

Luminosity Determination at ANKE

- *via nuclear reactions*
 - *via energy loss measurements*
-
- Introduction
 - Formalism
 - Calibration
 - Luminosity determination
 - Conclusion

Introduction

Why Luminosity?

$$\frac{d\sigma}{d\Omega} = \frac{1}{L} \frac{N_{\text{exp}}}{A_{\text{det}} \epsilon_i}$$

you have to know!

- N_{exp} reconstructed number of events
- A_{det} detector acceptance
- ϵ_i efficiencies

- The Near-Threshold Production of ϕ Mesons in pp Collisions
M.Hartmann et al., PRL 96, 242301 (2006)
- Precision measurement of the quasi-free $pn \rightarrow d\phi$ reaction close to threshold
Y.Maeda et al., PRL 97, 142301 (2006)
- Precision study of the $\eta^3\text{He}$ system using $dp \rightarrow ^3\text{He}\eta$ reaction
T.Mersmann et al., Accepted by PRL
- Shape of the $\Lambda(1405)$ hyperon measured through its $\Sigma^0\pi^0$ decay.
I.Zychor et al., Submitted to PRL
- There are some more publications

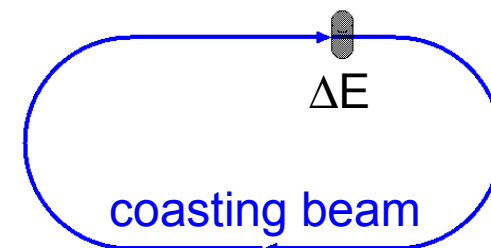
conventional

via nuclear reaction
(elastic \gg inelastic)

$$L = \frac{N'_{\text{exp}}}{A'_{\text{det}} \epsilon'_i (d\sigma/d\Omega)'}$$

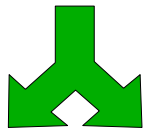
alternative

via energy loss measurement



Formalism

$$L = J_{beam} \cdot N_{target}$$



$$J_{beam} = \frac{I_{beam}}{q_{beam}}, [s^{-1}]$$

$$N_{target} = \frac{dT}{(dE/dx)m}, [cm^{-2}]$$

$$dT = \frac{\Delta T}{f_0 \Delta t}$$

$$\frac{\Delta T}{T_0} = \frac{1 + \gamma}{\gamma} \frac{\Delta p}{p_0}$$

$$\frac{\Delta p}{p_0} = \frac{1}{\eta} \frac{\Delta f}{f_0}$$

$$\eta = \frac{1}{\gamma^2} - \alpha$$

$$\frac{\Delta f}{f_0} = \alpha \frac{\Delta B}{B_0}$$

$$N_{target} = \frac{1 + \gamma}{\gamma} \frac{1}{\eta} \frac{1}{(dE/dx)m} \frac{T_0}{f_0^2} \frac{\Delta f}{\Delta t}$$

L - luminosity

J_{beam} - flux of beam [s^{-1}]

I_{beam} - COSY beam current [mA]

q_{beam} - electric charge of beam [C]

N_T - effective thickness of target [cm^{-2}]

dT - energy loss per single target traversal

dE/dx - stopping power of protons in hydrogen gas [NIST tables]

m - proton mass ($1.673 \times 10^{-24}g$)

f_0 - revolution frequency, measured

T_0 - beam kinetic energy

γ - Lorentz factor

p_0 - beam momentum

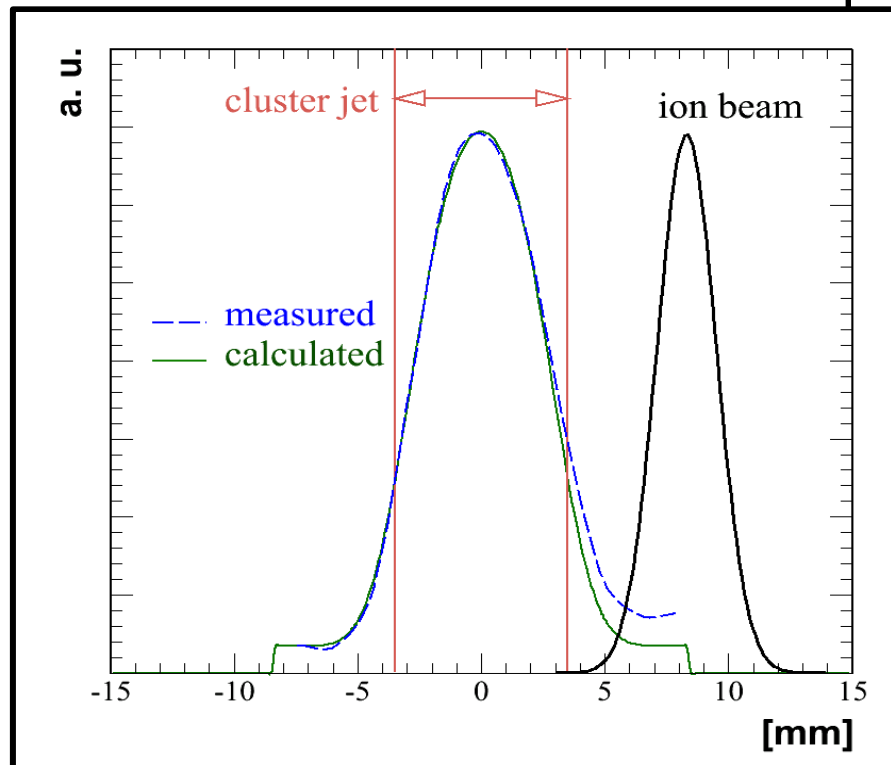
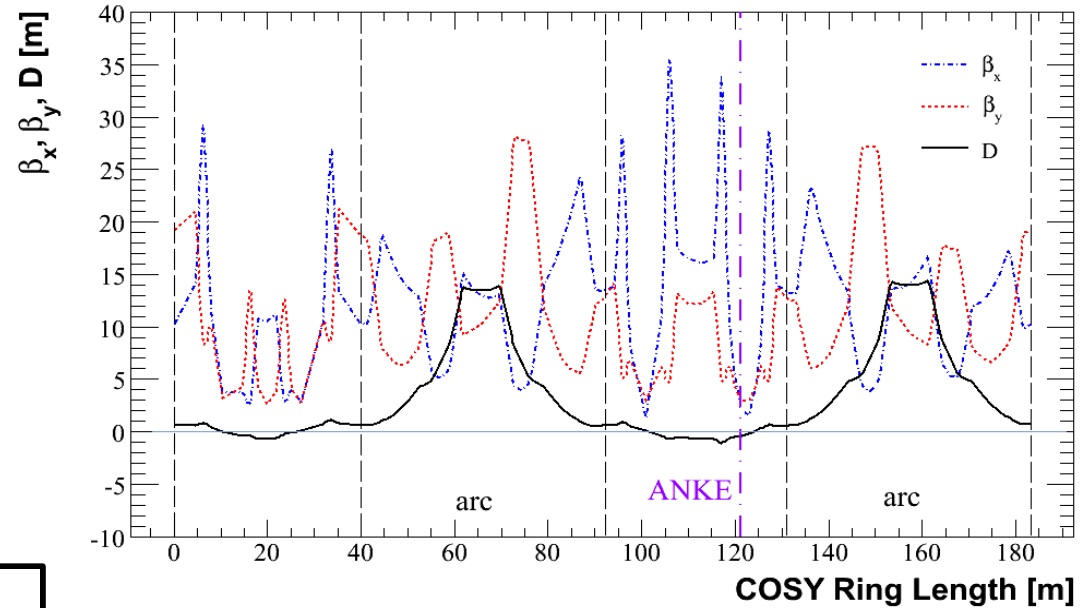
η - off-momentum factor based on measured α

