

# Experimental measurement and Monte Carlo simulation of coherent interaction between high-energy particles and oriented crystals

Mr. E. Bagli  
XXVI PhD course  
Tutor Prof. V. Guidi

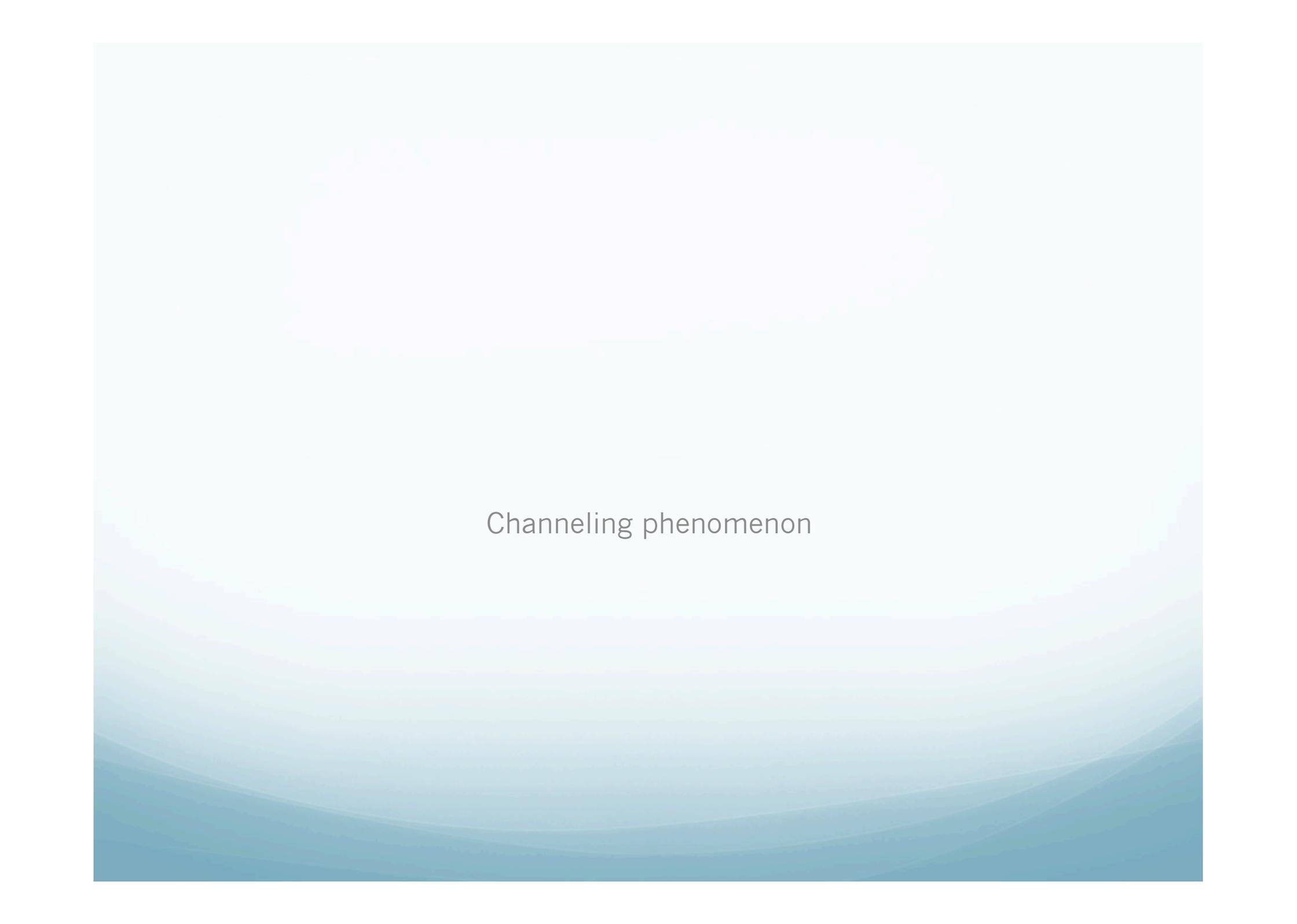


03 December 2013  
Physic and earth science department  
Università degli Studi di Ferrara



