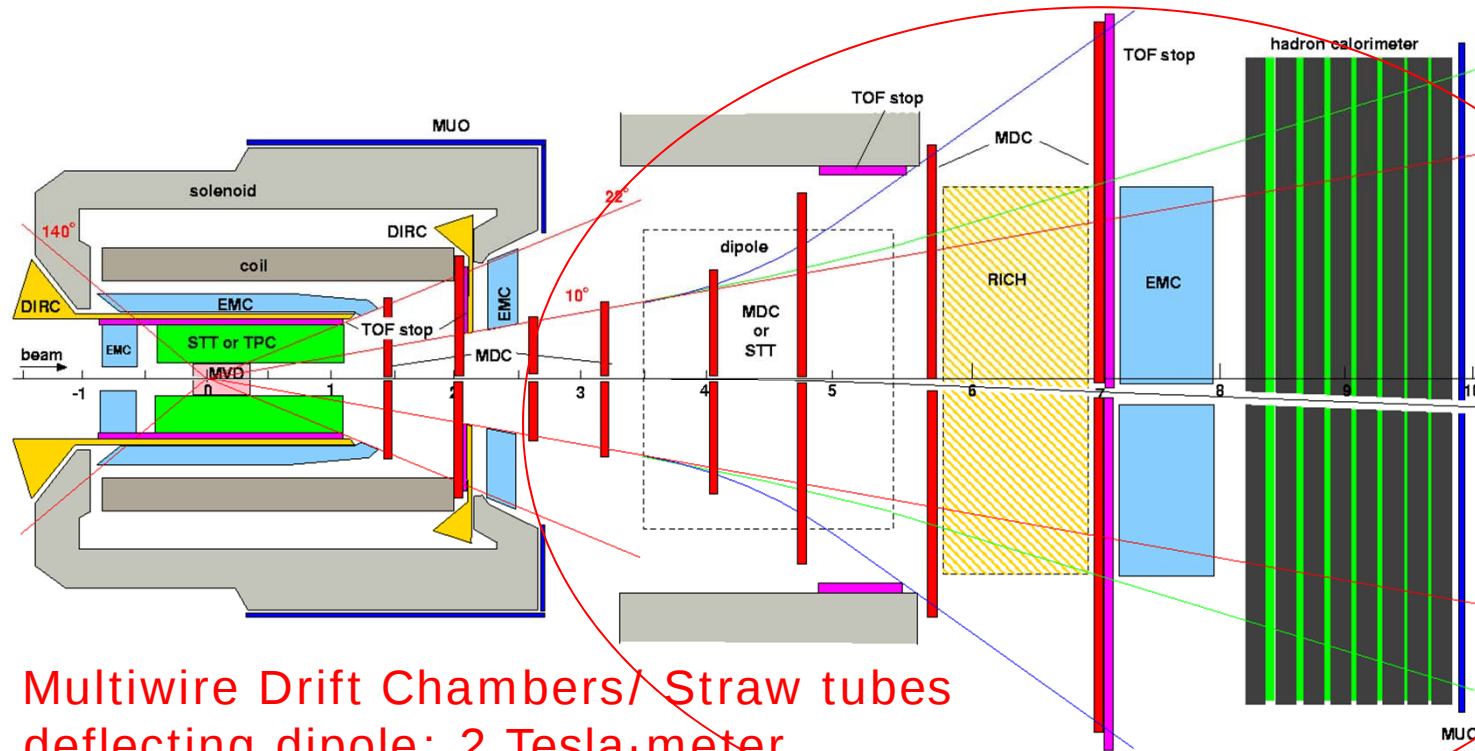


Target Spectrometer



- p of momentum from 1.5 up to 15 GeV/c
- 2 Tesla solenoid
- proton pellet target or gas jet target
- Micro Vertex Detector
- Inner Time of Flight detector
- Tracking detector: Straw Tubes/TPC
- DIRC
- Electromagnetic Calorimeter
- Muon counters
- Multiwire Drift Chambers

Forward Spectrometer



- ❑ Multiwire Drift Chambers/ Straw tubes
- ❑ deflecting dipole: 2 Tesla-meter
- ❑ Forward DIRC and RICH
- ❑ Forward Electromagnetic Calorimeters
- ❑ Time of Flight counters
- ❑ Hadron Calorimeter

PANDA Collaboration

- At present a group of **350 physicists** from **47 institutions of 15 countries**

Austria – Belaruz - China - Finland - France - Germany – Italy – Poland – Romania -
Russia – Spain - Sweden – Switzerland - U.K. – U.S.A..

Basel, Beijing, Bochum, Bonn, IFIN Bucharest, Catania, Cracow, Dresden, Edinburg, Erlangen, Ferrara, Frankfurt, Genova, Giessen, Glasgow, GSI, Inst. of Physics Helsinki, FZ Jülich, JINR Dubna, Katowice, Lanzhou, LNF, Mainz, Milano, Minsk, TU München, Münster, Northwestern, BINP Novosibirsk, Pavia, Piemonte Orientale, IPN Orsay, IHEP Protvino, PNPI St. Petersburg, Stockholm, Dep. A. Avogadro Torino, Dep. Fis. Sperimentale Torino, Torino Politecnico, Trieste, TSL Uppsala, Tübingen, Uppsala, Valencia, SINS Warsaw, TU Warsaw, AAS Wien