



# University of Ferrara

## PhD in Physics – XXV cycle

### Calibration and performances of in-situ gamma ray spectrometer

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Applied Geophysics Laboratory



università di ferrara

Physics Department

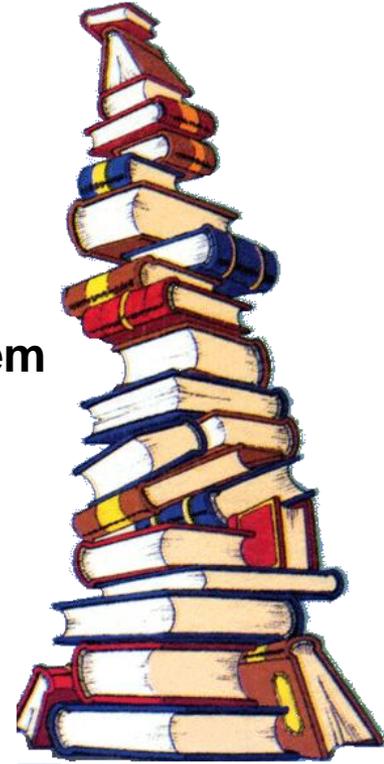


ISTITUTO NAZIONALE  
DI FISICA NUCLEARE

Legnaro National Laboratory

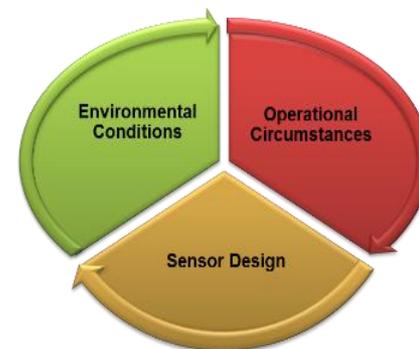
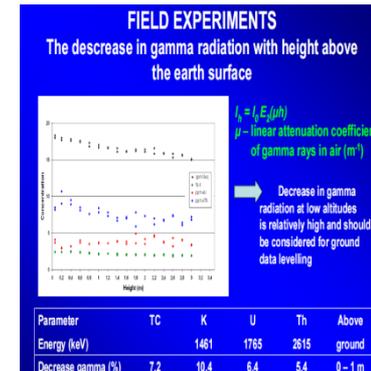
# Summary

- **Scientific motivation of this study**
- **Gamma – ray spectroscopy in situ. The ZnAl\_1.0 instrument**
- **Gamma – ray spectroscopy in laboratory. The MCA\_Rad system**
- **Investigation of different parameters in-situ measurements**
- **Analysis of data**
- **Conclusions**
- **Publications**



# Scientific motivation

- The use of portable spectrometer for gamma-ray spectroscopy in situ is a task required for: geological, environmental and mining explorations.
- Not only  $^{40}\text{K}$ ,  $^{238}\text{U}$ , and  $^{232}\text{Th}$  have to be measured, but also an important key is determination of anthropic elements abundances like  $^{137}\text{Cs}$  and  $^{131}\text{I}$ , which are used to monitor the effect of nuclear accidents or other human activities.
- In  $\gamma$ -ray spectrometry surveys, it is essential to apply accurate altitude correction. The height of the detector above the ground is an important parameter for an appropriate characterization of the site<sup>1234</sup>.
- Several factors can effect the measured concentrations of radioactive nuclides in situ gamma ray spectroscopy<sup>5</sup>.



<sup>1</sup> R. L. Grasty., 1975 Atmospheric Absorption of 2.62 MeV Gamma ray Photons emitted from the ground. Geophysics vol 40, 1058-1065.

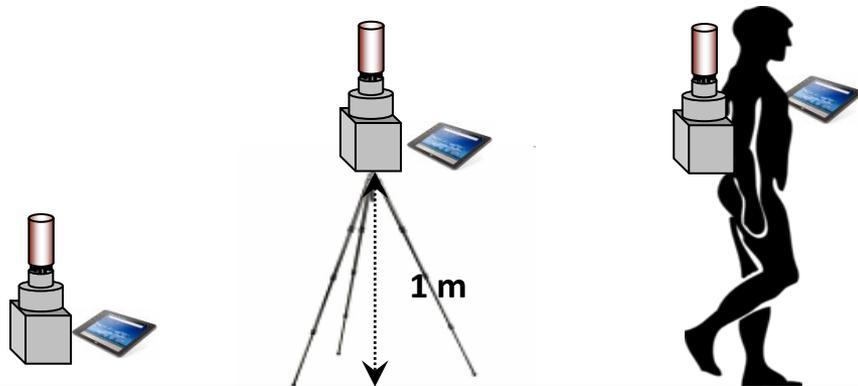
<sup>2</sup> Grasty et al., 1979 Fields of view of airborne gamma ray detectors. Geophysics, vol 44, 1447 – 1157.

<sup>3</sup>Guidelines for radioelement mapping using gamma ray spectrometry data, IAEA-TECDOC-1363, July 2003

<sup>4</sup>Mantolin and Minty., 2009 Levelling Airborne and ground gamma ray spectrometric data to assist uranium exploration. International Symposium on Uranium Raw Material for Nuclear Fuel Cycle. IAEA 2009.

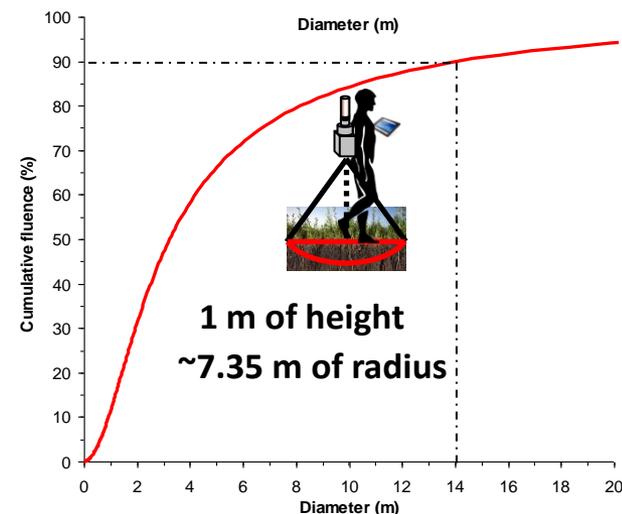
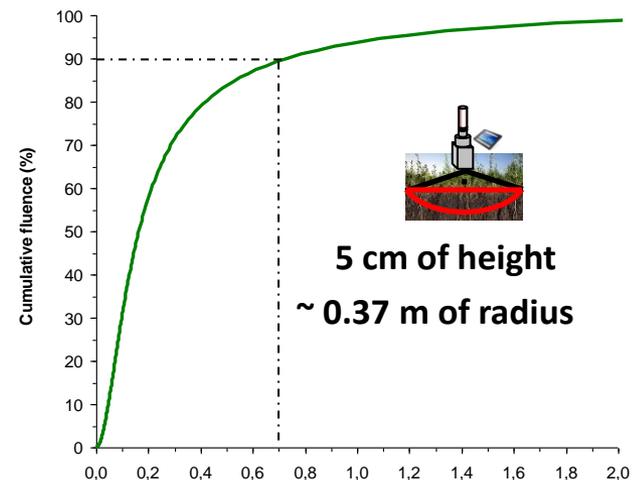
<sup>5</sup>E.H. Loonstral and F.M. van Egmond Factors influencing in situ gamma-ray measurements, EGU 2009-9247

# The ZaNaI\_1.0L instrument: design and features



At height  $h$ , the detector receive 90% of the signal from a circle of radius  $R$

$h$ (m)	0.05	0.5	1.0
$R$ (m)	0.37	3.7	7.35

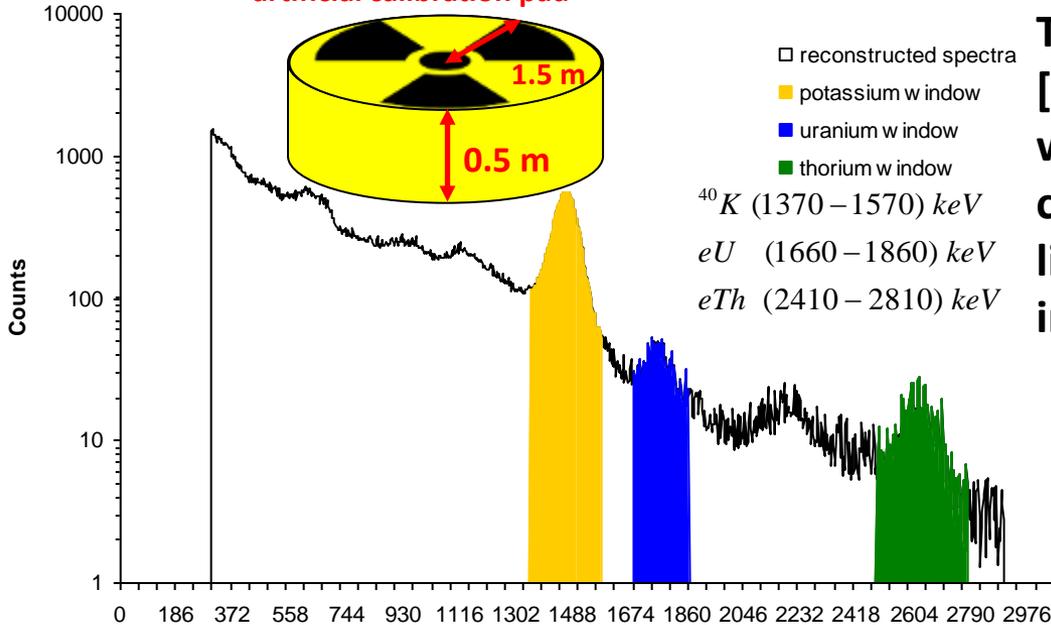


<b>Nal(Tl) detector</b>	<b>1 Liter (102 x 102 x 102 mm)</b>
<b>Energetic resolution</b>	<b>7.3% at 662 keV (<sup>137</sup>Cs)</b>
<b>Real-time feedback</b>	<b>notebook (smartphone &amp; tablet)</b>
<b>Power autonomy</b>	<b>6 hours</b>
<b>Weight (total)</b>	<b>~ 4.5 kg</b>
<b>Acquisition time</b>	<b>5 -10 min (static mode) 10 – 30 sec (dynamic mode)</b>
<b>Auxiliary sensors</b>	<b>Pressure &amp; Temperature</b>

R. L. Grasty., 1975 Atmospheric Absorption of 2.62 MeV Gamma ray Photons emitted from the ground. Geophysics vol 40, 1058-1065.