# Outline

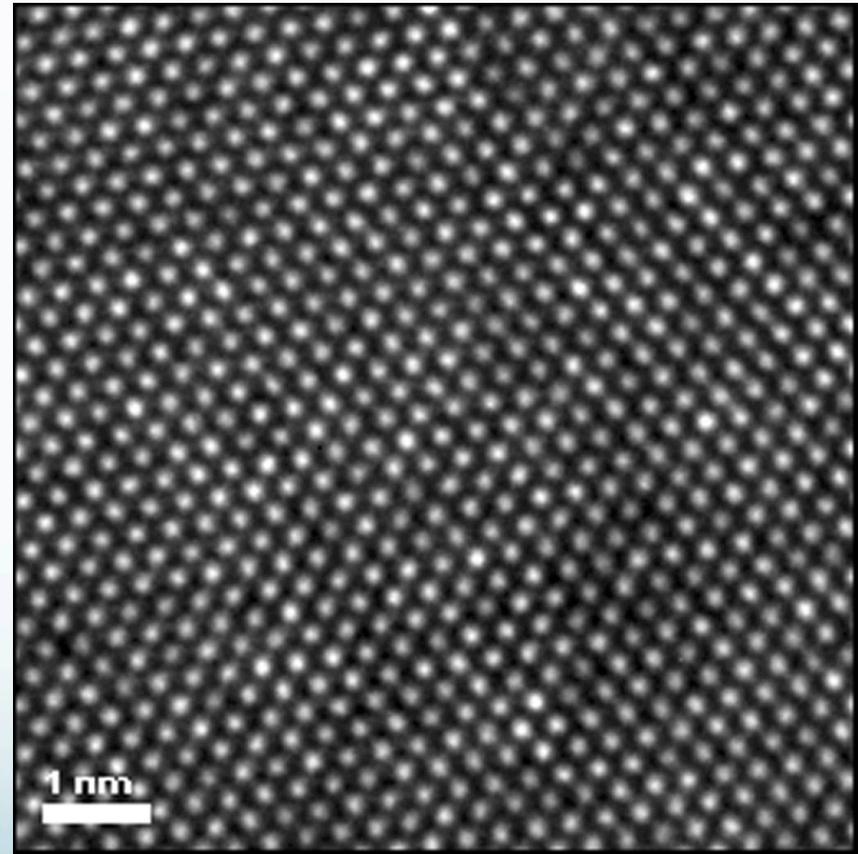
- High-energy coherent phenomena in crystals
- Experiments
  - 400 GeV/c protons:
    - Ge bent strip
    - Si crystalline undulator
    - Multi-crystals
    - SiGe self-bent crystal
  - 150 GeV/c  $\pi^-$ 
    - Dechanneling length
- Monte Carlo
  - DYNECHARM++
  - DYNECHARM++\_Phi
  - Geant4 Channeling



