

## Classical Solution of Wave equation

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$$\nabla^2 u = \frac{1}{c^2} \frac{\partial^2 u}{\partial t^2} ; u : \text{displacement}$$

- One dimensional

$$\frac{\partial^2 u}{\partial x^2} = \frac{1}{c^2} \frac{\partial^2 u}{\partial t^2}$$

$$u(x, t) = f(x - ct) + g(x + ct)$$

- Spherical Symmetry

$$\frac{\partial^2 u}{\partial r^2} + \frac{2}{r} \frac{\partial u}{\partial r} - \frac{2u}{r^2} = \frac{1}{c^2} \frac{\partial^2 u}{\partial t^2}$$

$$u(r, t) = f \frac{(r - ct)}{r} + g \frac{(r + ct)}{r}$$

- Cylindrical Symmetry

$$\frac{\partial^2 u}{\partial r^2} + \frac{1}{r} \frac{\partial u}{\partial r} - \frac{u}{r^2} = \frac{1}{c^2} \frac{\partial^2 u}{\partial t^2}$$

$$u(r, t) = \sum_{n=1}^{\infty} c_n J_1(\varepsilon_n \xi) \cos(\varepsilon_n \theta)$$

$$\xi = r/R, \theta = ct/R$$

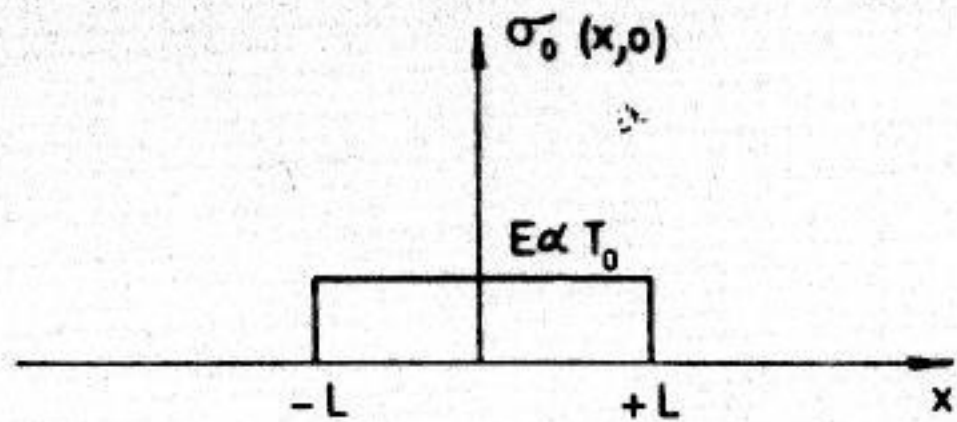


Fig. 1 Initial axial stress distribution in an instantaneously heated rod.

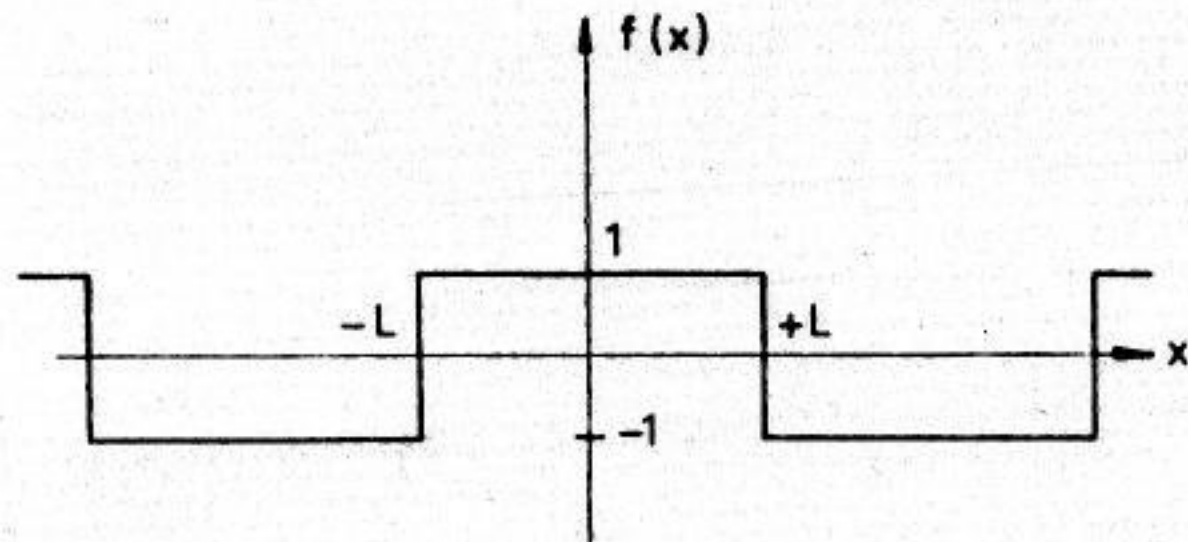


Fig. 2 The square wave describing the initial axial stress distribution in the rod  $-L \leq x \leq +L$ .