# Portable $\gamma$ -ray spectrometer: calibration methods

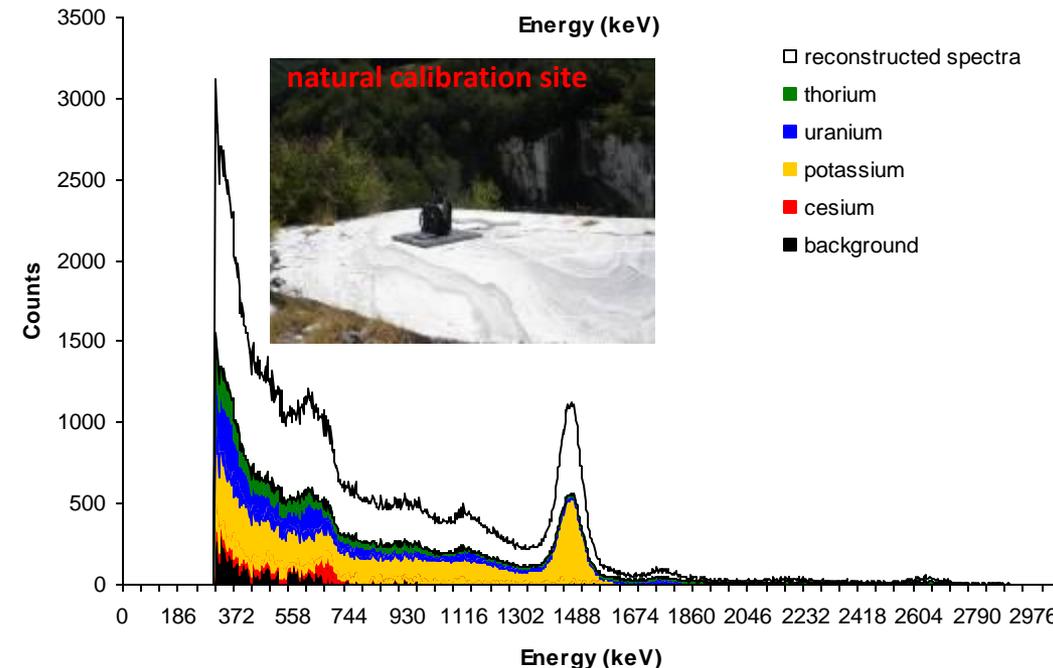
artificial calibration pad



The conventional “**stripping method**” [IAEA 2003] consider the K, eU, eTh window count rates  $[N]$  (background corrected) obtained over the pads are linearly related to the concentrations  $[C]$  in the pads.

$$[N] = [S] \times [C]$$

$[S]$  – 3 x 3 matrix of sensitivities.



The “**full spectrum analysis**” method consider the spectra composed by a number of **standard spectra** as the linear combination.

$$[N]^i = \sum_{j=1}^m [C]_j [S]_j^i$$

$i$  (1 to  $n$ ) channels and  $j$  (1 to  $m$ ) standard spectra.

## $\gamma$ -ray spectroscopy in situ

The ZaNaI\_1.0L is used in different site and it is acquired a total number of 338 spectrums in-situ.

**Time of acquisition for every single spectrum: 5 minutes**

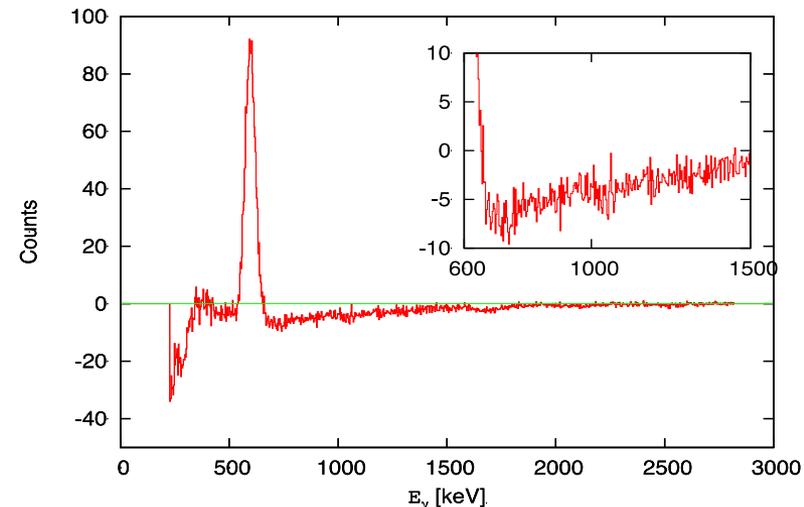
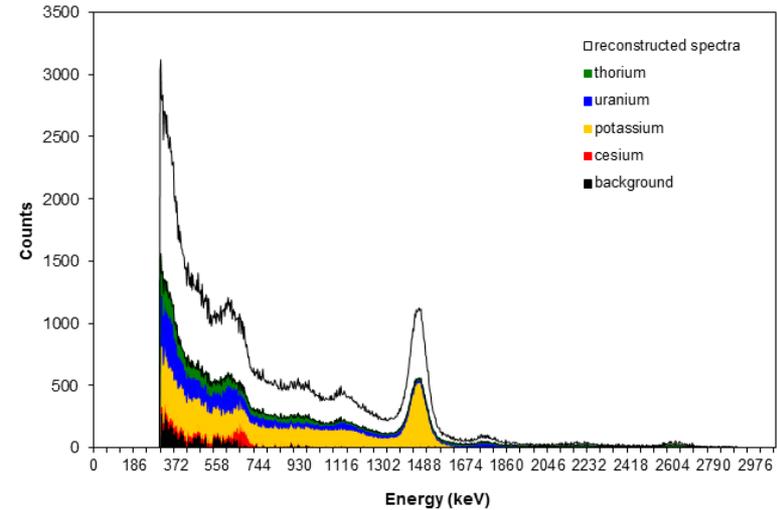
Placement of instrument	Number of sites
ZaNaI_1.0L placed on ground	80 sites (Ombrone Basin)
ZaNaI_1.0L placed on a tripod at 1m height	80 sites (Ombrone Basin)
ZaNaI_1.0 placed on the shoulders of an operator	89 sites (Schio District)
ZaNaI_1.0L placed on ground	89 sites (Schio District)



# FSA with Non-negative least square constrain

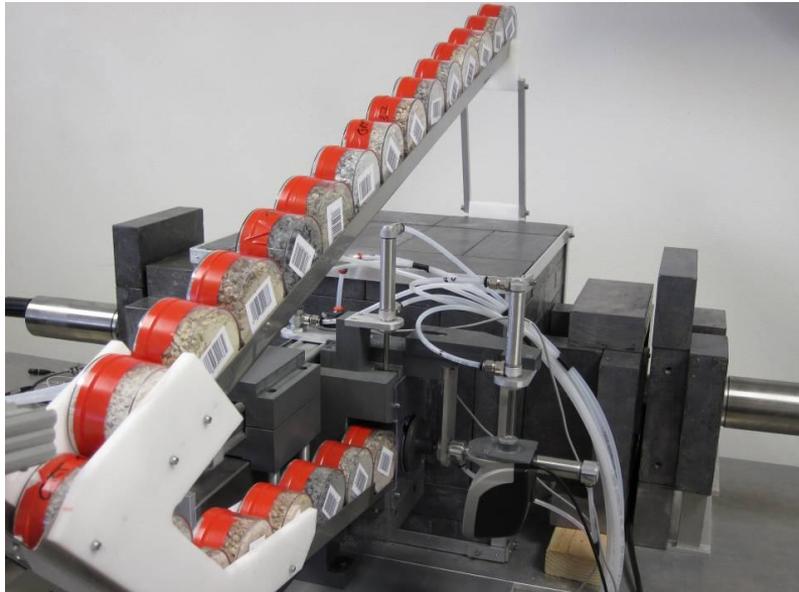
In FSA method the shape of the total spectrum is taken into account and is 'unfolded' into the spectra for the individual radionuclides (*standard spectra*) and a background spectrum.

Obtained the *standard spectra* from the calibration, a Non Negative Least-Square (NNLS) procedure is used to find the optimal activity concentrations



- ✓ It is studied the full range of energy  
450-2900 keV
- ✓ The structural features of the spectrum are included
- ✓ It is investigated the presence of additional radionuclides such as  $^{137}\text{Cs}$ .

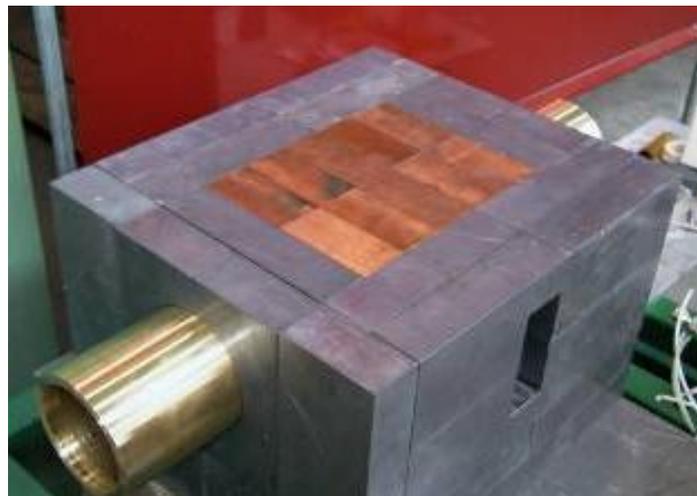
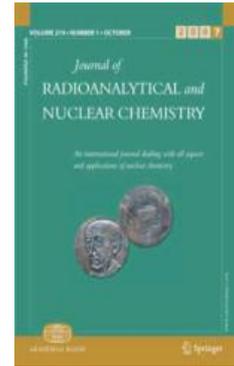
# The MCA\_Rad system



J Radioanal Nucl Chem  
DOI 10.1007/s10967-012-1791-1

## The worldwide NORM production and a fully automated gamma-ray spectrometer for their characterization

G. Xhixha · G. P. Bezzon · C. Brogginì · G. P. Buso · A. Caciolli ·  
I. Callegari · S. De Bianchi · G. Fiorentini · E. Guastaldi · M. Kaçeli Xhixha ·  
F. Mantovani · G. Massa · R. Menegazzo · L. Mou · A. Pasquini ·  
C. Rossi Alvarez · M. Shtyì



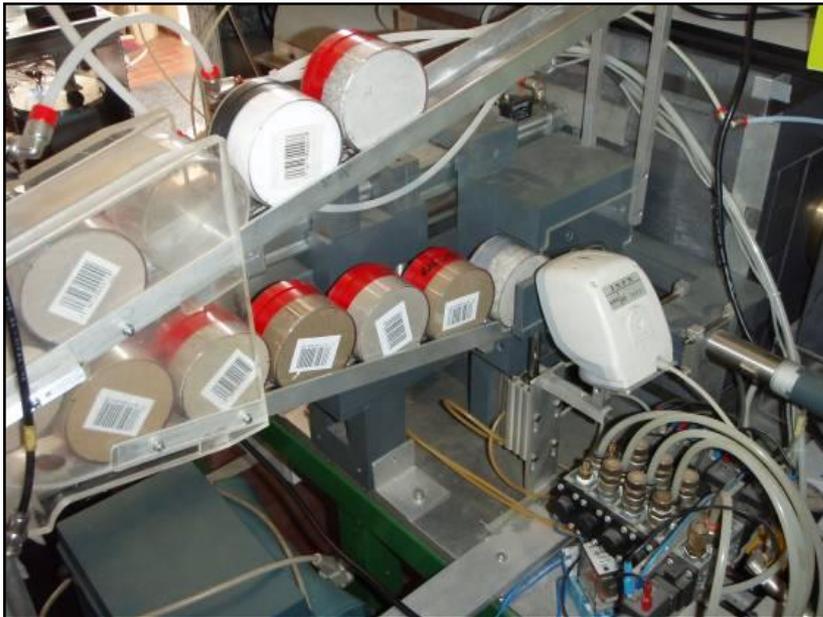
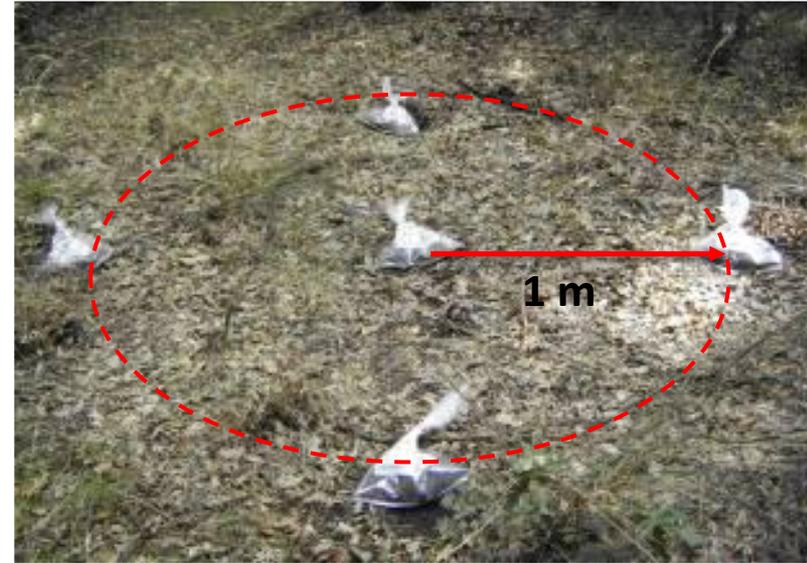
<b>HPGe detectors</b>	<b>Coaxial p-type, 60% of rel. eff.</b>
<b>Energetic resolution</b>	<b>1.9 keV at 1.33 MeV (<sup>60</sup>Co)</b>
<b>Cooling technology</b>	<b>Electromechanical (~ -190°C)</b>
<b>Shielding composition</b>	<b>10 cm Pb and 5 cm of Cu</b>
<b>Standard acquisition time</b>	<b>1 hour (180 cc sample volume)</b>
<b>Automatic sample manage</b>	<b>24 samples</b>