Channeling phenomenon

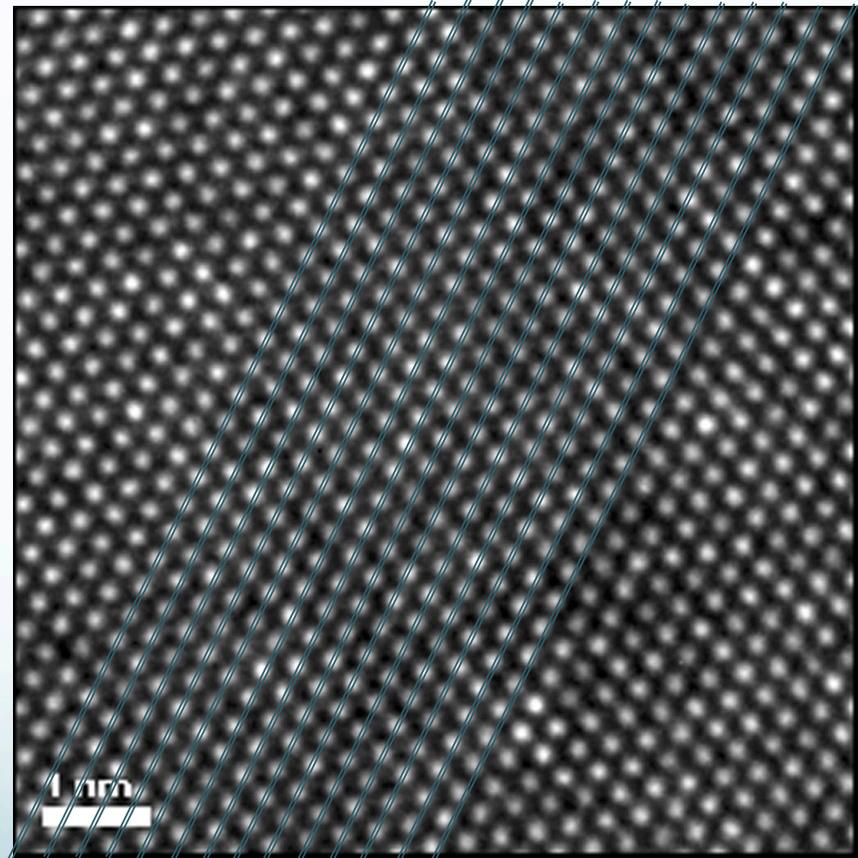
# Crystal

- Ordered pattern of atoms.



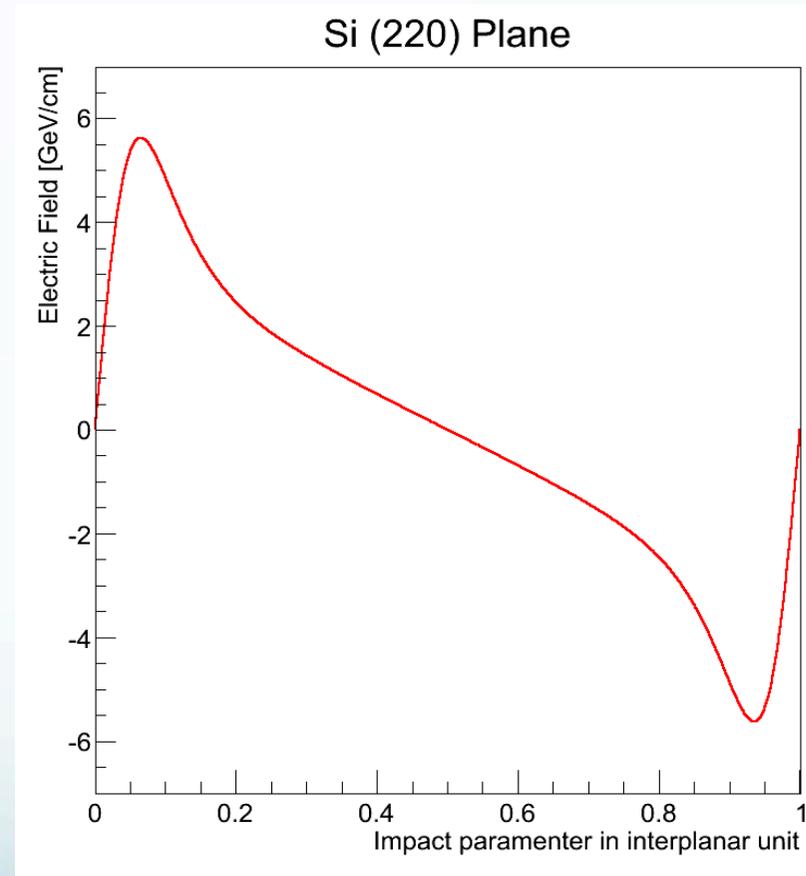
# Crystal

- Ordered pattern of atoms.
- Aligned atoms can be seen as planes or axes.