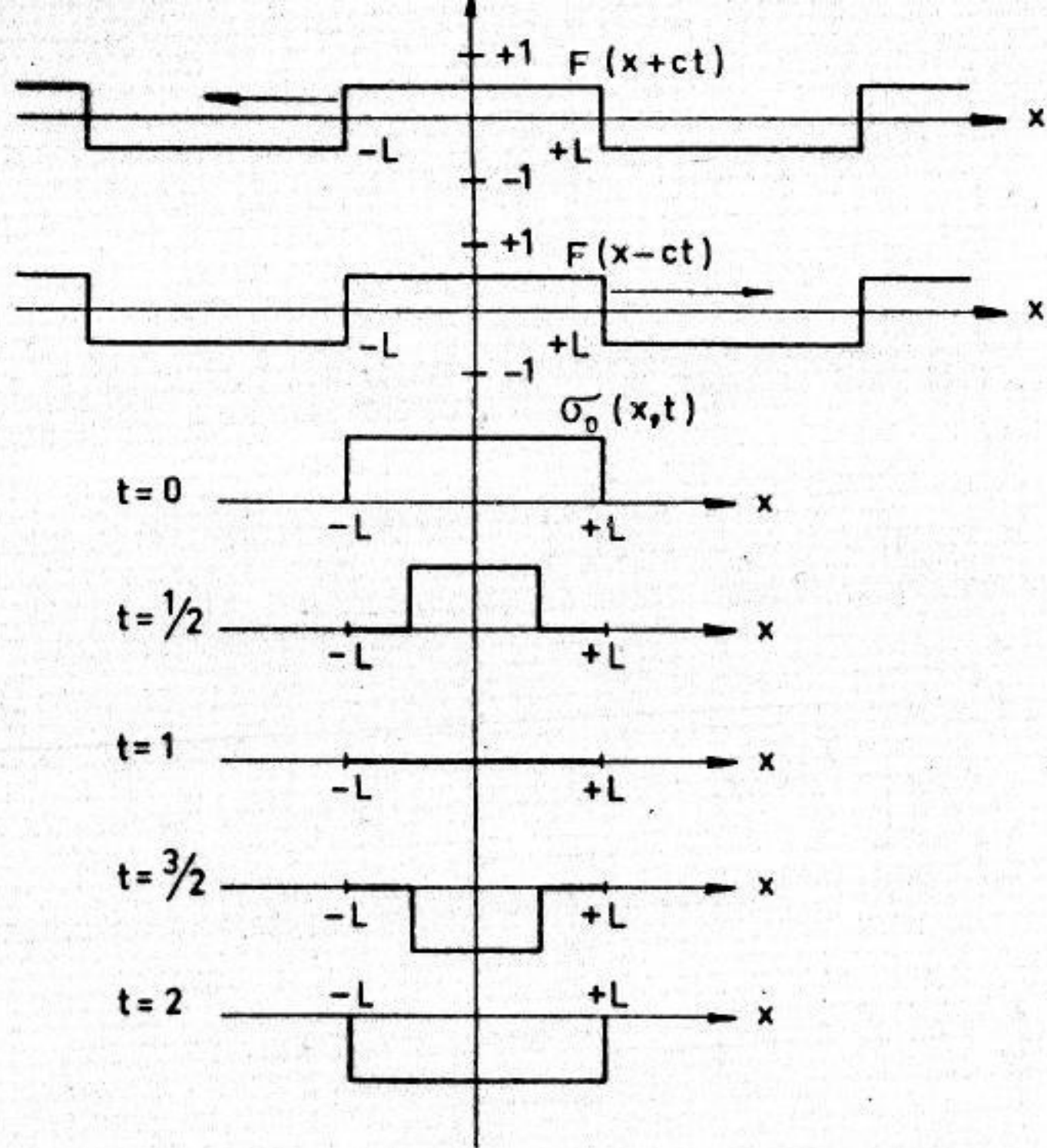
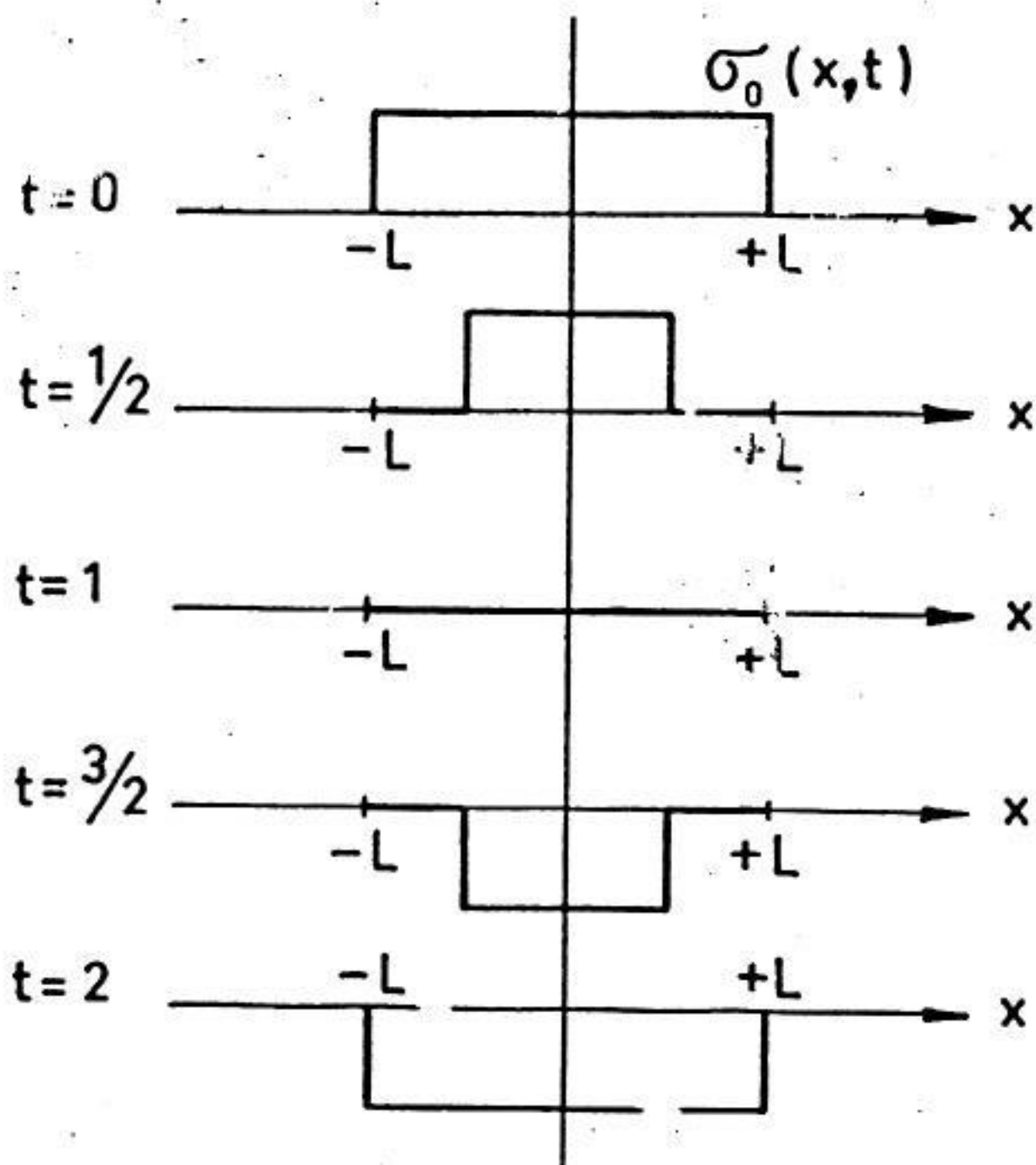
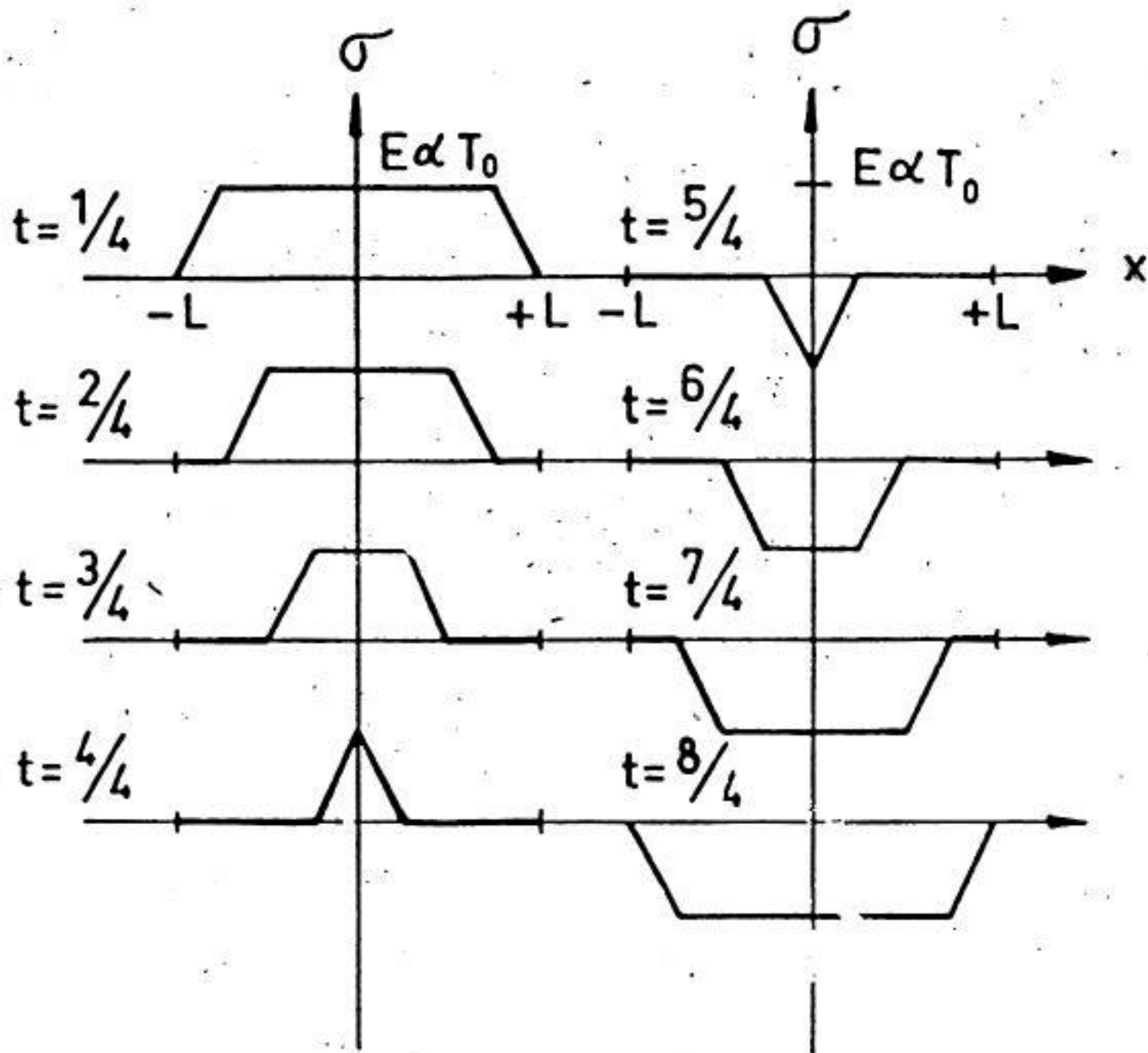