# $\gamma$ -ray spectroscopy in laboratory

Five soil samples on each selected place

- ✓ One central point is `ZaNaI_1.0L` position
- ✓ The other 4 samples 1m apart

A total of **400 soil samples from 80 places** were measured and analysed using a HPGe setup in the University of Ferrara



# DataBase Rad\_Nat.mdb

## Environmental parameters to define in the campaign:

- temperature
- humidity
- climatic conditions
- density of vegetative cover
- typology of vegetative cover

Microsoft Access - [Temp\_Hum\_Tuscany : Tabella]

File Modifica Visualizza Inserisci Formato

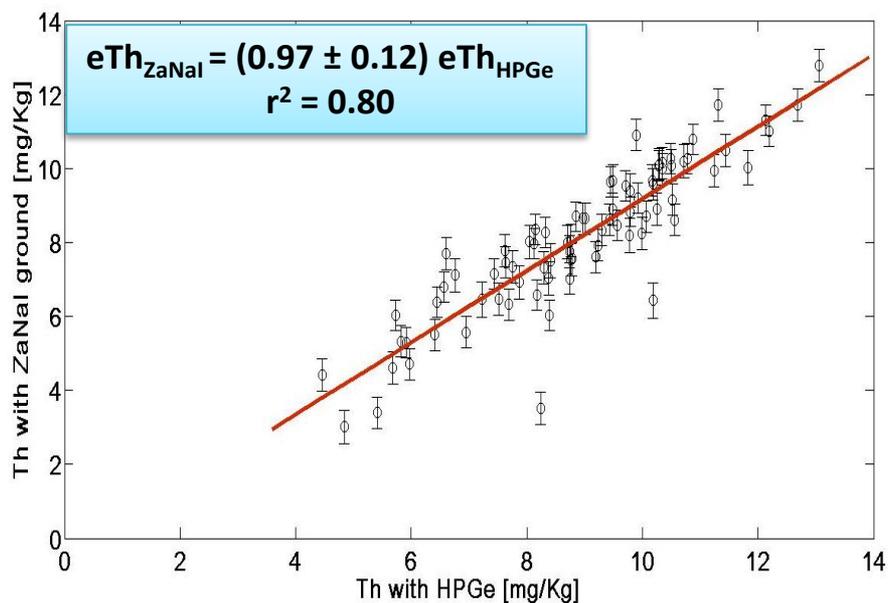
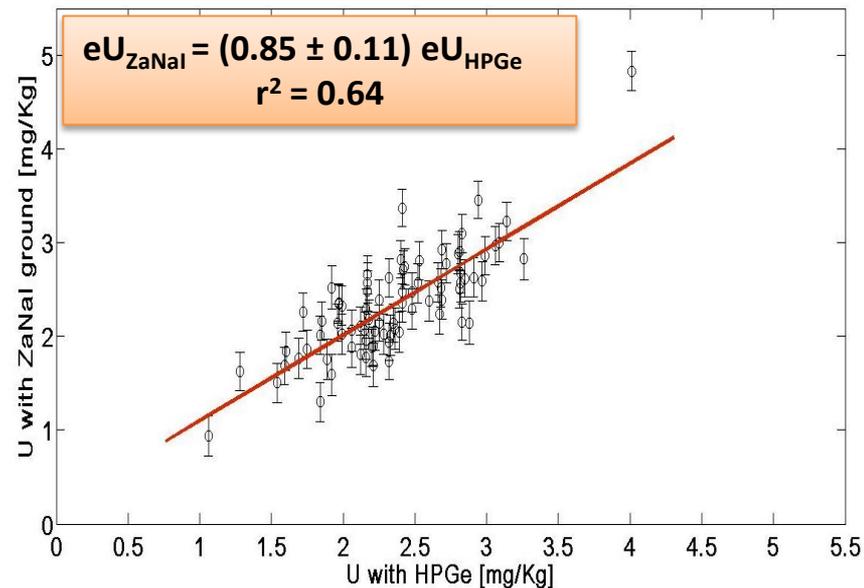
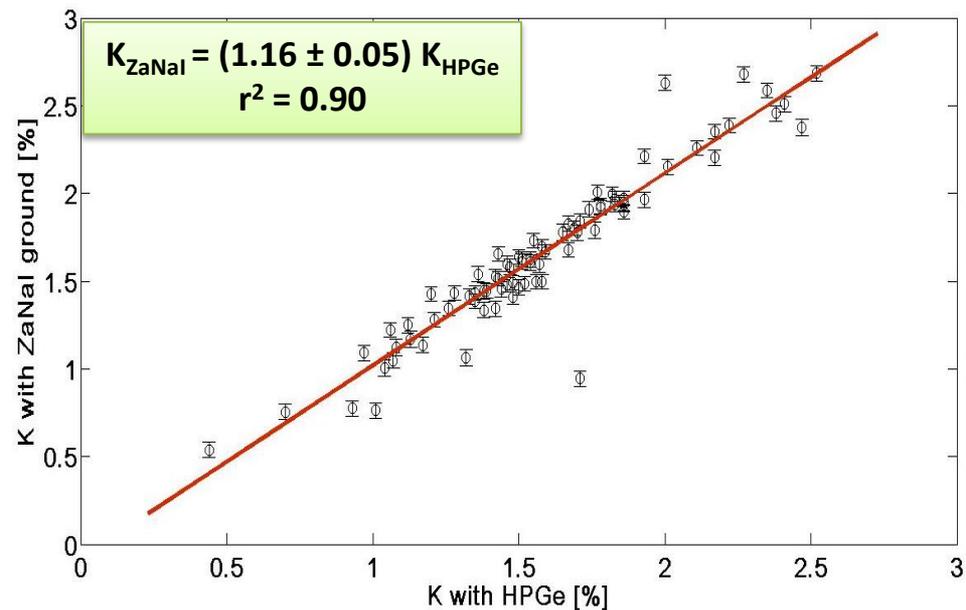
	ID_GPS	Temp (°C)	Hum (%)
▶ +	GPS_1200	40,96	35,8
▶ +	GPS_1205	31,01	48,58
▶ +	GPS_1210	37,27	34,52
▶ +	GPS_1215	39,1	51,84
▶ +	GPS_1220	43,23	34,43
▶ +	GPS_1225	43,44	26,46
▶ +	GPS_1230	28,3	48,53
▶ +	GPS_1235	42,47	24,7
▶ +	GPS_1240	26,37	54,95
▶ +	GPS_1245	24,94	60,38
▶ +	GPS_1250	29,66	54,5
▶ +	GPS_1255	28,48	56,77
▶ +	GPS_1260	36,05	26,95
▶ +	GPS_1265	43,51	21,42
▶ +	GPS_1270	39,23	21,68

## Pedological parameters to define in the campaign:

- litology
- granulometry
- rockness
- soil\_use
- PH of soil
- colours
- water content

	ID_Soil	ID_GPS	Soil_Colour	Speckled	Weaving	Lithology	Soil_Use	PH	Depth_Max_(cm)
2	Soil_1200	GPS_1200	3	1	12	SEDIMENTI MARINI	110	8	10
3	Soil_1201	GPS_1201	3	1	12	SEDIMENTI MARINI	110	8	10
4	Soil_1202	GPS_1202	3	1	12	SEDIMENTI MARINI	110	8	10
5	Soil_1203	GPS_1203	3	1	12	SEDIMENTI MARINI	110	8	10
6	Soil_1204	GPS_1204	3	1	12	SEDIMENTI MARINI	110	8	10
7	Soil_1205	GPS_1205	3	1	15	SEDIMENTI MARINI	200	8	10
8	Soil_1206	GPS_1206	3	1	15	SEDIMENTI MARINI	200	8	10