B_0 - COSY dipole magnetic field

Beam target overlap

$T=2.65\text{GeV}$

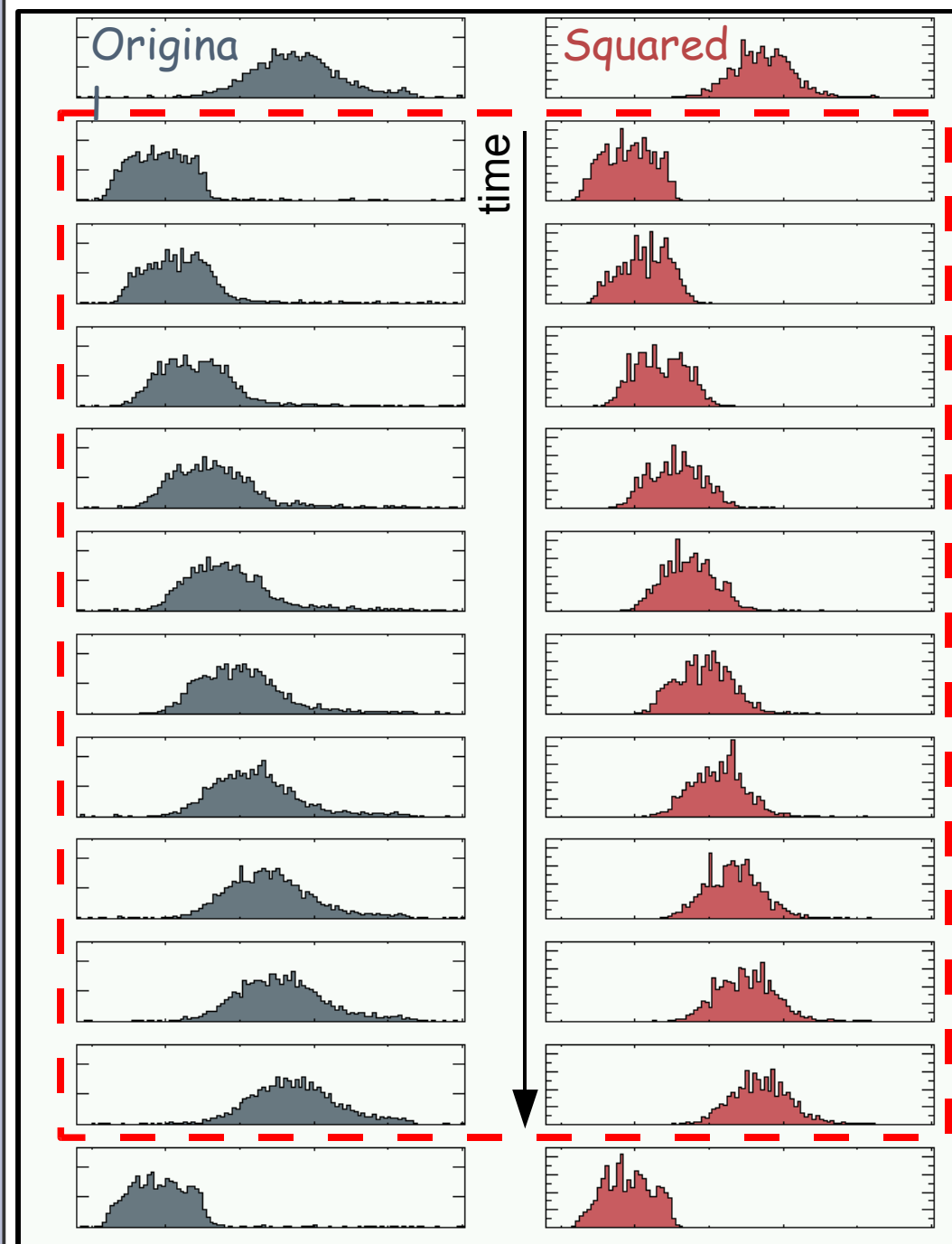
- estimated emittance growth in 10 minutes = $0.15\text{mm}\cdot\text{mrad}$
- possible beam position shift due to residual dispersion = 0.1mm



measurement of the beam target overlap

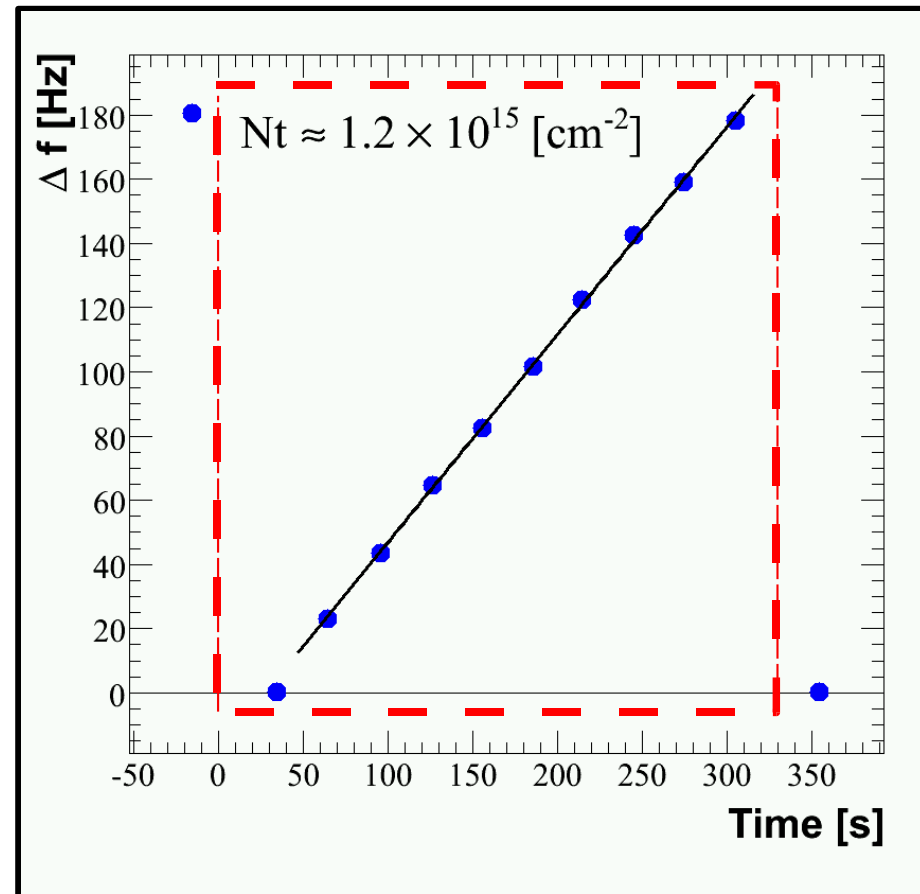
- beam foot width = 4.8mm (4σ)
- cluster jet diameter = 7mm

Raw Schottky Spectra's



Original - measured

Squared \sim momentum

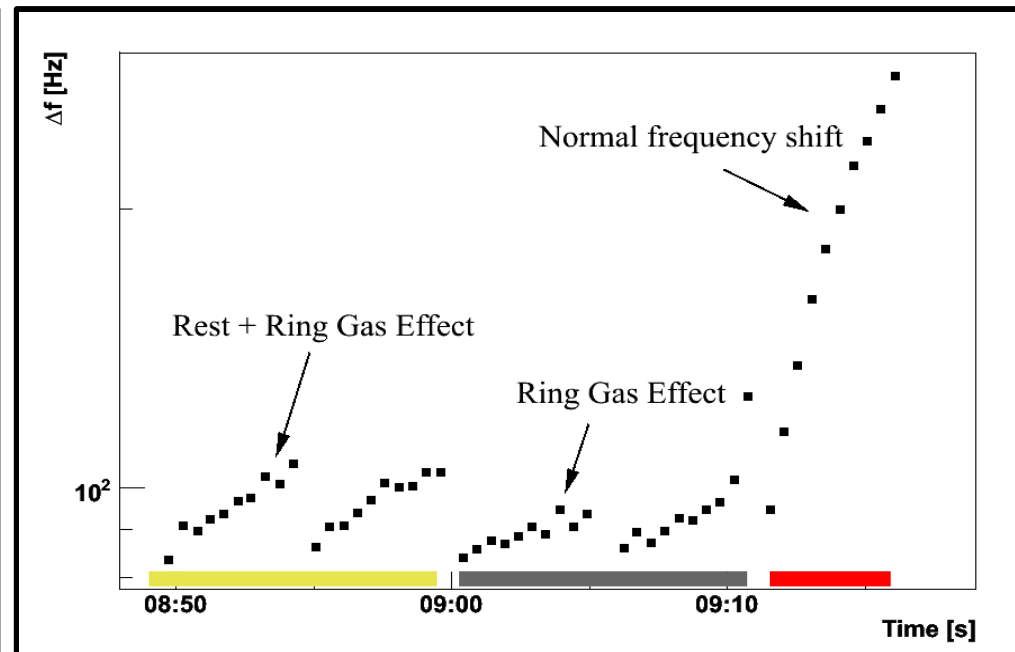
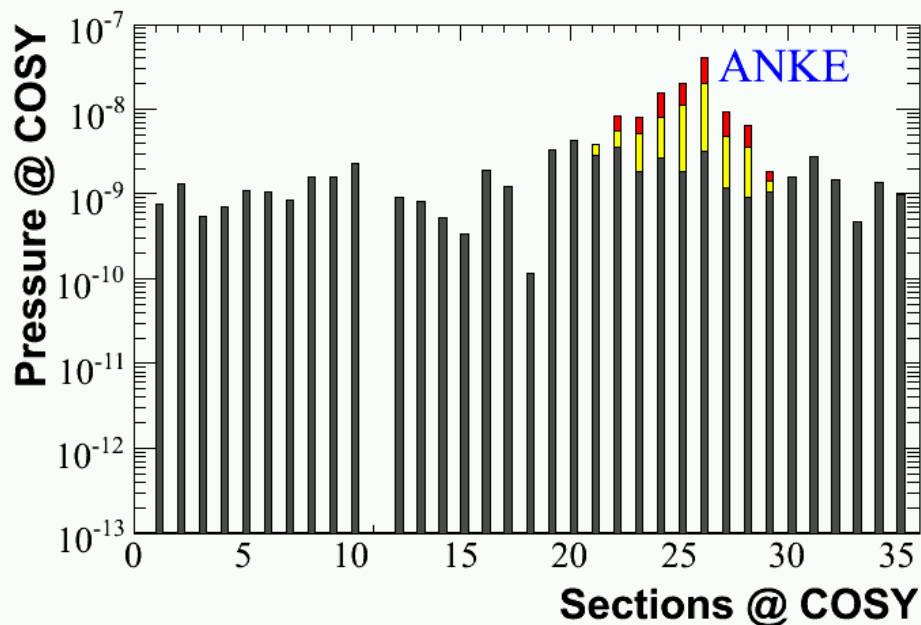