Fig. 3 The development of the axial stress in the instantaneously heated rod, obtained by the superposition of two square waves  $F(x,t)$ , travelling in opposite directions. The time  $t$  is measured in units of  $L/c$ .



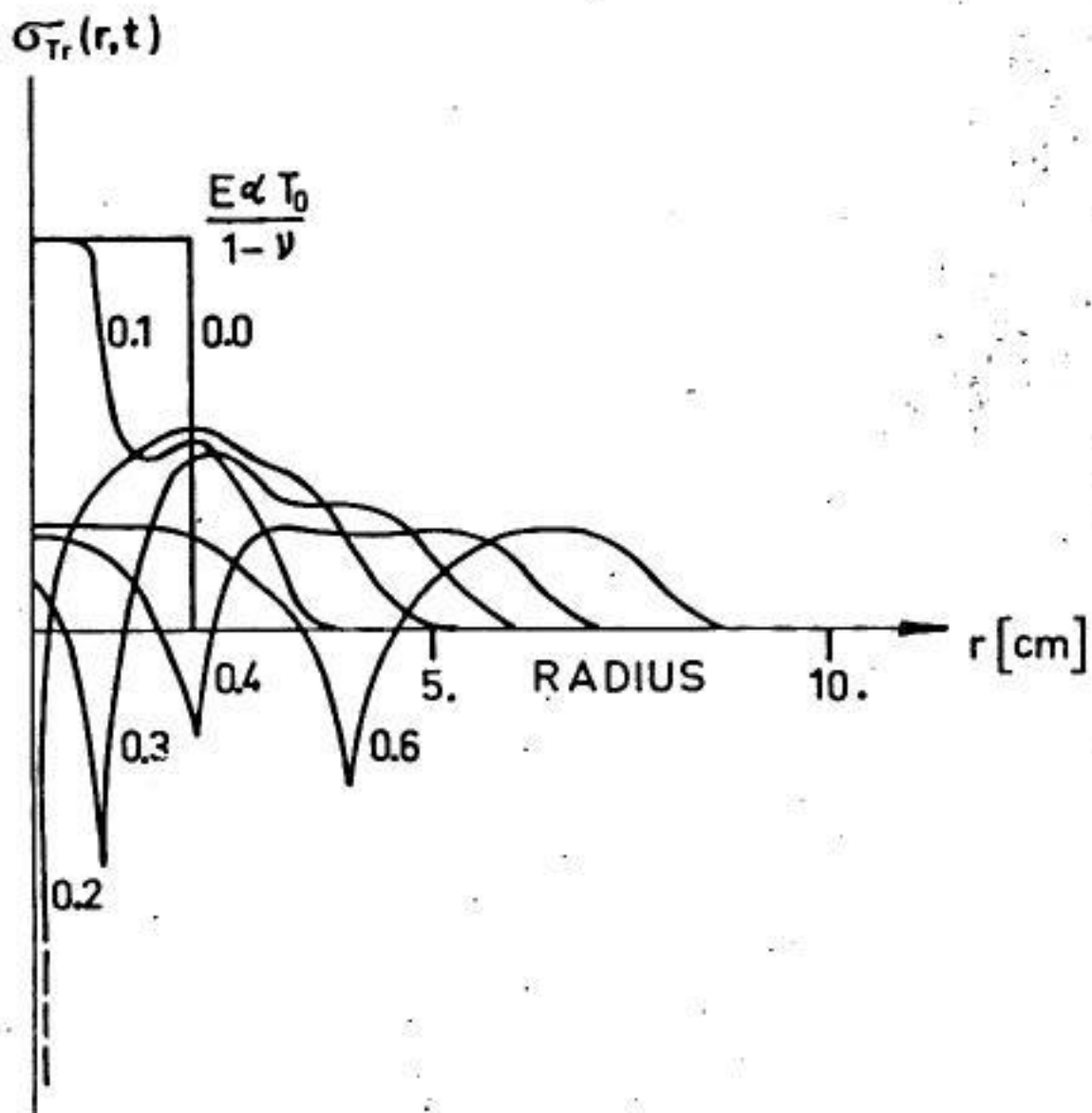


Fig. 13 The total (quasi-static plus dynamic) radial stress in an instantaneously heated disk of radius  $R$  at different times. The time parameters are given in units of  $R/c$ .