# Correlation between in-situ acquisition on ground and laboratory measurements

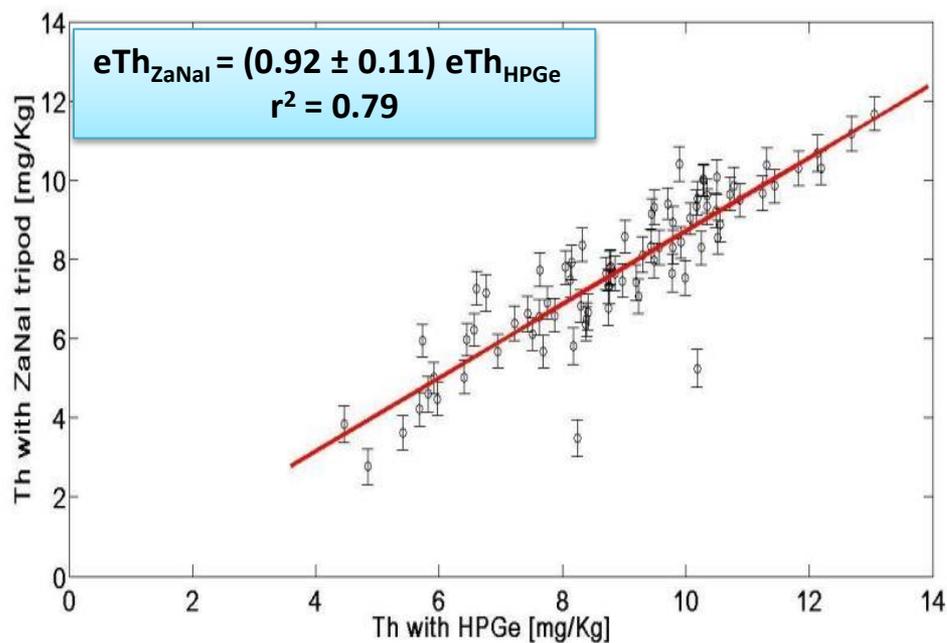
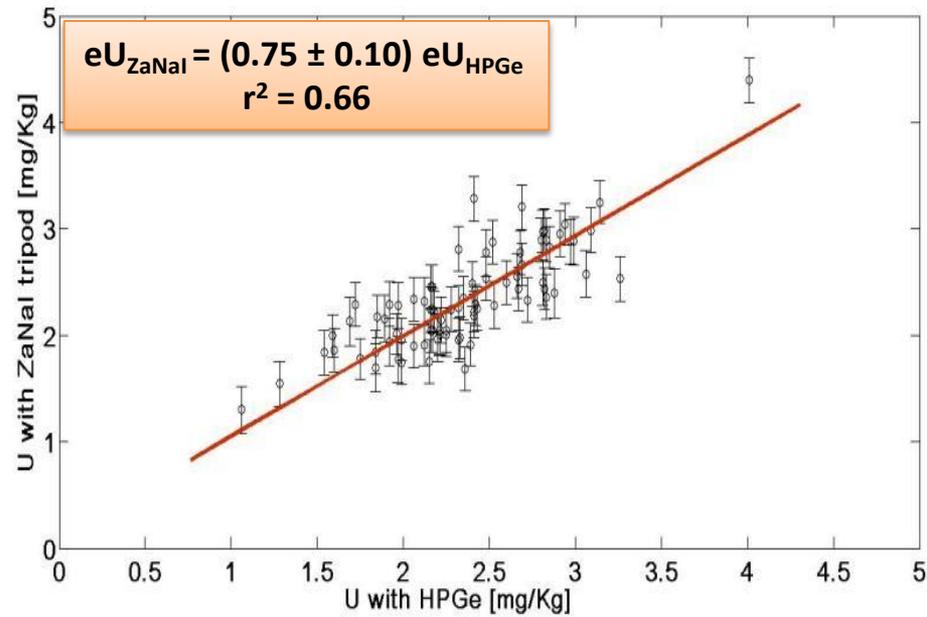
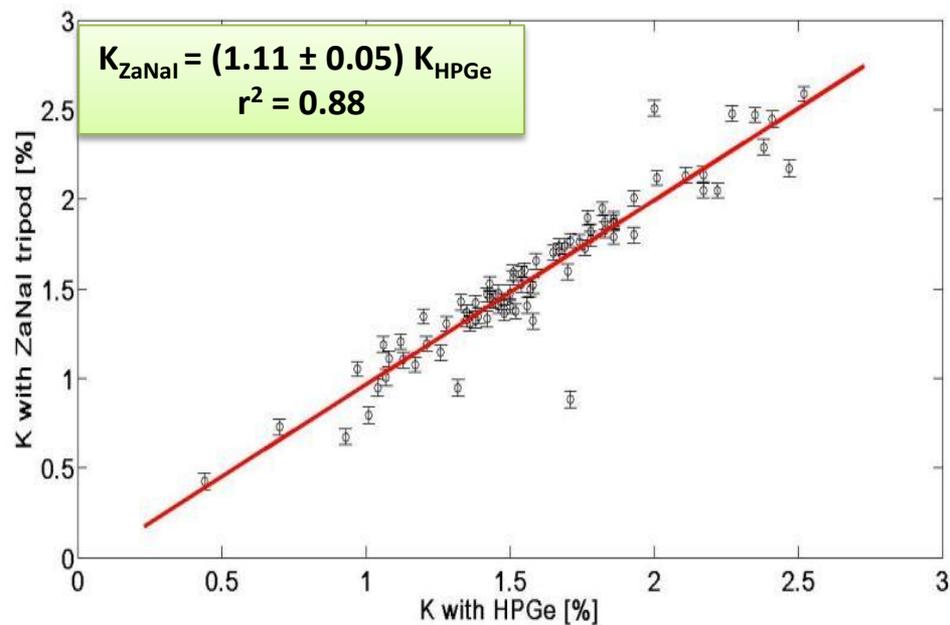


# The correlation parameters obtained for in-situ measurements on ground and laboratory measurements.

Isotopes	$a \pm \sigma_a$	$R^2$
K [%]	$1.16 \pm 0.05$	0.90
U [mg/Kg]	$0.85 \pm 0.11$	0.64
Th [mg/Kg]	$0.97 \pm 0.12$	0.80

- A good correlation between in-situ and laboratory measurements.
- The linear regression coefficient  $r^2$  obtained for K and Th is very close to unity, while for U the data are more dispersed due to the effect of atmospheric radon.
- For Th the data are comparable within  $1\sigma$ , while for U within  $1.5\sigma$  and for K for more than  $3\sigma$ .
- The final relative uncertainties for K, U and Th are less than about 20%, respectively 13%, 19% and 12%.

# Correlation between in-situ acquisition on tripod and laboratory measurements

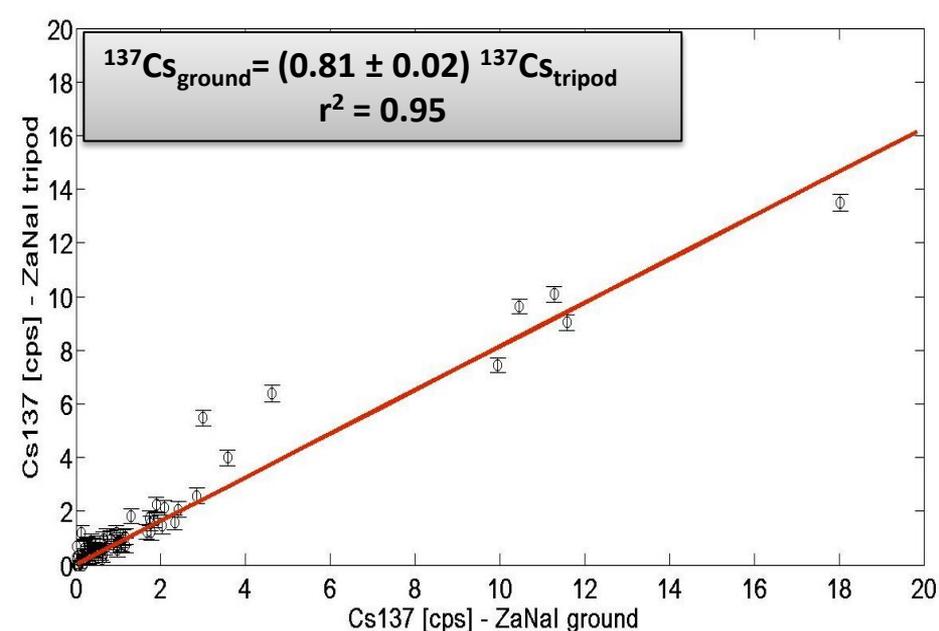
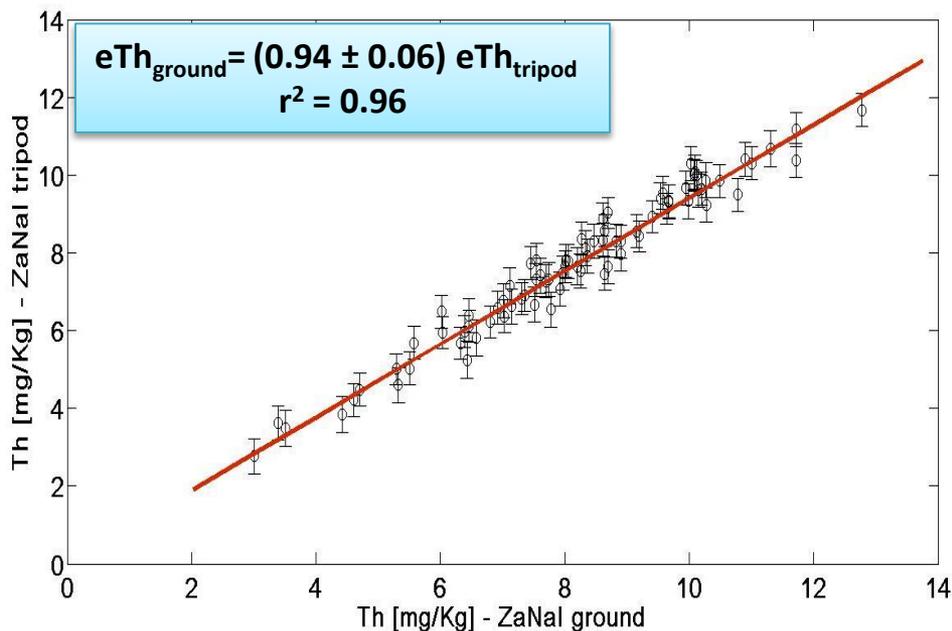
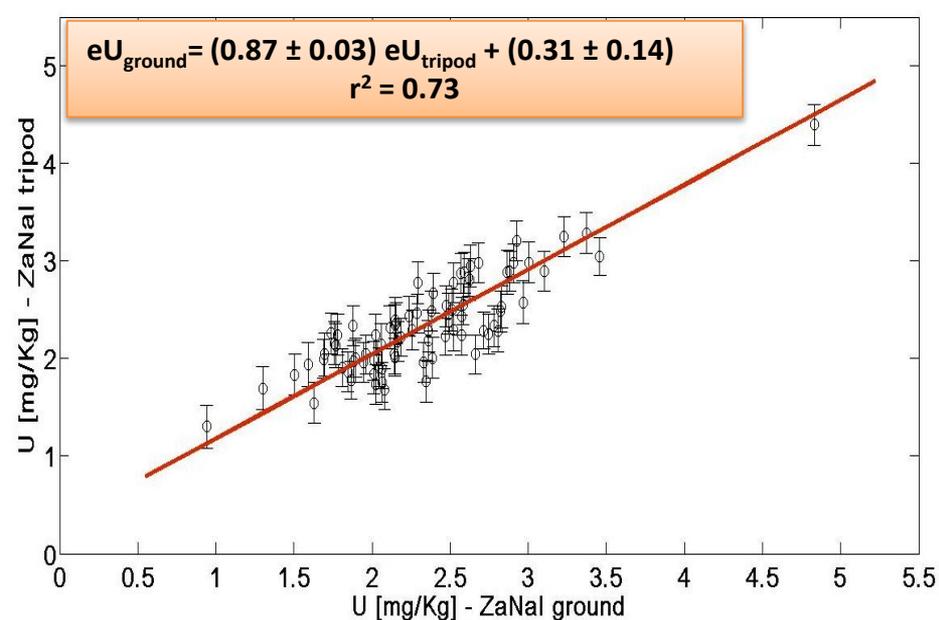
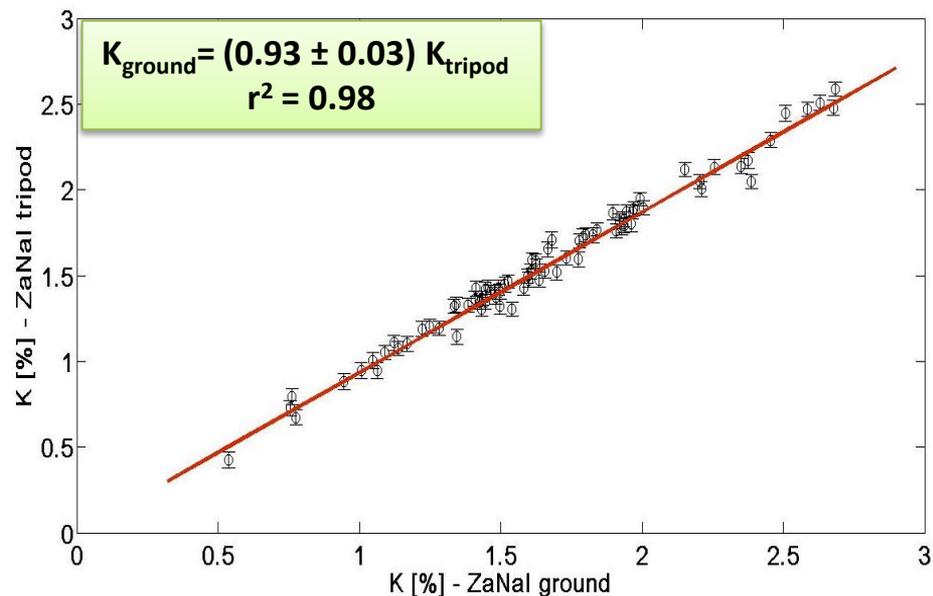


# The correlation parameters between measurements in-situ acquisition on tripod and in the laboratory.

Isotopes	$a \pm \sigma_a$	$R^2$
K [%]	$1.11 \pm 0.05$	0.88
U [mg/Kg]	$0.75 \pm 0.10$	0.66
Th [mg/Kg]	$0.92 \pm 0.11$	0.79

- Good correlation between in-situ and laboratory measurements.
- The linear regression coefficient shows similar results as those obtained for in-situ measurements placing the detector on ground. For Th the data are comparable within  $1\sigma$ , while for U within  $2.5\sigma$  and for K for more than  $2\sigma$ .
- The final relative uncertainties for K, U and Th are less than about 35%, respectively 10%, 33% and 12%.
- The increase of discrepancy between the two data sets can be attributed to the attenuation of 1m air for in-situ measurement performed by placing the detector on tripod.
- The attenuation due to 1 m air can be calculated as the difference between ground and tripod in-situ measurements compared with laboratory measurements, and are  $5 \pm 0.3 \%$ ,  $10 \pm 1.9 \%$  and  $5 \pm 0.9 \%$  respectively for K, U and Th.