Residual gas effect

- 100% beam+target overlap (red)
- Rest+Ring Gas - target ON but ~0% overlap (yellow)
- Ring Gas - target OFF (black)

$$N_{target} = N_{total} - N_{Ring + Rest}$$

- 1) Total frequency shift = $1.35 \cdot 10^{15} \text{ [cm}^{-2}\text{]}$
- 2) Rest+Ring Gas = $1.32 \cdot 10^{14} \text{ [cm}^{-2}\text{]}$
- 3) Ring Gas = $5.31 \cdot 10^{13} \text{ [cm}^{-2}\text{]}$



α measurement at 2.65 GeV

$$\eta = \frac{1}{\gamma^2} - \alpha$$

η - off-momentum factor based on measured α

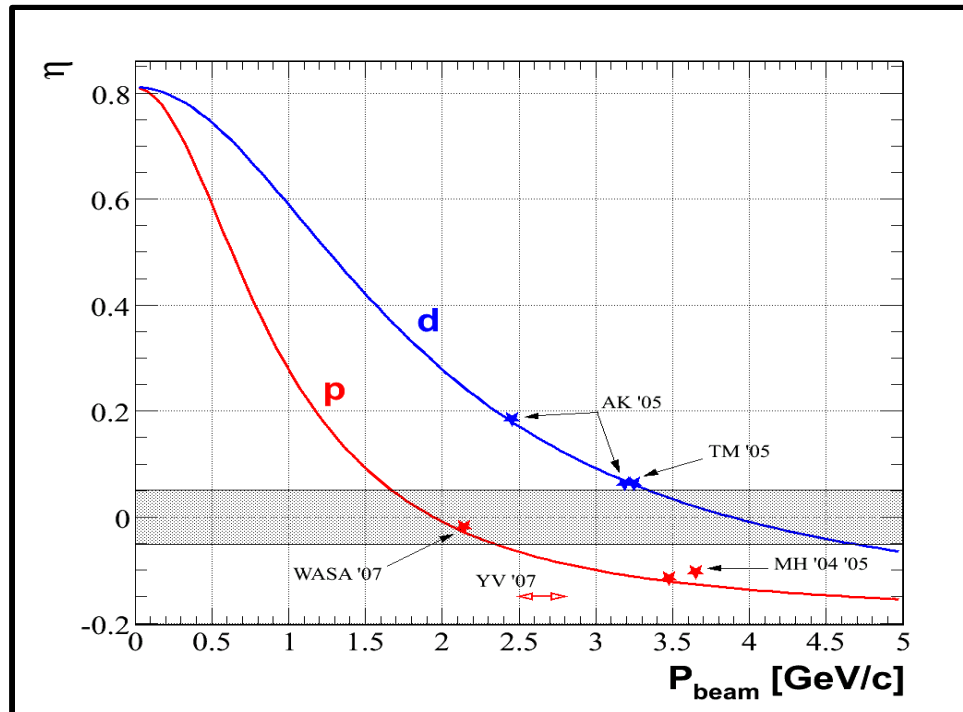
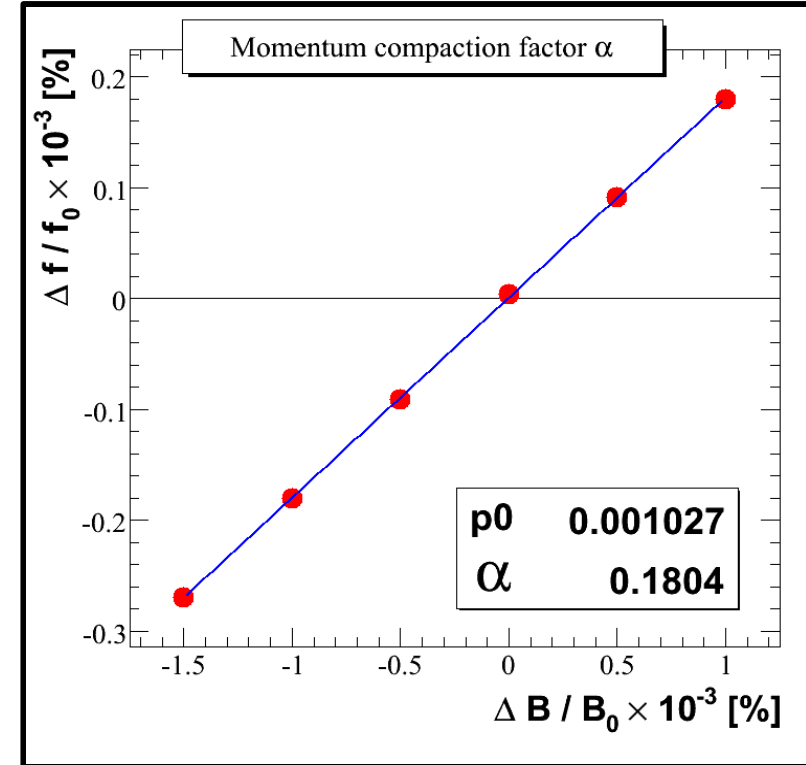
α - momentum compaction factor

f_0 - revolution frequency

γ - Lorentz factor

B_0 - COSY dipole magnetic field

$$\frac{\Delta f}{f_0} = \alpha \frac{\Delta B}{B_0}$$

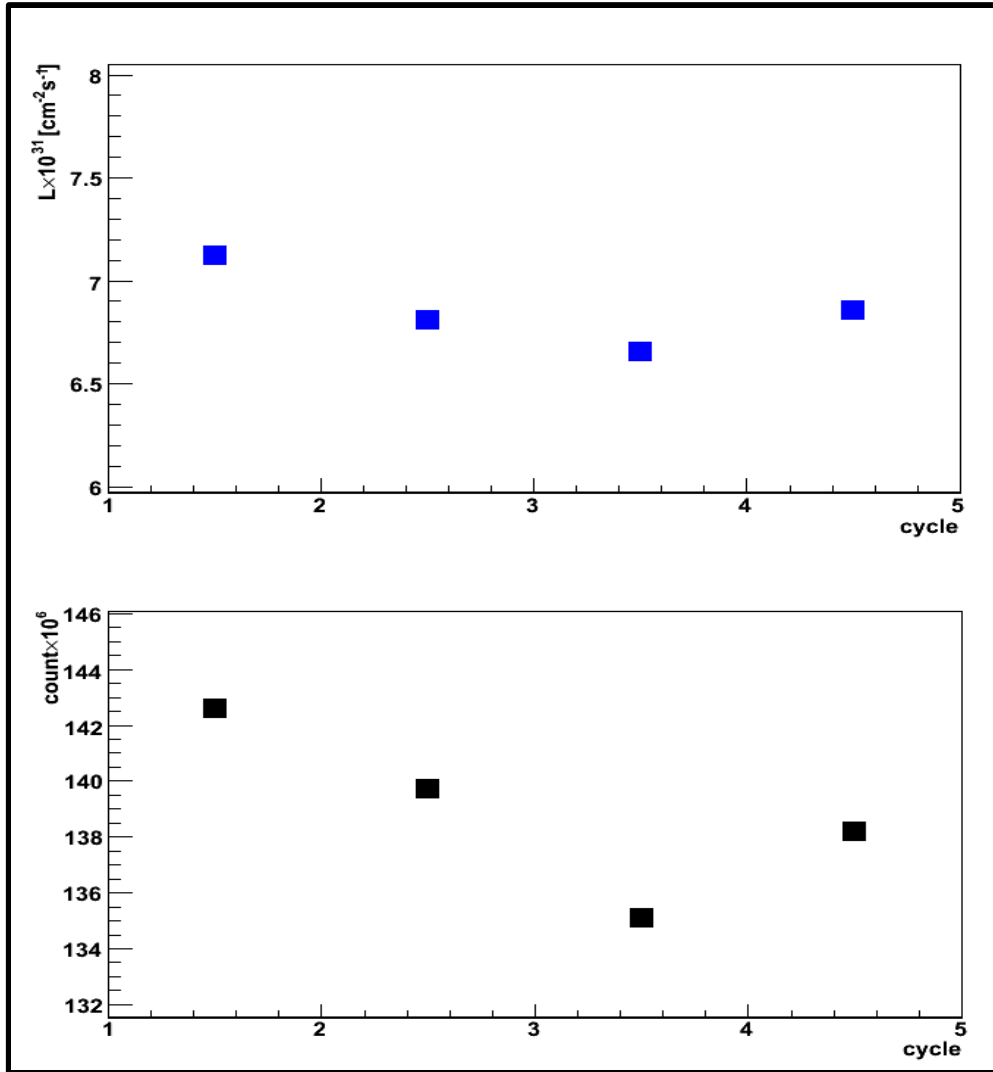
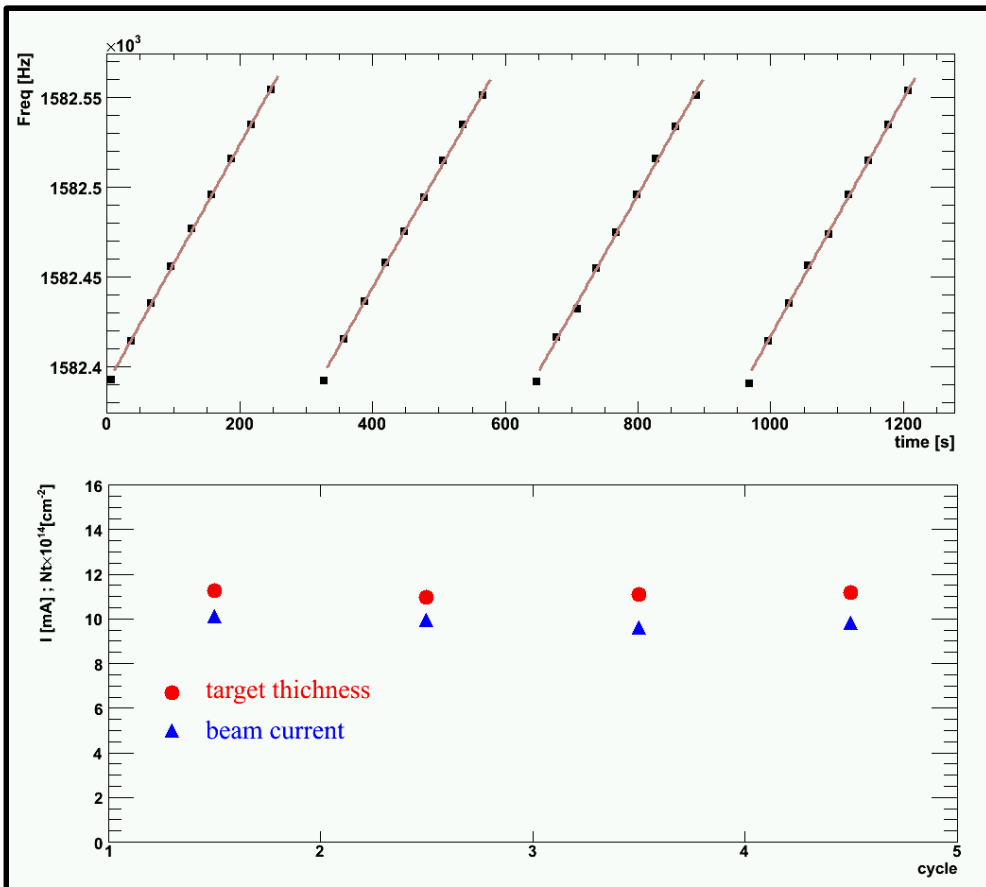