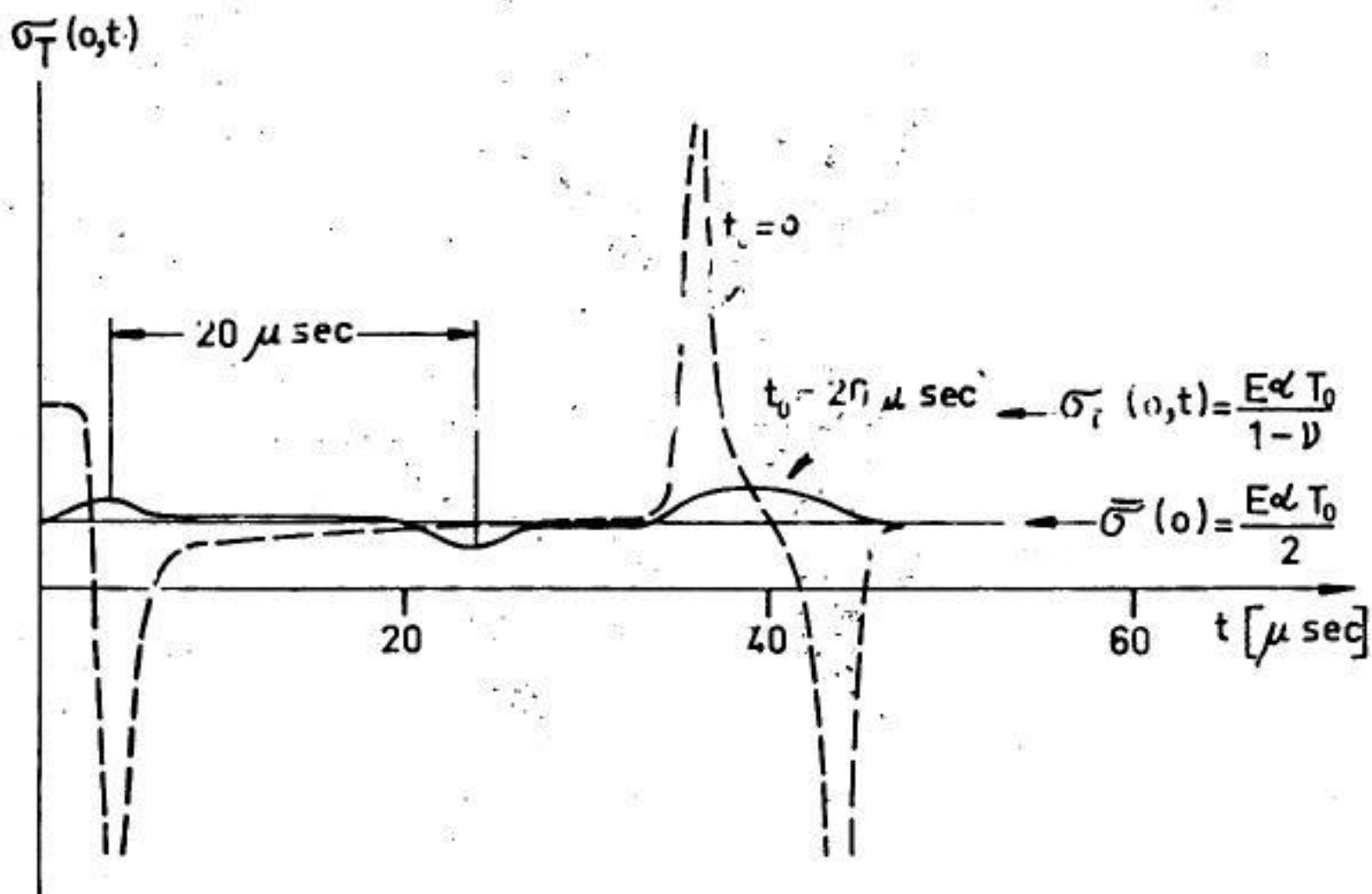
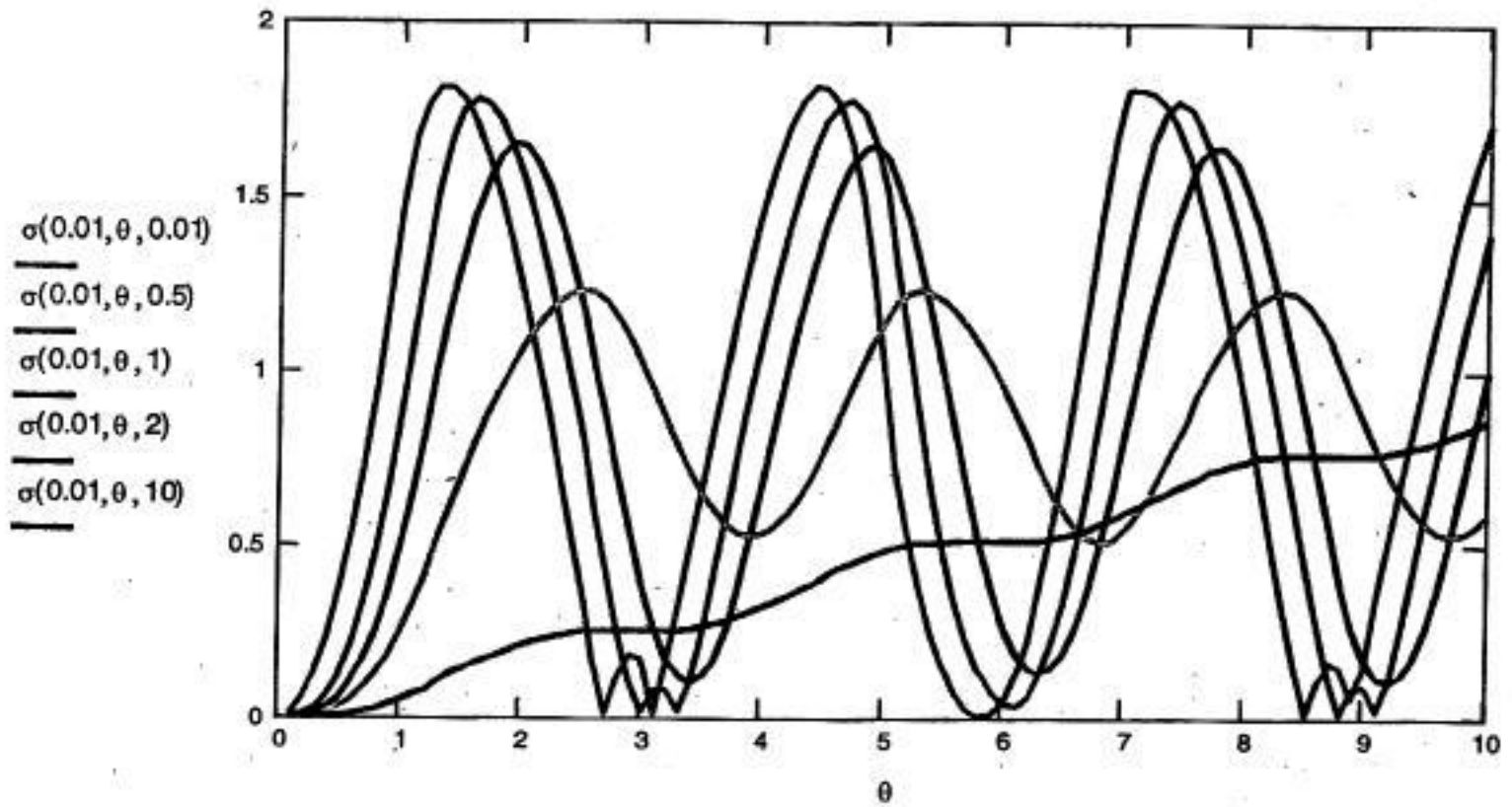