# Correlation between in-situ acquisition on ground and on tripod

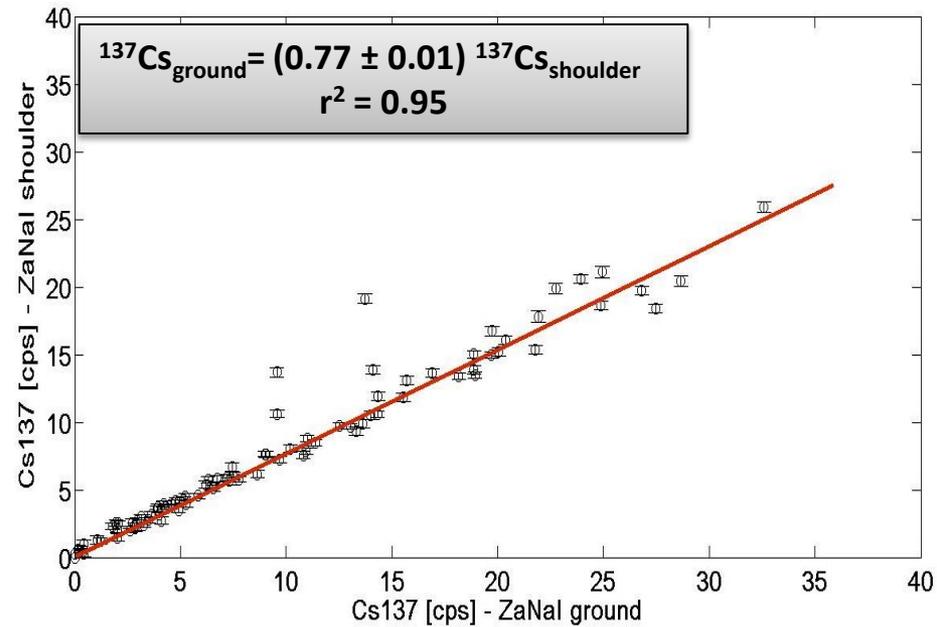
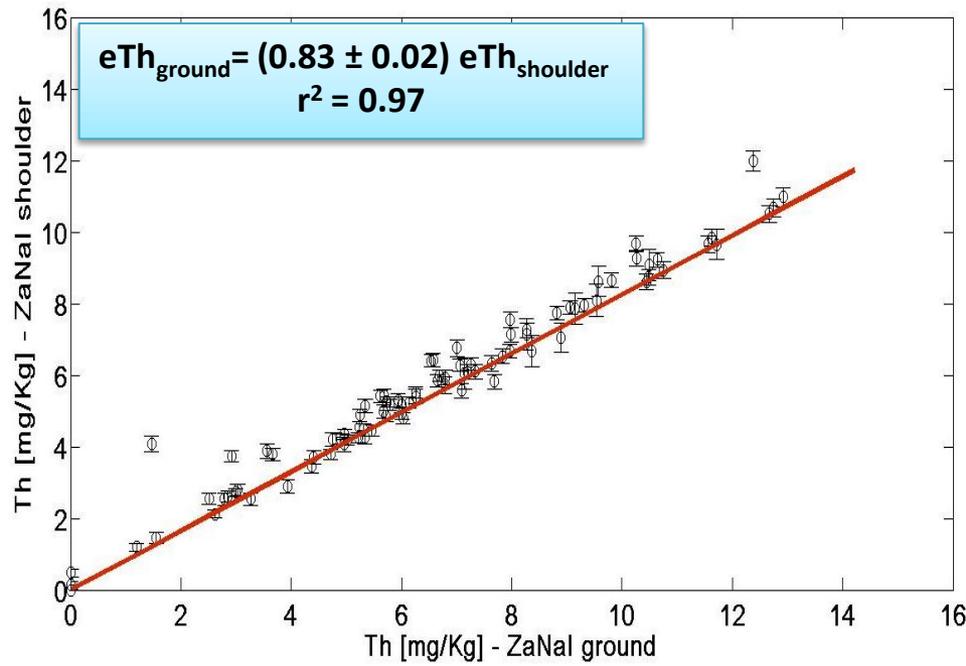
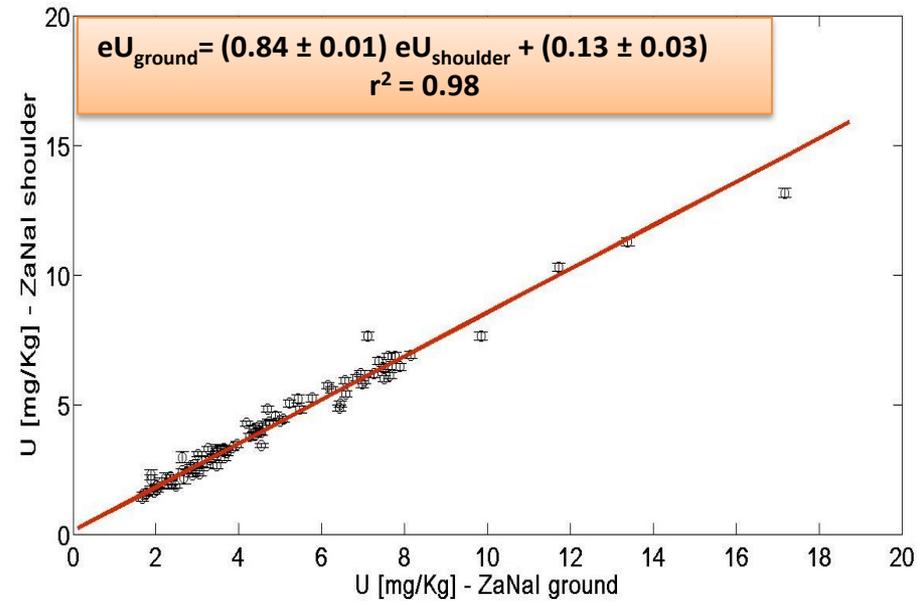
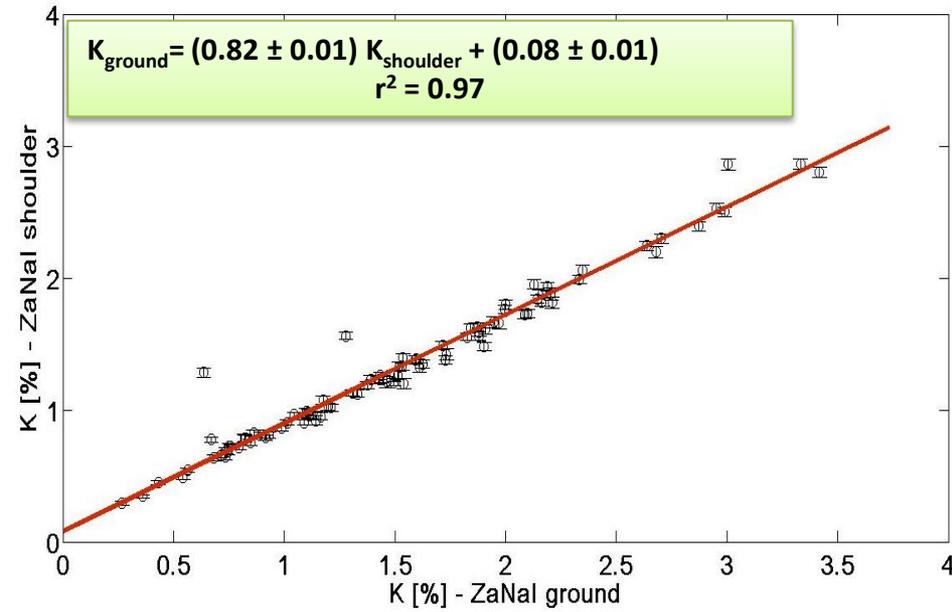


## Correlation parameters between in-situ measurements on ground and on tripod

Isotopes	$a \pm \sigma_a$	$b \pm \sigma_b$	$r^2$
K [%]	$0.93 \pm 0.03$	-	0.98
U [mg/Kg]	$0.87 \pm 0.06$	$0.31 \pm 0.14$	0.73
Th [mg/Kg]	$0.94 \pm 0.06$	-	0.96
$^{137}\text{Cs}$ [cps]	$0.81 \pm 0.02$	-	0.95

- There is a very good correlation between in-situ measurements on ground and on tripod. Linear regression coefficient close to unity are an evidence of the homogeneity of the selected sites.
- The deviation between the angular coefficients and the unity value quantifies the correction of the signal due to the attenuation effect of 1 m air, obtaining for  $^{40}\text{K}$ ,  $^{238}\text{U}$ ,  $^{232}\text{Th}$  and  $^{137}\text{Cs}$  respectively  $7 \pm 0.3\%$ ,  $13 \pm 0.9\%$ ,  $6 \pm 0.4\%$  and  $19 \pm 0.5\%$ .
- For  $^{137}\text{Cs}$  the attenuation is higher due to the fact that it emits a gamma ray with relative lower energy (662 keV).