$$\eta = \frac{1}{\gamma^2} - \frac{1}{\gamma_{tr}^2}; \gamma_{tr} = 2.3$$

Luminosity determination

$$N_{target} = \frac{1+\gamma}{\gamma} \frac{1}{\eta} \frac{1}{(dE/dx)} \frac{T_0}{m f_0^2} \frac{\Delta f}{\Delta t}$$

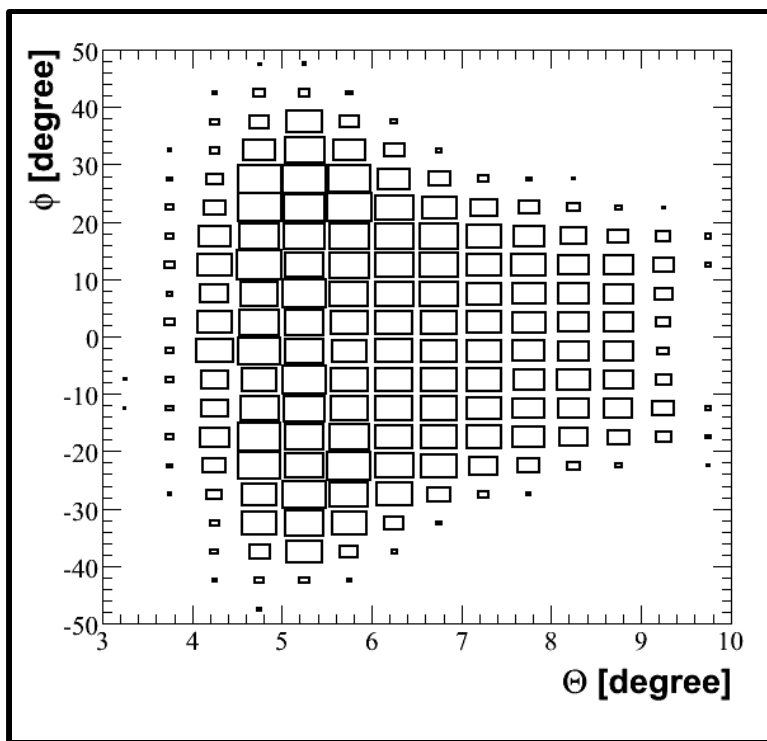
$\Delta f \approx 180 \text{ Hz / cycle}$



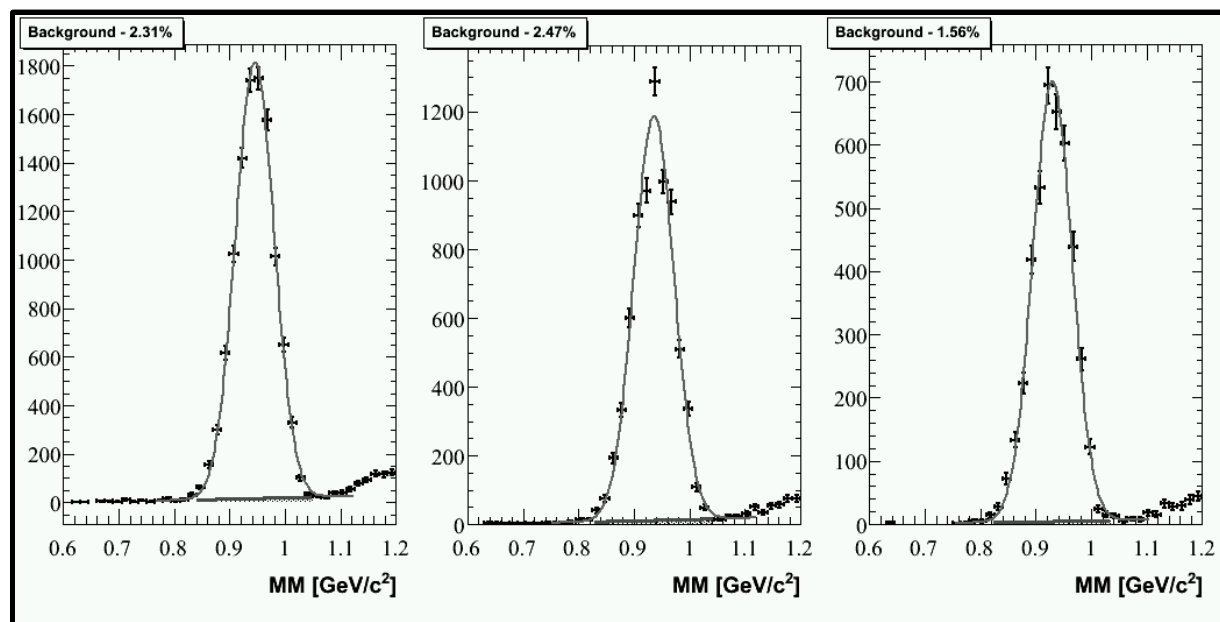
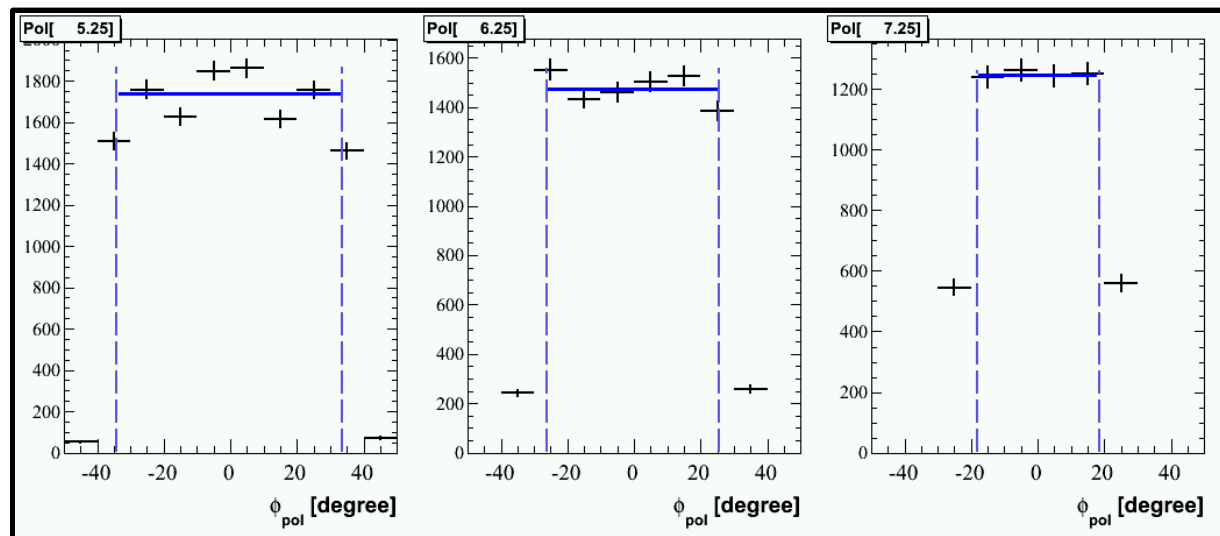
$L \sim \text{Countrate (Sum of the Starts)}$