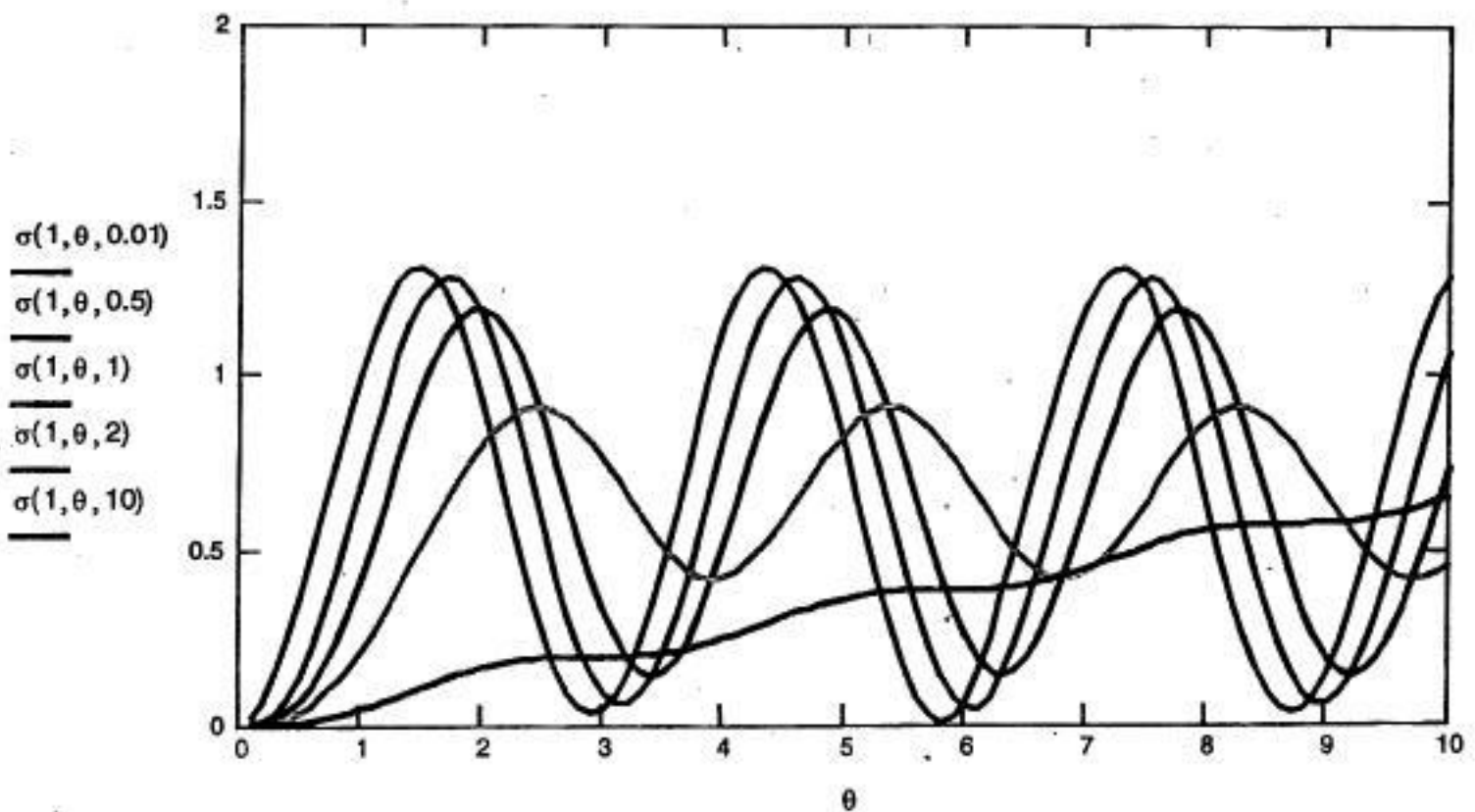