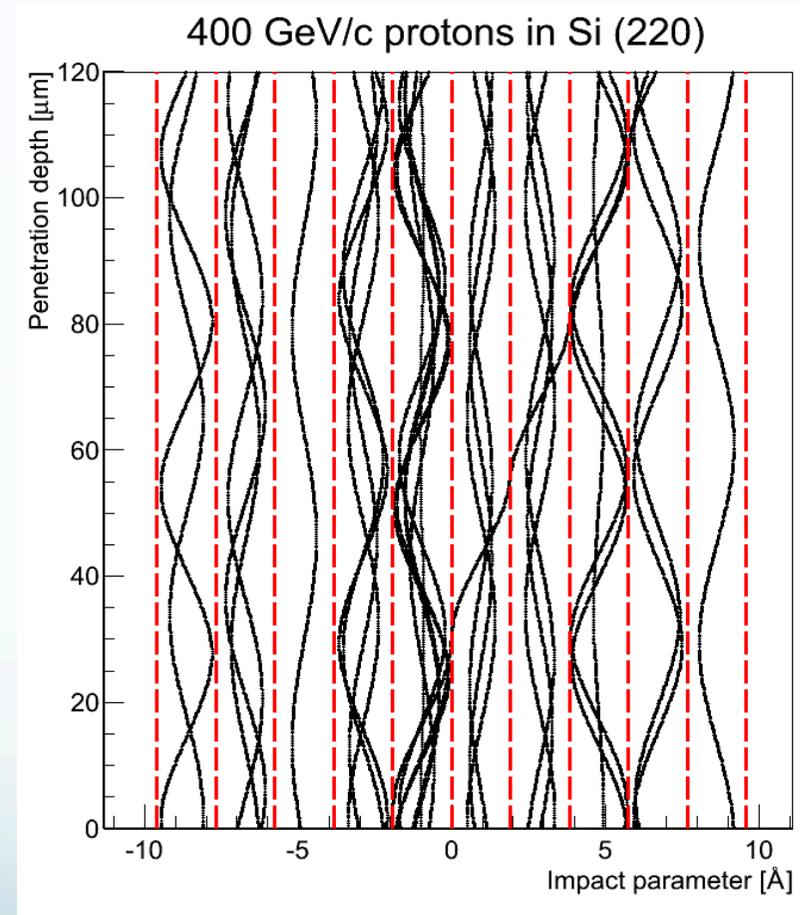
# Crystal

- Ordered pattern of atoms.
- Aligned atoms can be seen as planes or axes.
- Strong electromagnetic field between planes and between axes (GeV/cm).



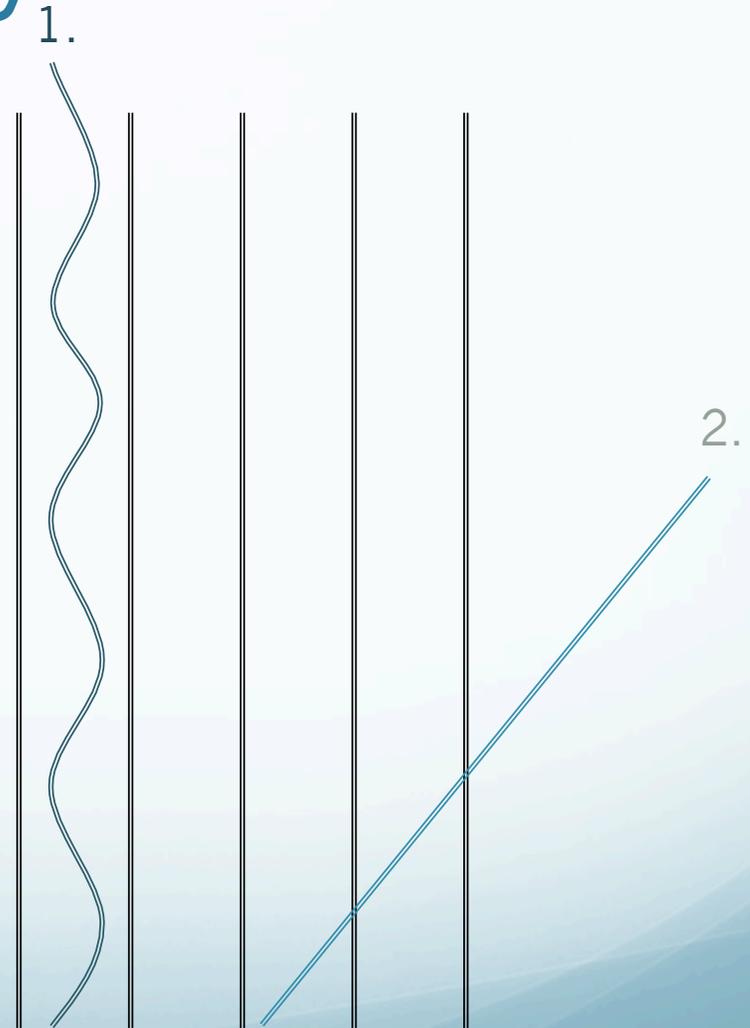
# Crystal

- Ordered pattern of atoms.
- Aligned atoms can be seen as planes or axes.
- Strong electromagnetic field between planes and between axes (GeV/cm).
- Channeling if particle direction