Luminosity via pp elastic scattering

$$L = \frac{N'_{\text{exp}}}{A'_{\text{det}} \varepsilon'_i (d\sigma/d\Omega)'}$$



2D acceptance of
 $pp \rightarrow pp$ @ ANKE

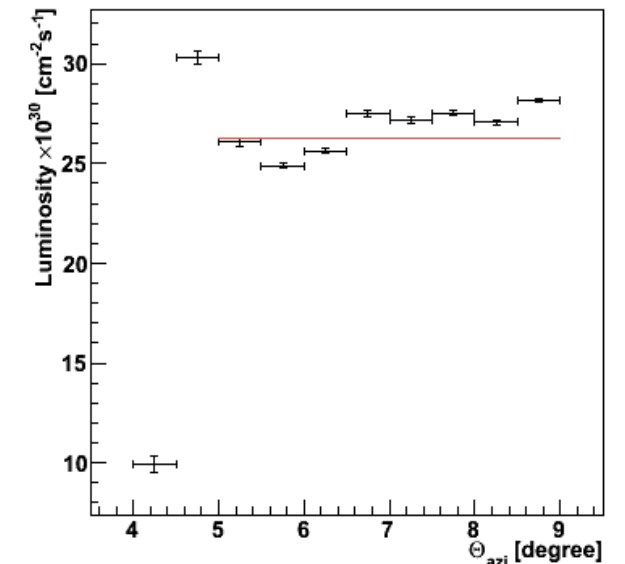
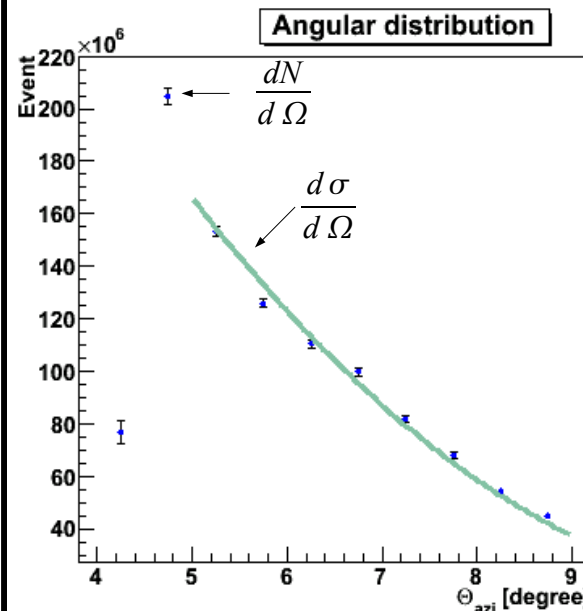
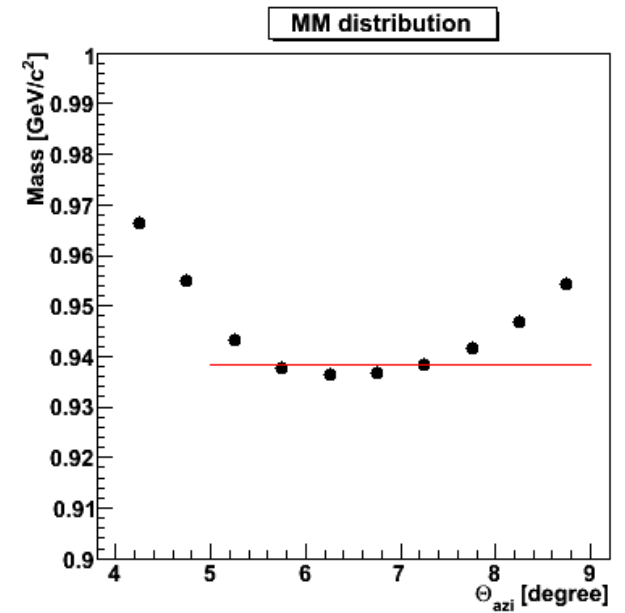
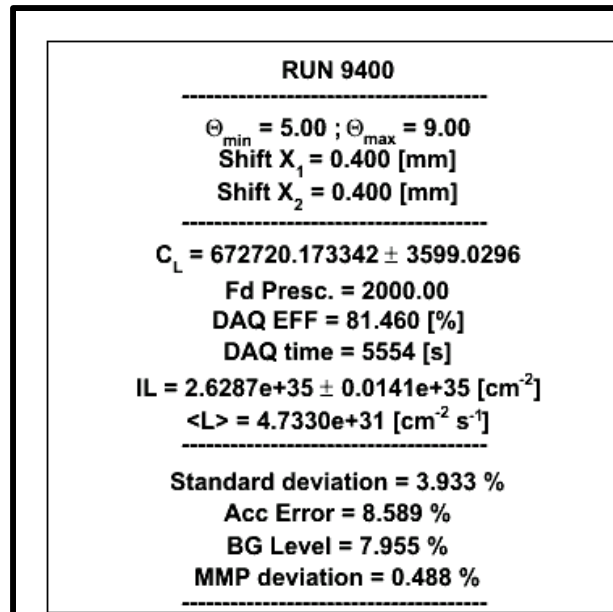


Luminosity via pp elastic scattering

$$N_{pp} = \frac{N_{det} \times p}{\epsilon_{det} \times \epsilon_{dt}}$$

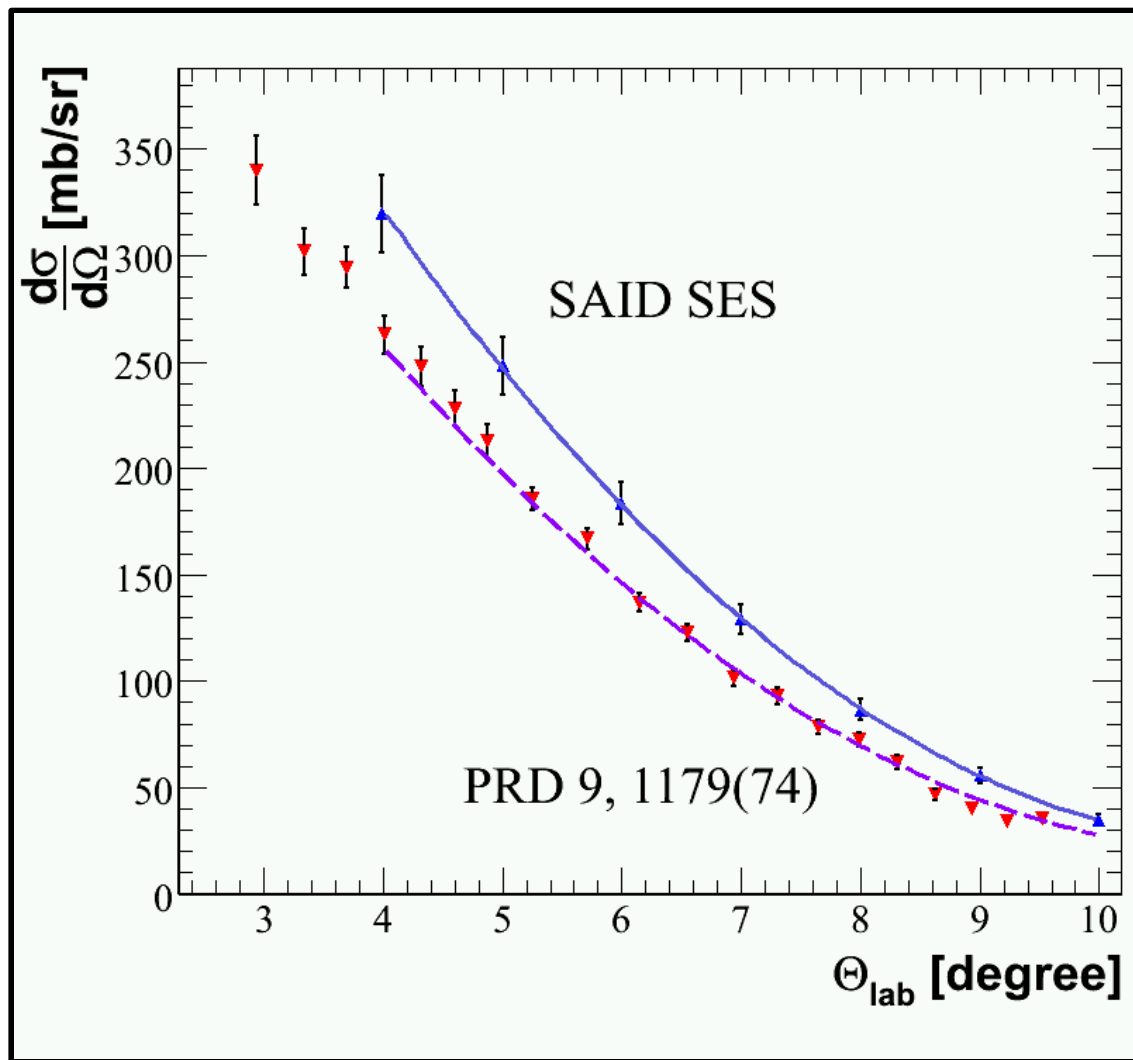
where

- N_{det} is number of reconstructed events via MM
- p is prescaling factor
- ϵ_{det} is detection efficiency
- ϵ_{dt} is dead time correction