# Correlation between in-situ acquisition on ground and on operator shoulder

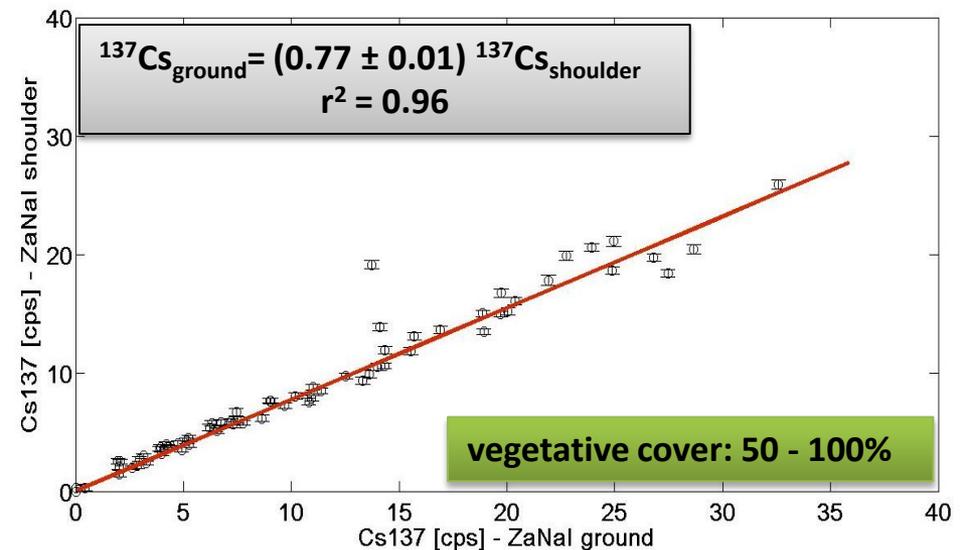
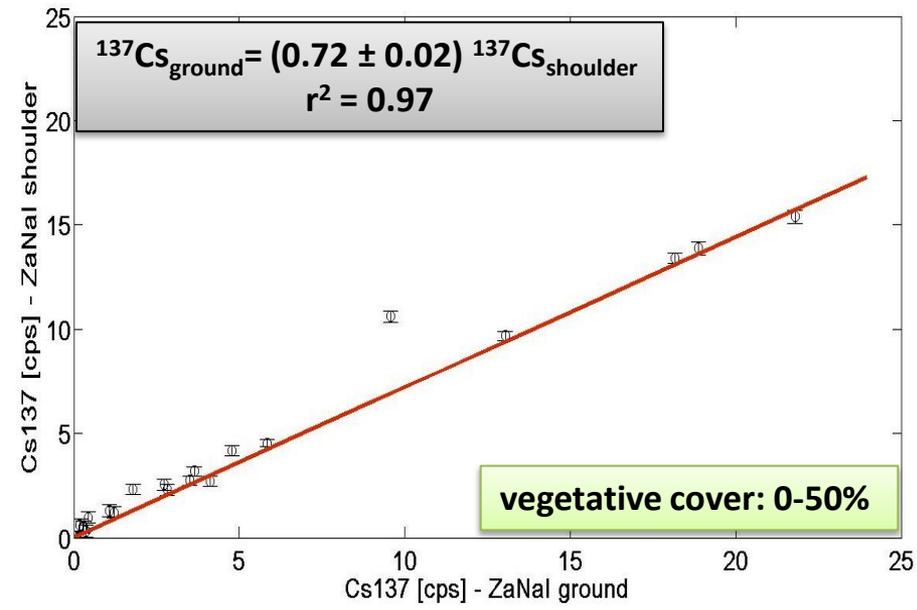
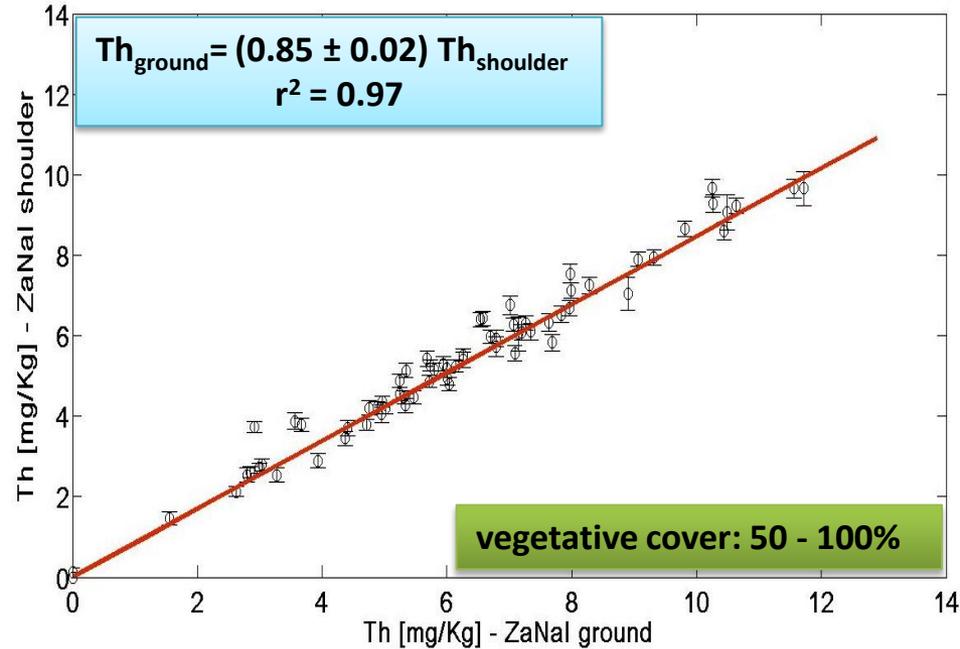
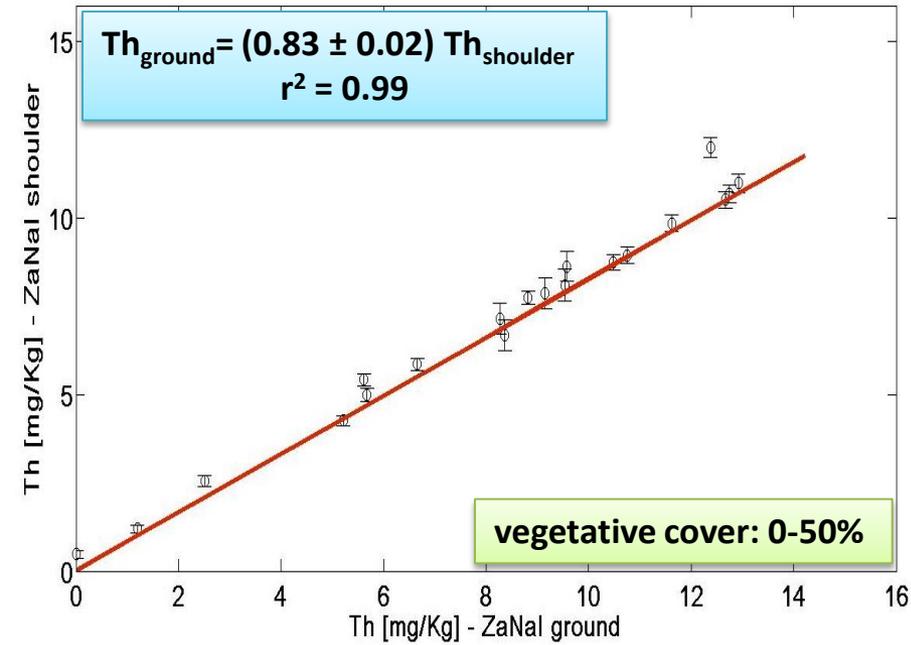


# Correlation parameters between in-situ measurements on ground and on shoulder

Isotopes	$a \pm \sigma_a$	$b \pm \sigma_b$	$r^2$
K [%]	$0.82 \pm 0.01$	$0.08 \pm 0.01$	0.97
U [mg/Kg]	$0.84 \pm 0.01$	$0.13 \pm 0.03$	0.98
Th [mg/Kg]	$0.83 \pm 0.02$	-	0.97
$^{137}\text{Cs}$ [cps]	$0.77 \pm 0.01$	-	0.95

- A very good correlation between in-situ measurements on ground and on shoulder.
- The deviation between the angular coefficients and the unity value quantifies the correction of the signal due to the presence of an operator, obtaining for  $^{40}\text{K}$ ,  $^{238}\text{U}$ ,  $^{232}\text{Th}$  and  $^{137}\text{Cs}$  respectively  $18 \pm 0.2\%$ ,  $16 \pm 0.2 \%$ ,  $17 \pm 0.4\%$  and  $23 \pm 0.3\%$ .

# Interference of vegetative cover for-situ acquisition on ground and on operator shoulder



# Correlation parameters between in-situ measurements on ground and on shoulder for two classes of vegetative coverage

Isotopes	$a \pm \sigma_a$	
	Vegetative coverage 0-50 %	Vegetative coverage 50-100 %
Th [mg/kg]	$0.83 \pm 0.02$	$0.85 \pm 0.02$
$^{137}\text{Cs}$ [cps]	$0.72 \pm 0.02$	$0.77 \pm 0.01$

- In the case of  $^{232}\text{Th}$  it is observed a minor degree of influence due to the vegetative cover from 50-100%, but comparable within  $1\sigma$  with the case of 0-50% of vegetative coverage.
- In the case of  $^{137}\text{Cs}$  it is seen clearly within the  $1\sigma$  the influence due to the presence of the vegetative cover.
- As it is expected, the presence of vegetative cover is more visible in the case of relatively lower energies.

# Conclusions

- Realization of extensive measurements (80 sites) investigated both in-situ using ZaNaI\_1.0L (FSA-NNLS method) and in laboratory using MCA\_Rad showing a very good correlation between them.

Isotope	$[\text{ZaNaI}]_{\text{ground}} = (a \pm \sigma_a)$ [HPGe]	$[\text{ZaNaI}]_{\text{tripod}} = (a \pm \sigma_a)$ [HPGe]
$^{40}\text{K}$ (%)	$1.16 \pm 0.05$	$1.11 \pm 0.05$
eTh (mg/kg)	$0.85 \pm 0.11$	$0.75 \pm 0.10$
eU (mg/kg)	$0.97 \pm 0.12$	$0.92 \pm 0.11$

- The final relative uncertainties for K, U and Th are found to be less than about 20% for ZaNaI\_1.0L on ground versus HPGe measurements and about 35 % ZaNaI\_1.0L on tripod versus HPGe measurements.
- In the case of  $^{238}\text{U}$ , correction is much more complex during the measurement in situ because the presence of Radon in air distorts our signal.

# Conclusions

- By using a **ZaNaI\_1.0L** detector in situ measurements it is evaluated experimentally the corrections between different configurations (on the ground, at 1m height and on the shoulders)

Isotopes	Max. Energy [keV]	Correction at 1 m height [%]	Air + operator attenuation correction [%]
<b><sup>40</sup>K [%]</b>	<b>1460</b>	<b>7 ± 0.3</b>	<b>18 ± 0.2</b>
<b>eTh [mg/kg]</b>	<b>2615</b>	<b>6 ± 0.4</b>	<b>17 ± 0.4</b>
<b>eU [mg/kg]</b>	<b>1764</b>	<b>13 ± 0.9</b>	<b>16 ± 0.2</b>
<b><sup>137</sup>Cs [cps]</b>	<b>662</b>	<b>19 ± 0.5</b>	<b>23 ± 0.3</b>

- As expected from theoretical models, the corrections for different configurations are lower for gamma rays with high energy.
- In the obtained concentrations of radioactive nuclides are studied several parameters as environmental conditions, operational circumstances and vegetative cover for their interference. In several parameters that are taken into account it is seen a light influence of them, but inside the errors 1 sigma we can give a clear result only for the influence of vegetative cover in the case of **<sup>137</sup>Cs**.

## Peer-reviewed scientific papers

1. Xhixha G. et al (2013). *First Characterization Of Natural Radioactivity In Building Materials Manufactured In Albania*. Journal of Radiation Protection Dosimetry. doi: 10.1093/rpd/ncs334.
2. Xhixha G. et al. (2012). *Fully automated gamma-ray spectrometer for NORM characterization*. Journal of Radioanalytical and Nuclear Chemistry, 1-13. doi: 10.1007/s10967-012-1791-1.
3. Caciolli A. et al. (2012). *A new FSA approach for in situ  $\gamma$ -ray spectroscopy*. Science of the Total Environment 414 (2012) 639–645.
4. Cfarku F. et al. (2011). *Radioactivity Monitoring in Drinking Water of Albania*. J. Int, Environmental Protection & Ecology, ISSN 1311-5065, Vol. 12, Nr. 3 - p.1116.
5. Bode K. et al. (2010). *Results Of The National Survey On Radon Indoors In Albania*. doi: 10.1063/1.3322533, ISSN 0094-243, ISBN 978- 0-7354-0740-4. American Institute of Physics.