Fig. 14 The development of the total central stress in time for an infinitely rapid ( $t_0 = 0$ ) and a finite ( $t_0 = 20 \mu \text{sec}$ ) temperature increase.



**Fig. 1:** Equivalent v. Mises stress (in relative units of  $E\alpha_L\Delta T_0$ ) vs. time  $\theta$  ( $\theta$  in relative units of  $R/c$ ) in the center of a solid target. In addition to the black curve, which is for infinitely fast heating, also oscillations are shown for uniform heating over the durations  $\theta_0 = 0.5, 1, 2$  and  $10$  ( $\theta_0$  in units of  $R/c$ ).

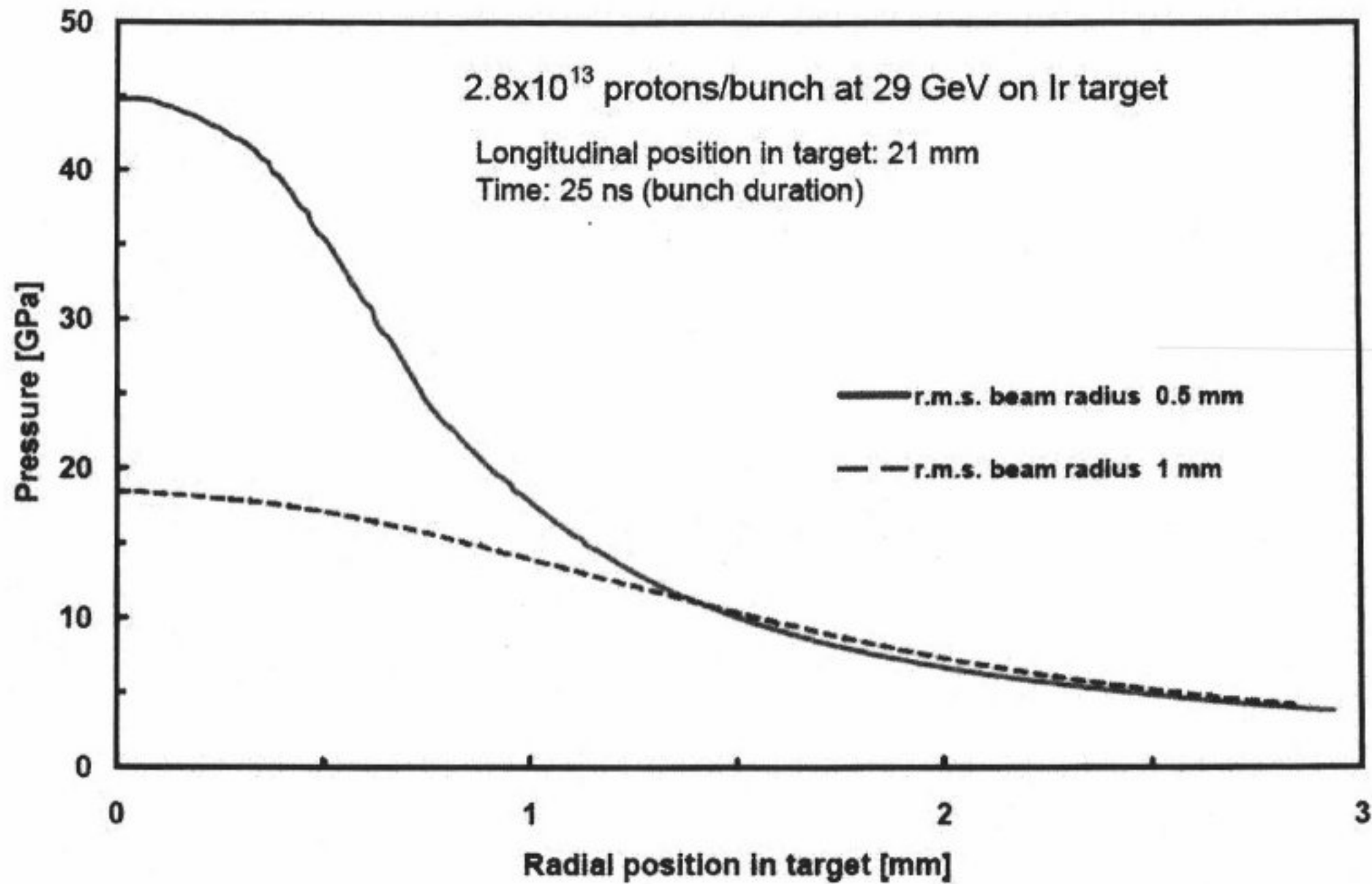


**Fig. 2:** Equivalent v. Mises stress vs. time at the outer radius of a solid target. The same units as in Fig. 1 apply.



# Pressure in Ir

(by N. Tahir, Aug. 2006)

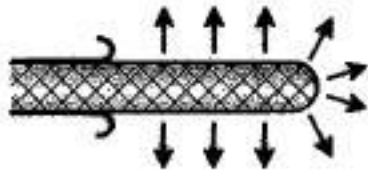


Burst Frequency : 50 Hz

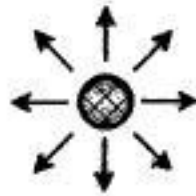
Target : 1cm x 1cm

L = 40cm

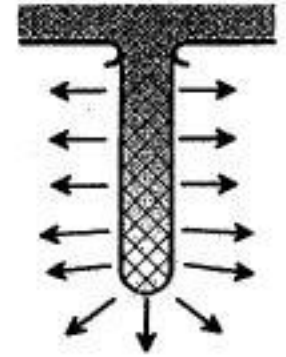
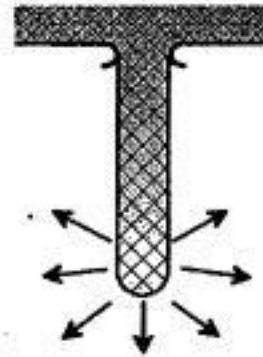
Free  
Jet



Pulsed  
Curtain



Continuous Curtain  
Tip explodes    Curtain explodes



Volume Flow  
( cm<sup>3</sup>/s )

2000.

2000.

2000.

5000.

Velocity at  
nozzle  
( m/s )

>20.

1.25

0.5

1.25

Pressure  
( kPa )