Difference between 2 XS

- ▲ SAID Single Energy Solution for $T_p = 2.83\text{GeV}$
- ▼ Experimental measurements @ 2.83GeV



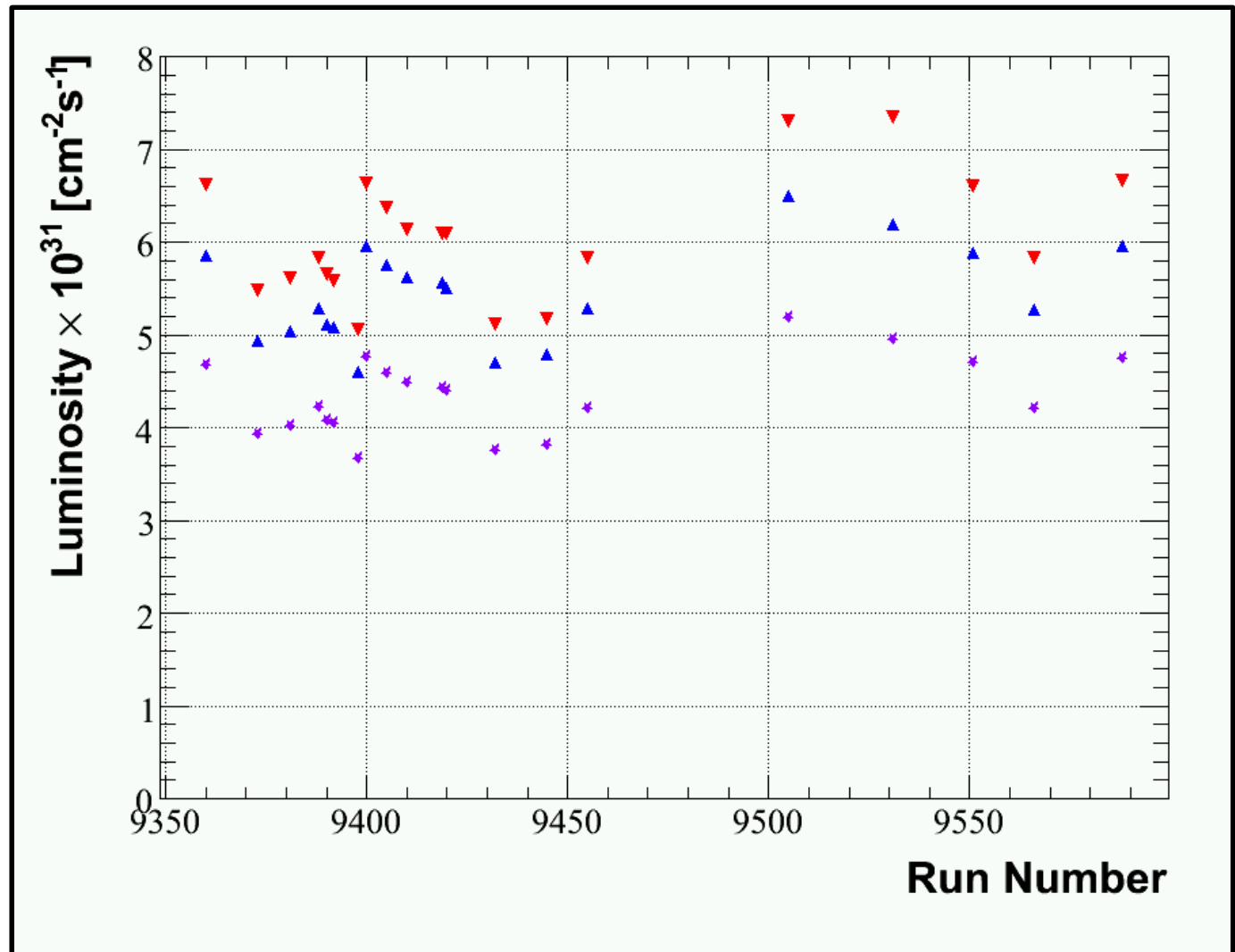
Comparison of pp and Schottky

- ▼ Schottky
- ▲ pp elastic (experimental data)
- ★ pp elastic (SAID SES)