## Conference proceedings and papers not peer-reviewed

1. 1. Mou L. et al. (2011). *Nuovo spettrometro gamma per il monitoraggio della radioattività in situ*. Mus. Civ. Rovereto, Atti del Workshop in geofisica, 59-72.
2. Bezzon G.P. et al. (2011). *Mapping of natural radioelements using gamma-ray spectrometry: Tuscany Region case of study*. ISSN 1828-8545, INFN-LNL Rep. 234.
3. Bezzon G.P. et al. (2011). *A  $\gamma$ -Spectroscopy System for Atmospheric Radon Detection*. ISSN 1828-8545, INFN-LNL Rep. 234.
4. 4. Bezzon G.P. et al. (2010). *Preliminary results for the characterization of the radiological levels of rocks in Tuscany Region*. Atti 85° Congr. Soc. Geol. It., vol. 11, 513-514.
5. Cfarku F. et al. (2009). *Determination of alpha and total beta radiation in water by the GPC method (gas proportional counters)*. Bulletin of Natural Science No. 7, 83-88.



Thank You





## Theoretical models

The number of photons detected per second in the thorium window is given by<sup>1</sup>:

$$N = \varphi A \varepsilon$$

where:

$\varphi$  - flux of 2.62 MeV photons at the detector

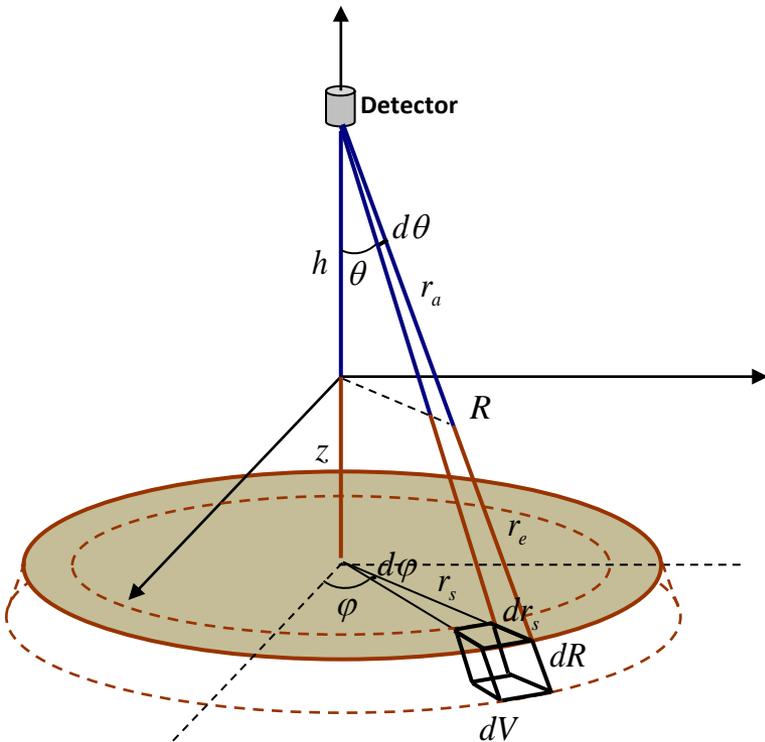
$A$  - cross-section area of the detector

$\varepsilon$  - photopeak efficiency

$$N = \frac{A \varepsilon n}{2\lambda} \int_1^\infty \frac{e^{-\mu h \sec \theta} d(\sec \theta)}{(\sec \theta)^2} = N_0 E_2(\mu h)$$

$\mu$  and  $\lambda$  - linear absorption coefficients for air and soil

$N_0$  - thorium count rate at ground level



The theoretical models depend on the calculation of exponential integral of second kind:

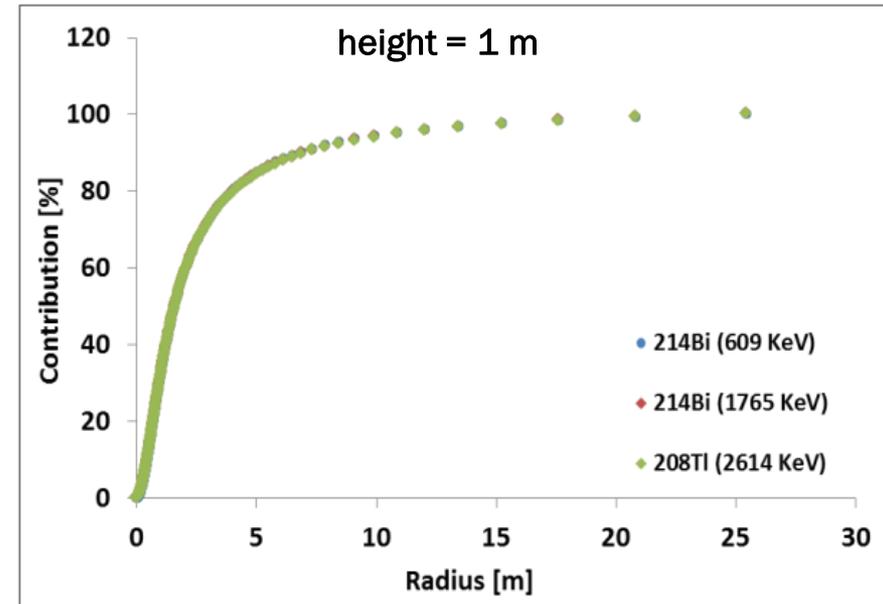
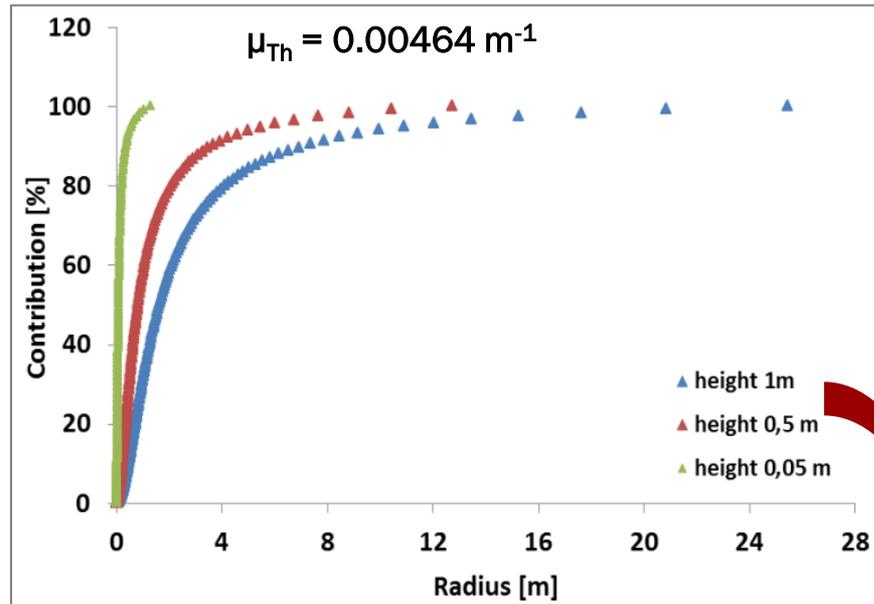
$$E_2(\mu h) = \int_1^\infty \frac{e^{-\mu h t}}{t^2} dt$$

<sup>1</sup> R. L. Grasty., 1975 Atmospheric Absorption of 2.62 MeV Gamma ray Photons emitted from the ground. Geophysics vol 40, 1058-1065.

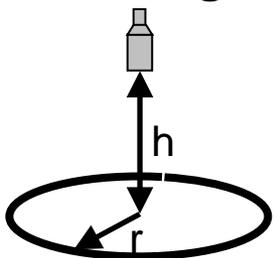
# Variation in response of a spherical detector versus heights and energies

The number of photons  $N$  detected above a uniformly radioactive infinite source per unit time is:

$$N = \frac{n}{2\lambda} \int_1^{\sec\theta} \frac{A\varepsilon e^{-\mu h \sec\theta}}{\sec^2\theta} d(\sec\theta)$$



At height  $h$ , the detector receive 90% of the signal from a circle of radius  $R$

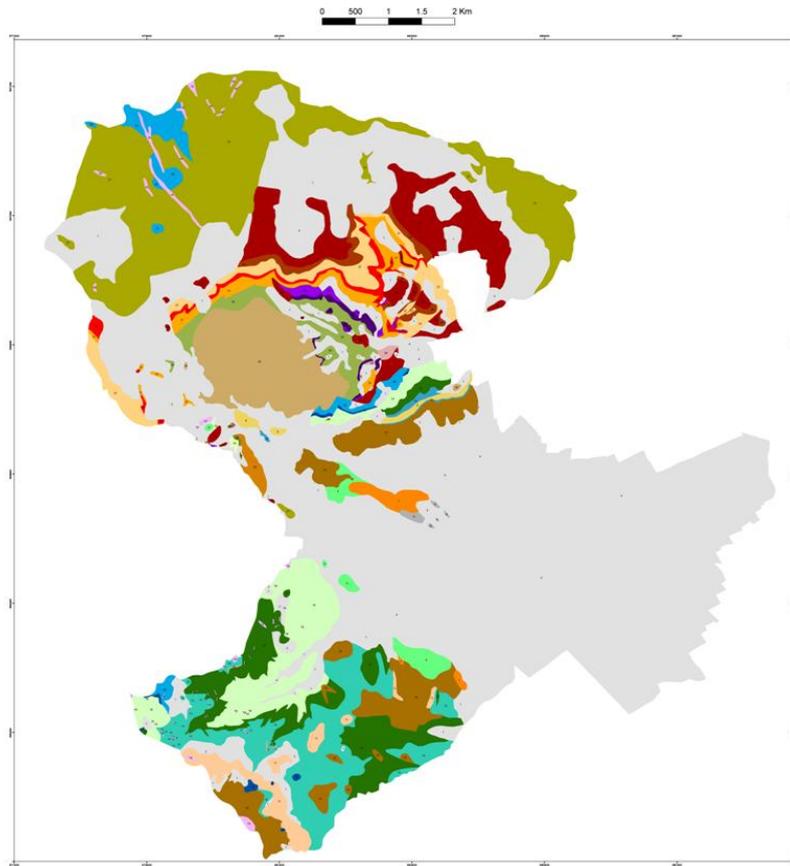


$h$ (m)	0.05	0.5	1.0
$R$ (m)	0.37	3.7	7.35

	Energy (keV)	$\mu$ _Linear absorption coeff ( $\text{m}^{-1}$ )-air
$^{214}\text{Bi}$	609	0.00990
	1764	0.00558
$^{208}\text{Tl}$	2614	0.00464