2700

10.5

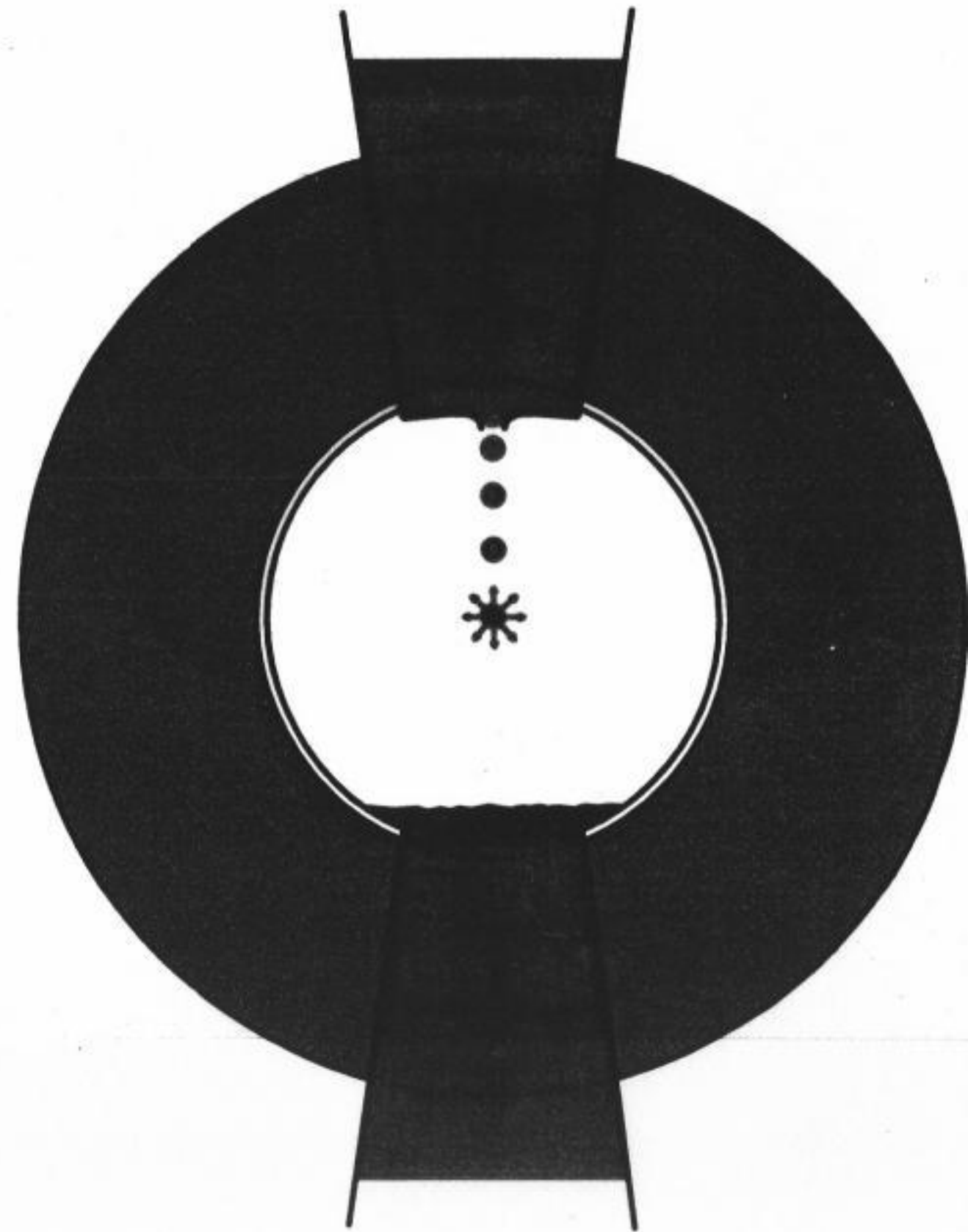
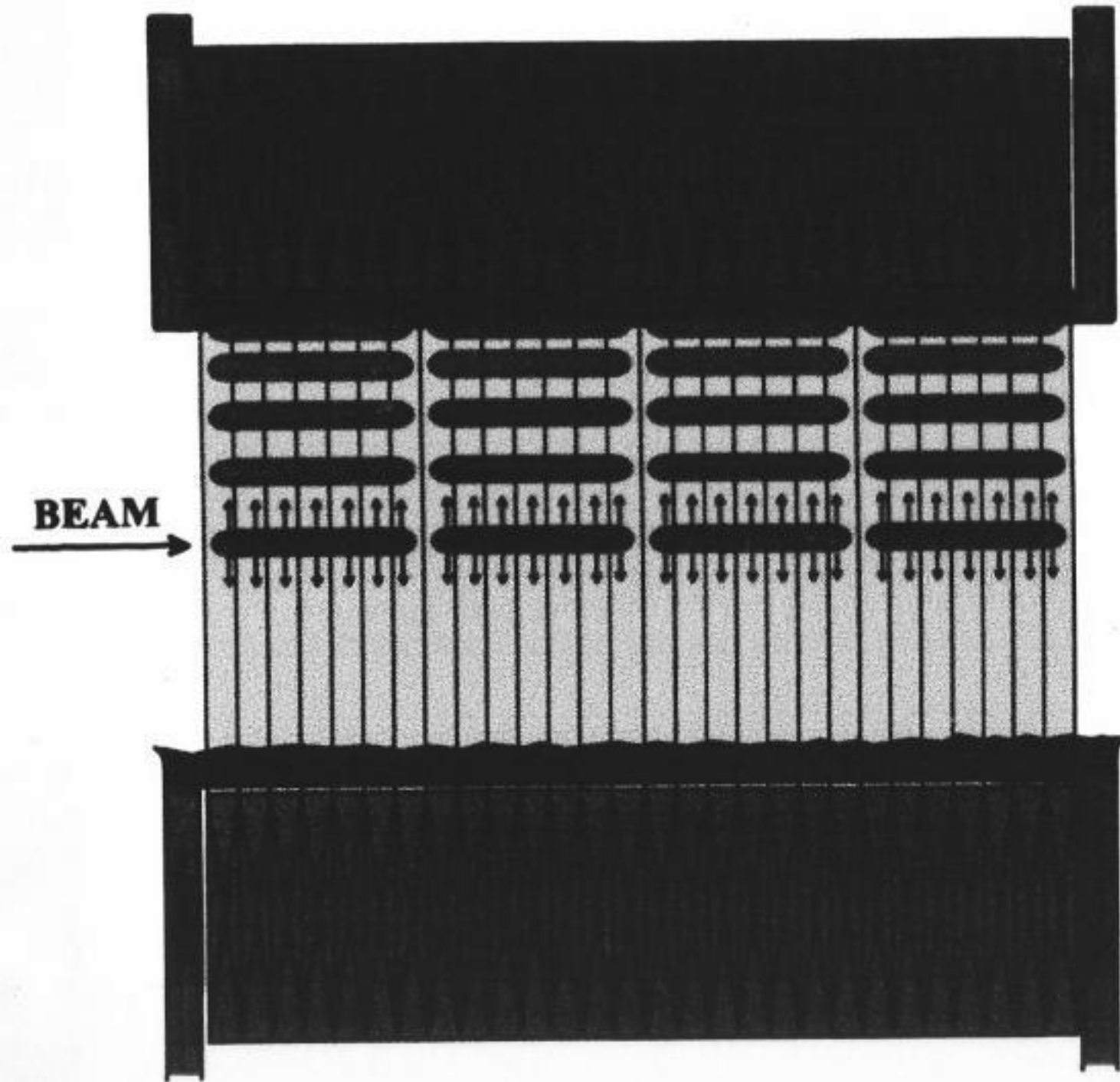
1.7