$$\text{diff} = \frac{L_{\text{Schottky}} - L_{pp}}{L_{\text{Schottky}}}$$

Difference (SAID) ~ 27%

Difference (Exp.) ~ 5%



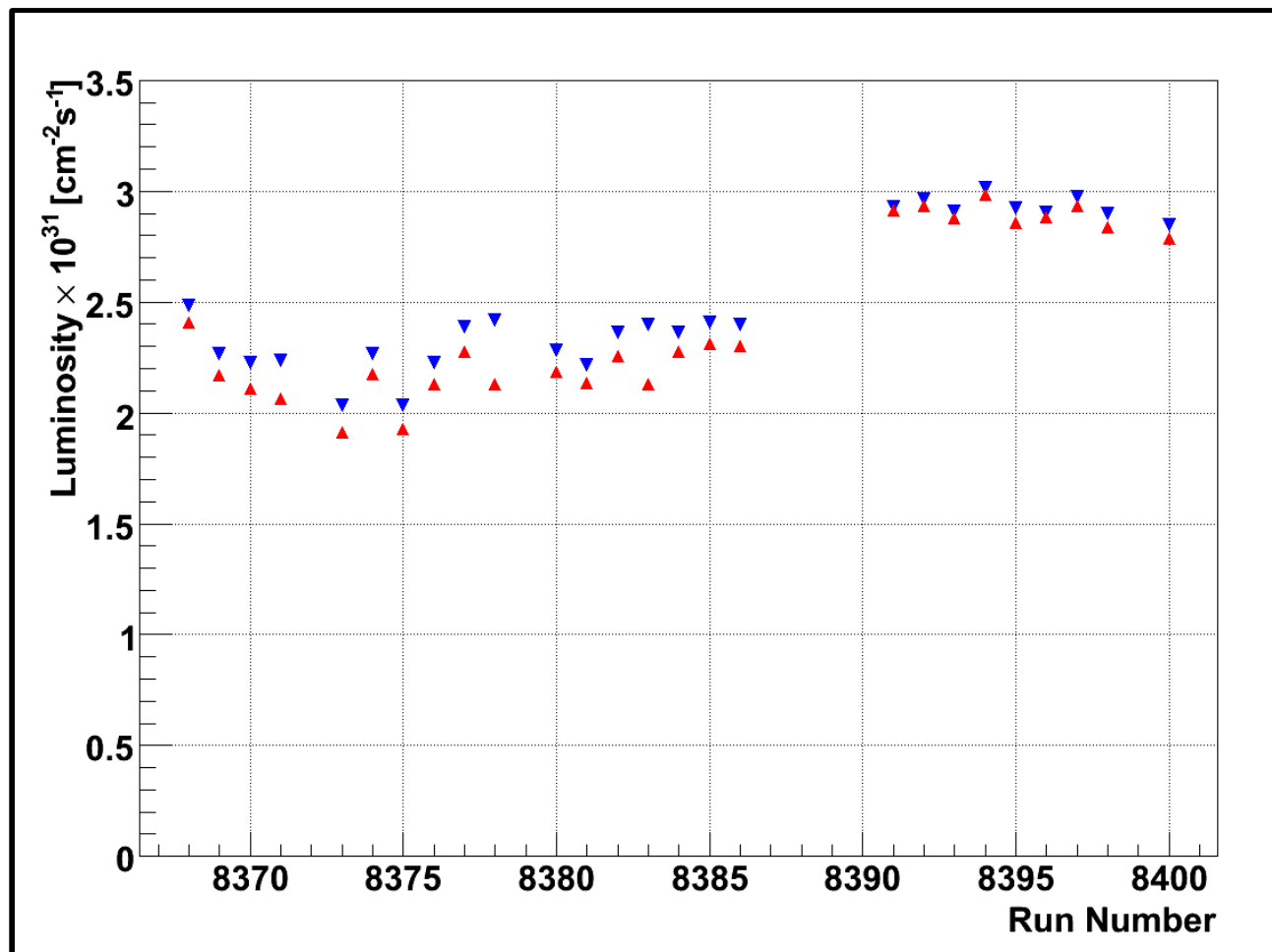
Comparison of dp and Schottky

▼ dp elastic

▲ Schottky

$$diff = \frac{L_{Schottky} - L_{dp}}{L_{Schottky}}$$

Difference < 5%



Uncertainties for both method

Error propagation via energy loss measurement

BCT: $I \approx 10\text{mA}$ $\sigma \leq 1\%$

Frequency shift: $\Delta f/f \approx 0.6\text{Hz/s}$ $\sigma \leq 3\%$

Eta: $\leq \eta \approx -0.103$ $\sigma \leq 5\%$

Ring gas: $Nt \sim 10^{14}\text{cm}^{-2}$ $\sigma \leq 3\%$

Stopping power: dE/dx $\sigma \leq 1\%$

Error propagation via *pp* elastic reaction

Detector Eff.: $\varepsilon \sim 5\%$

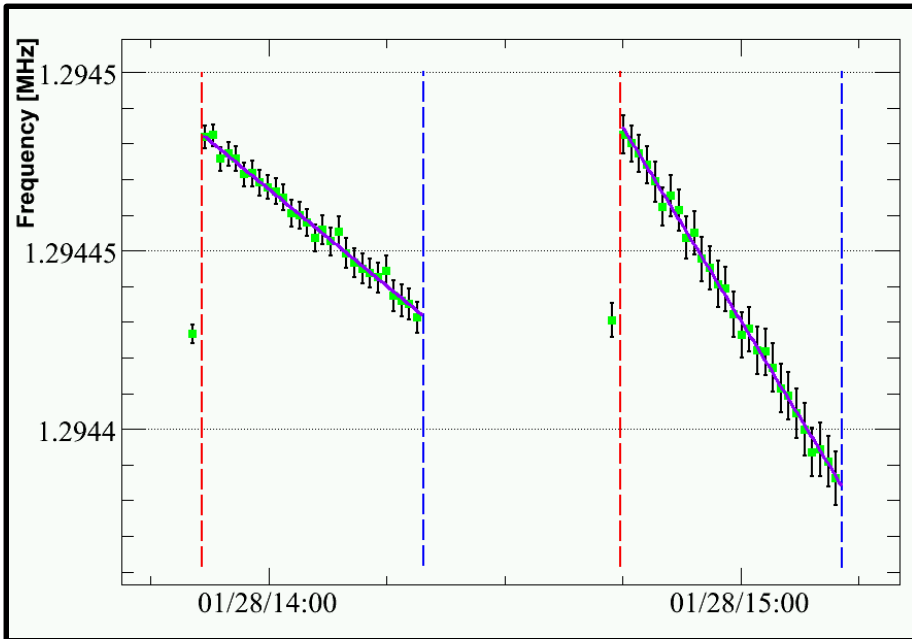
Acceptance: $A \sim 8\%$

Statistical error: $\varepsilon \sim 2\%$

SAID: $\leq 2\% ?$

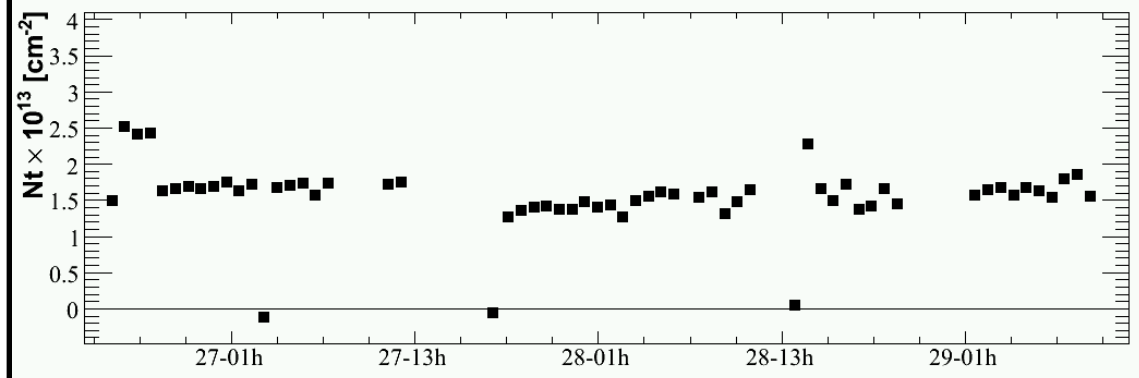
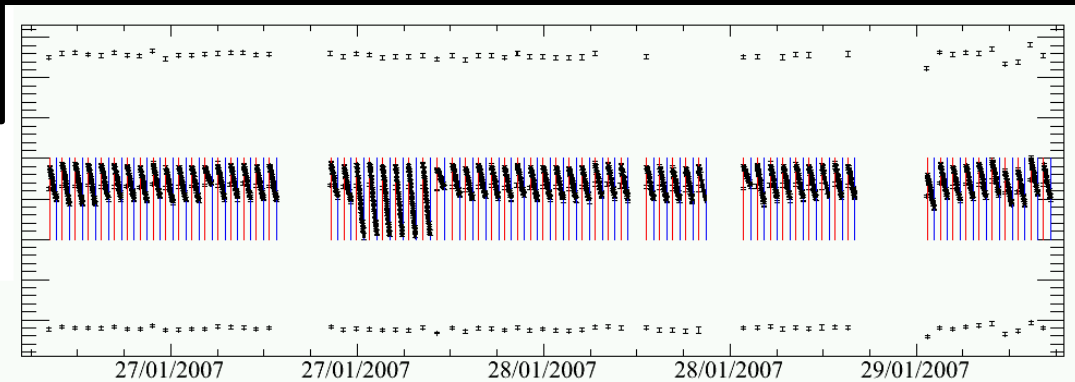
BG subtraction: $\leq 3\%$

With internal cell target



Total frequency shift $\sim 3.6 \cdot 10^{13} \text{ [cm}^{-2}\text{]}$
 Rest+Ring Gas $\sim 1.8 \cdot 10^{13} \text{ [cm}^{-2}\text{]}$

Cell TARGET thickness $\sim 1.8 \cdot 10^{13} \text{ [cm}^{-2}\text{]}$



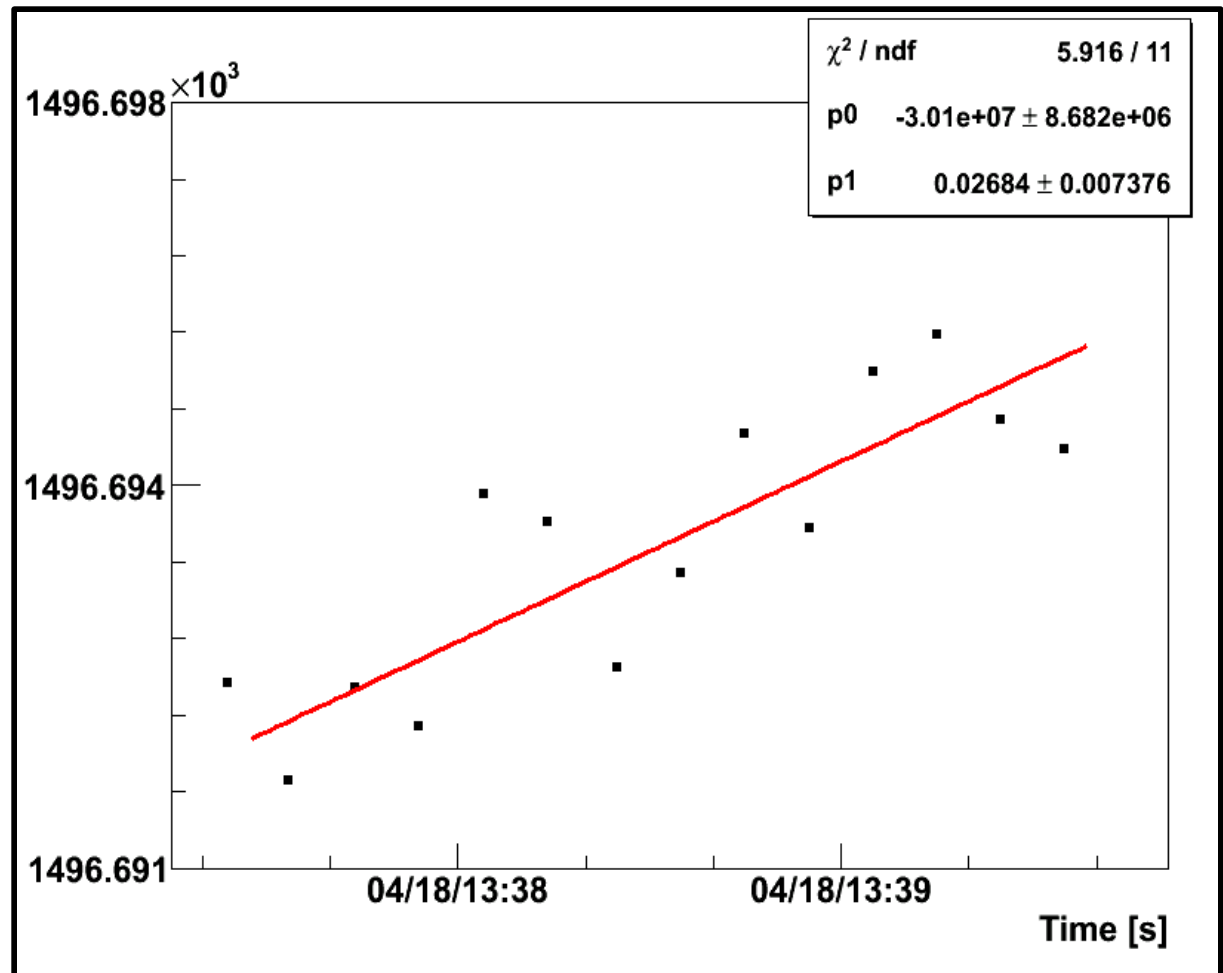
$\eta = 0.2164$; // average
 $f_0 = 1.294358$; // MHz
 $T_0 = 1198$; // MeV