# Campaign activity

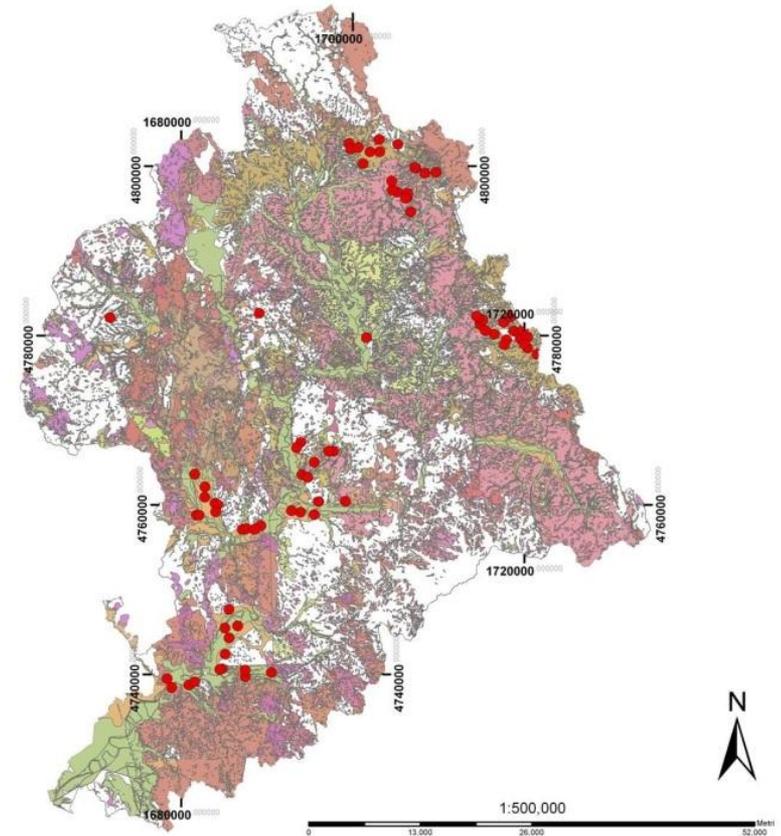
## Geological map of the Commune of Schio



### LEGENDA

Depositi quaternari	21 Dolomia principale (Triassico)
6 Molasse (Miocene)	23 Latti, latandesiti e latibasalti (Triassico)
7 Arenarie di S. Urbano (Miocene)	24 Rioliti e daciti (M. Guizza-Fasolo) (Triassico)
8 Calcicare di Lonetto (Oligocene)	25 Rioliti, riolaciti, daciti, andesiti basaltiche di colata (Triassico)
9 Calcareniti di Castelgomberto (Oligocene)	26 Formazione a Nodosus (Triassico)
10 Mame di Priabona (Eocene)	27 Calcicare di Monte Spitz (Triassico)
11 Calcari nummulitici (Eocene)	28 Calcicare di Monte Spitz (Calcicare a Sturia) (Triassico)
12 Breccie di esplosione (Eocene)	29 Conglomerato del Tretto (Triassico)
13 Ialoclastiti (Eocene)	30 Calcicare di Recoaro (Triassico)
14 Basalti alcalini e basaniti (camini vulcanici e filoni) (Eocene)	31 Formazione a Gracilis - Marni a Voltia (Triassico)
15 Basaniti e basalti alcalini di colata (Eocene)	32 Dolomia della Serla inferiore (Triassico)
16 Calcari di Spilecco (Paleocene)	33 Formazione di Werfen (Triassico)
17 Scaglia Rossa (Cretaceo)	34 Formazione a Bellerophon (Permico)
18 Biancone (Cretaceo)	35 Arenarie di Val Gardena (Permico)
19 Rosso Ammonitico (Giurassico)	36 Basamento cristallino sudalpino (Prepermico)
20 Calcari grigi di Noriglio (Giurassico)	

## Geological map of Ombrone Basin with the location of sampling points



### Legend

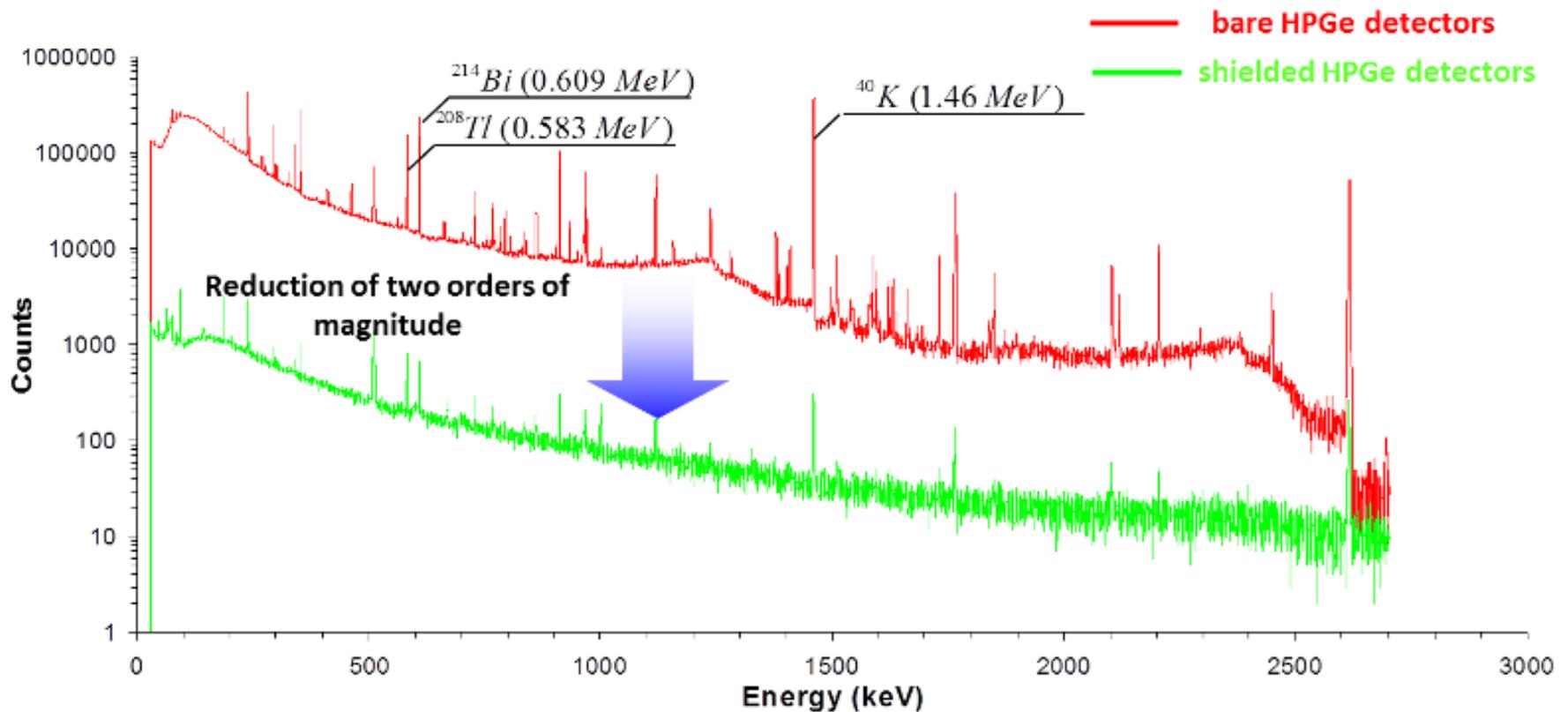
<b>Geology</b>	FIAa	MESa	SRC	a1	b2a
ACCb	FNE	MESb	SRCa	a1a	bnb
APA	FOS	MUL	TNI	a1q	h2
AVA	FOSo	OFI	VILa-b	a1s	h5
CCA	FRM	PLIb	VILe	aa	h5
FAA	GAMMA	PLIs	VINb	acb	ro
FAAd	MAC	SLEc	VINc	b	• Sampling points

ED50

# Background reduction of MCA\_Rad system

Estimation of Minimum Detectable Activity (MDA) for blank test [Curie 1986].

Isotope	E (keV)	MDA (Bq)
$^{40}\text{K}$	1460	0,26
$^{214}\text{Bi}$	609	0,04
$^{208}\text{Tl}$	583	0,06



# Efficiency analysis: three main corrections

1- **Geometrical correction ( $C_G$ ):** moving the standard point source in three positions (for three planes) It is calculated the  $C_G$  for different energies ( $E_i$ ) fitting the expression.

$$C_G = \sum_{i=0}^3 a_i (E_i / E_0)^i$$

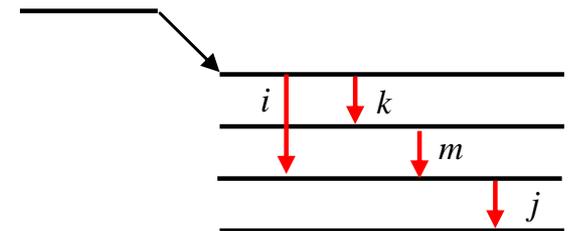
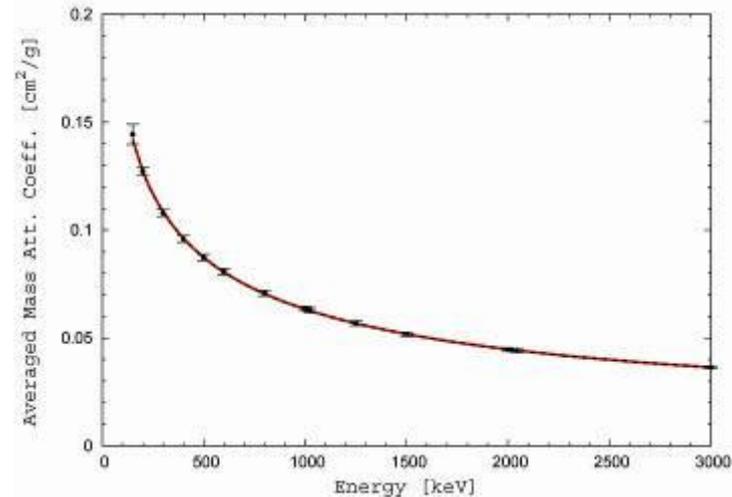
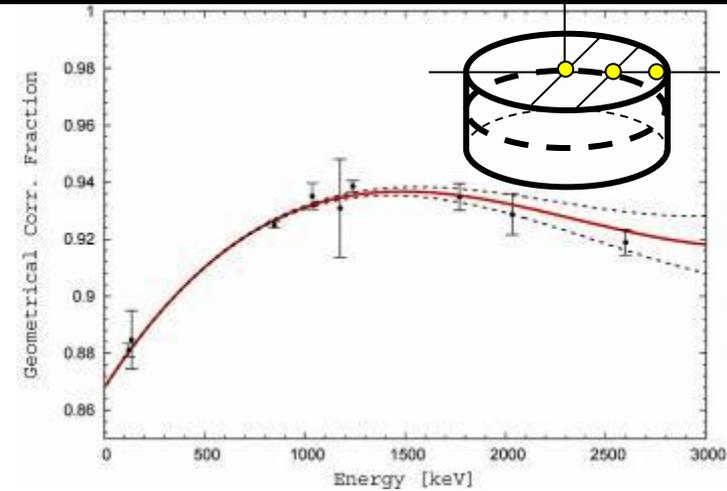
where  $E_0 = 1\text{keV}$ .

2- **Self absorption correction ( $C_{SA}$ ):** averaging the mass attenuation coeff.  $\mu$  for a “standard rock” with density  $\rho$ , It is calculated the  $C_{SA}$  for the sample thickness  $t = 4.5\text{ cm}$  using the simplified approach:

$$C_{SA} = \frac{1 - e^{-(\mu_s \rho_s - \mu_{ref} \rho_{ref})t}}{(\mu_s \rho_s - \mu_{ref} \rho_{ref})t}$$

3- **Coincidence summing correction ( $C_{CS}$ ):** the correction of (i) events takes into account the summing out (j) and summing in (k,m) and effects:

$$C_{CS(i)} = \left[ 1 - \frac{\sum_j P_{ij} P_i P_j \varepsilon_{ij}}{I_{\gamma i}} \right] \left[ 1 + \frac{\sum_{k,m} P_{tkm} P_k P_m \varepsilon_k^{app} \varepsilon_m^{app}}{I_{\gamma i} \varepsilon_i^{app}} \right]$$



# Absolute full-peak energy efficiency for MCA\_Rad system