10.5

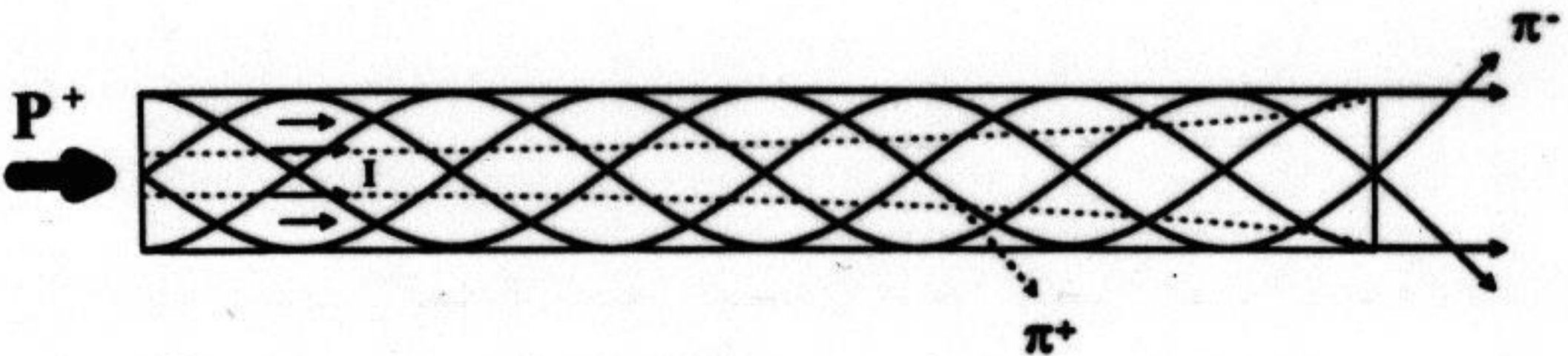
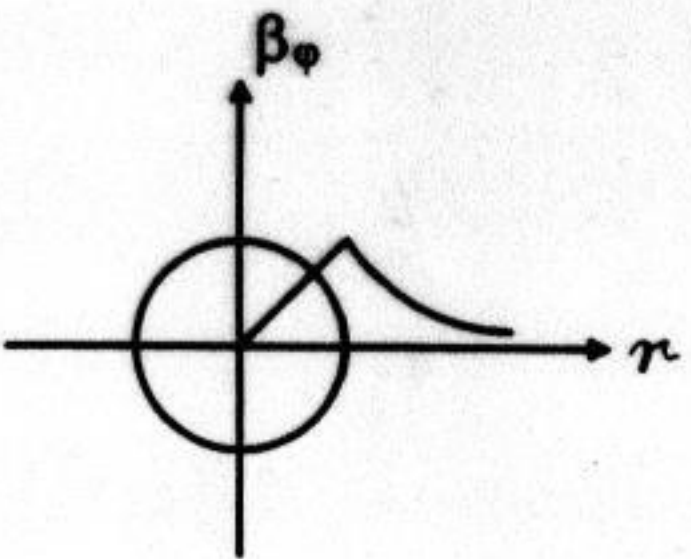
Pulsed Pressure.  
Mech. or el. magn.  
valve



# LIQUID TARGET RADIAL INJECTION INTO SOLENOID





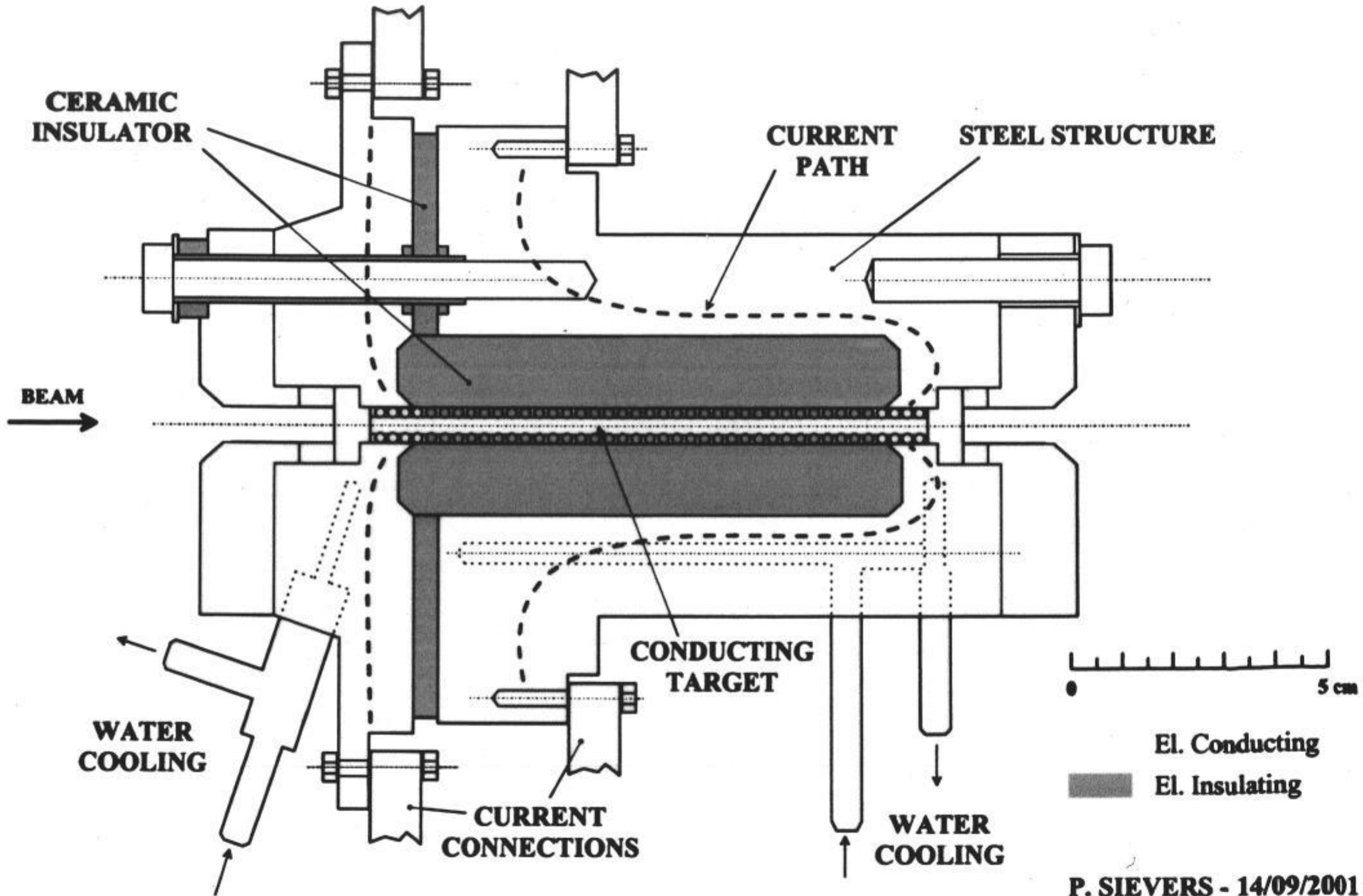


SOLENOID



$p = 500 \text{ MeV/c}$   
 $R = 4 \text{ cm}$

# PULSED TARGET





10 CM