With pellet target

$\eta = 0.02;$ // to small

$f_0 = 1.496688;$ // MHz

$T_0 = 1400;$ // MeV



Conclusion

- I. We have 2 independent method to determine luminosity
 - ◇ via *nuclear* elastic scattering
 - ◇ via *energy loss* measurement

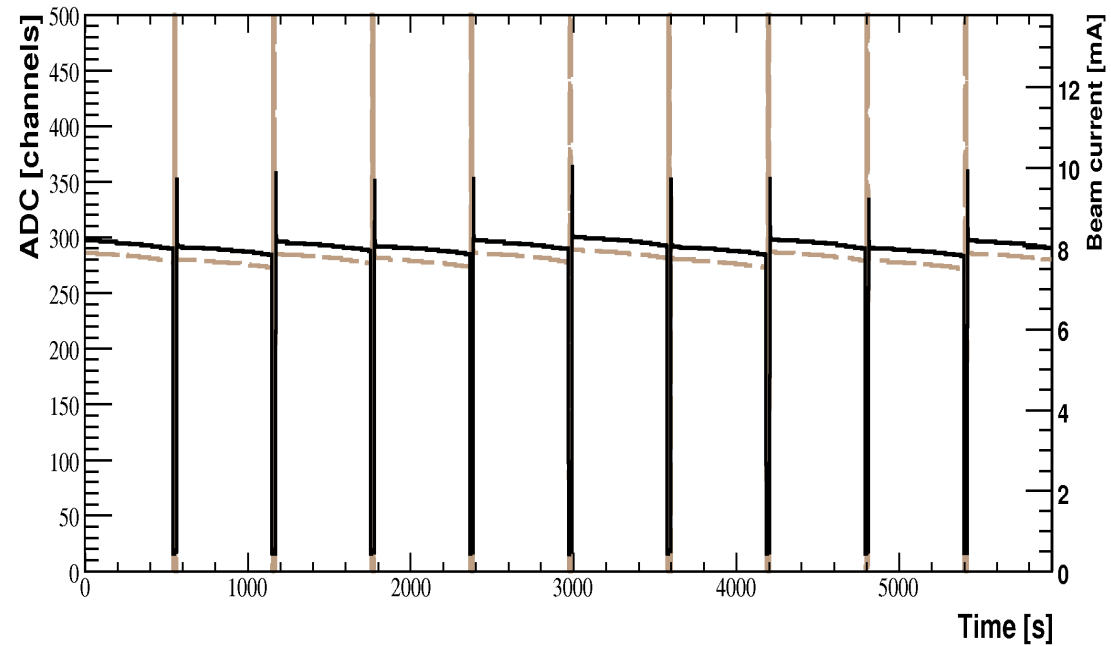
- II. Both methods just coincide within the error limits

- III. We can use 'Schottky' method for different targets
 - ◇ with cluster jet target
 - ◇ with cell target
 - ◇ with pellet target

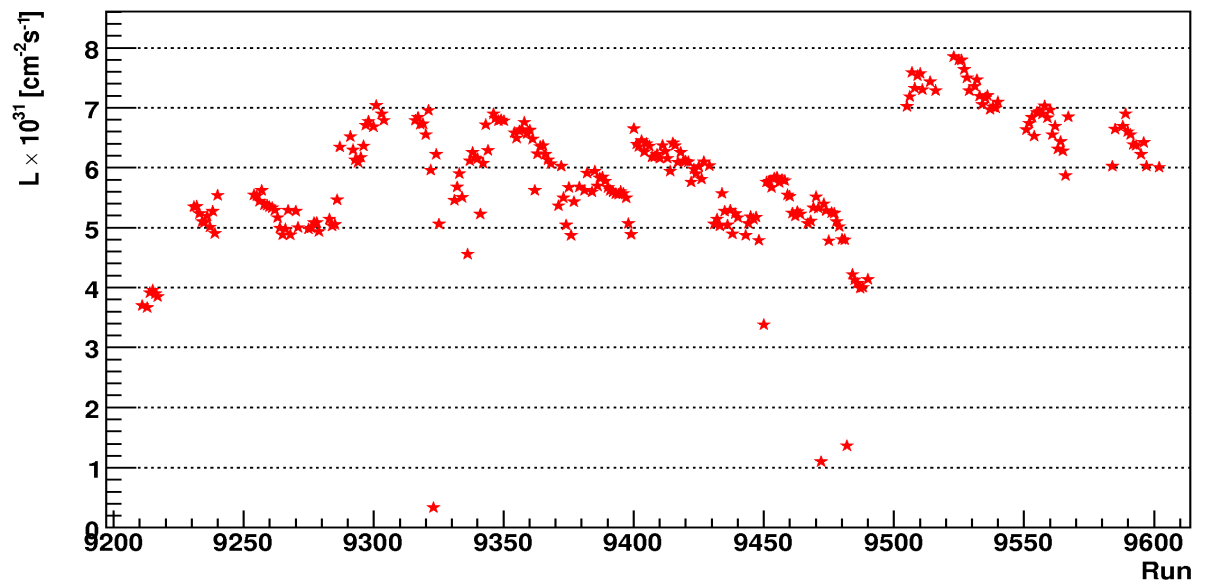
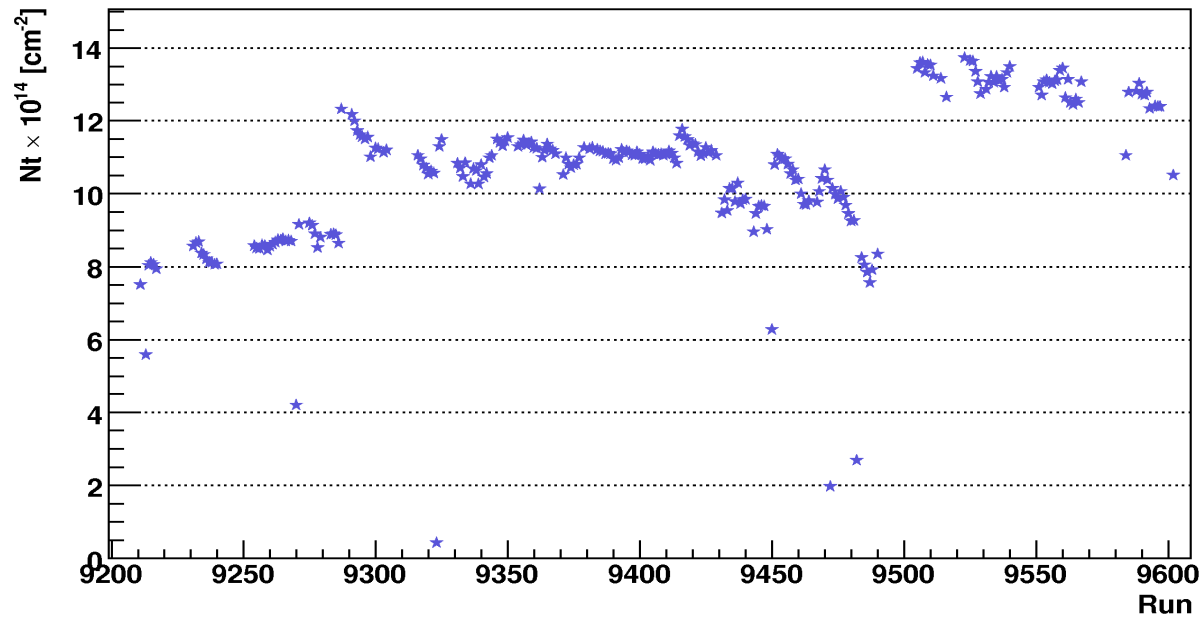
Beam intensity determination

$$J_{beam} = \frac{I_{beam}}{q_p}, [S^{-1}]$$

- Calibration (ADC-mA)
- Offset determination (EDDA, between cycles)



Luminosity determination



Schottky Method for ANKE