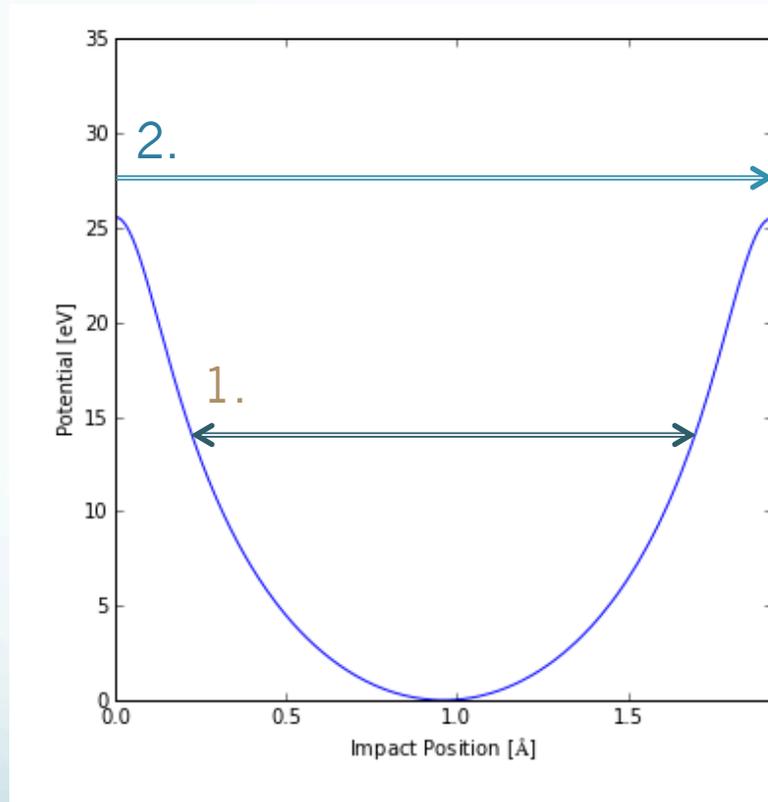


# Straight crystal

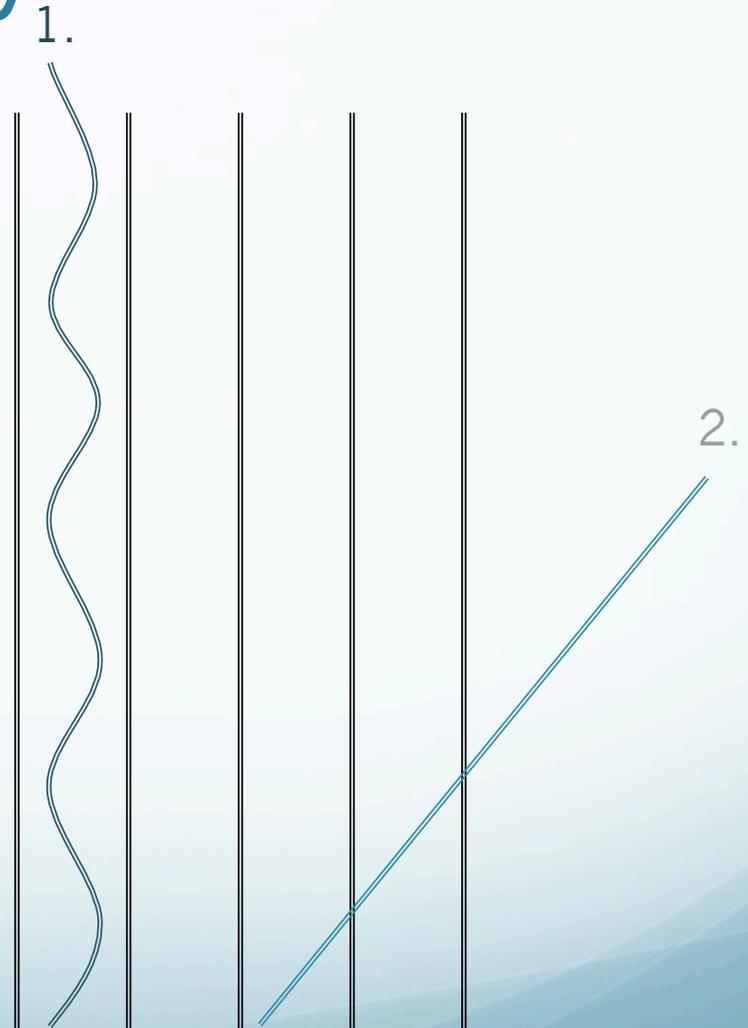
- Particle whose direction of motion is aligned with crystal planes are captured in channeling.



# Straight crystal

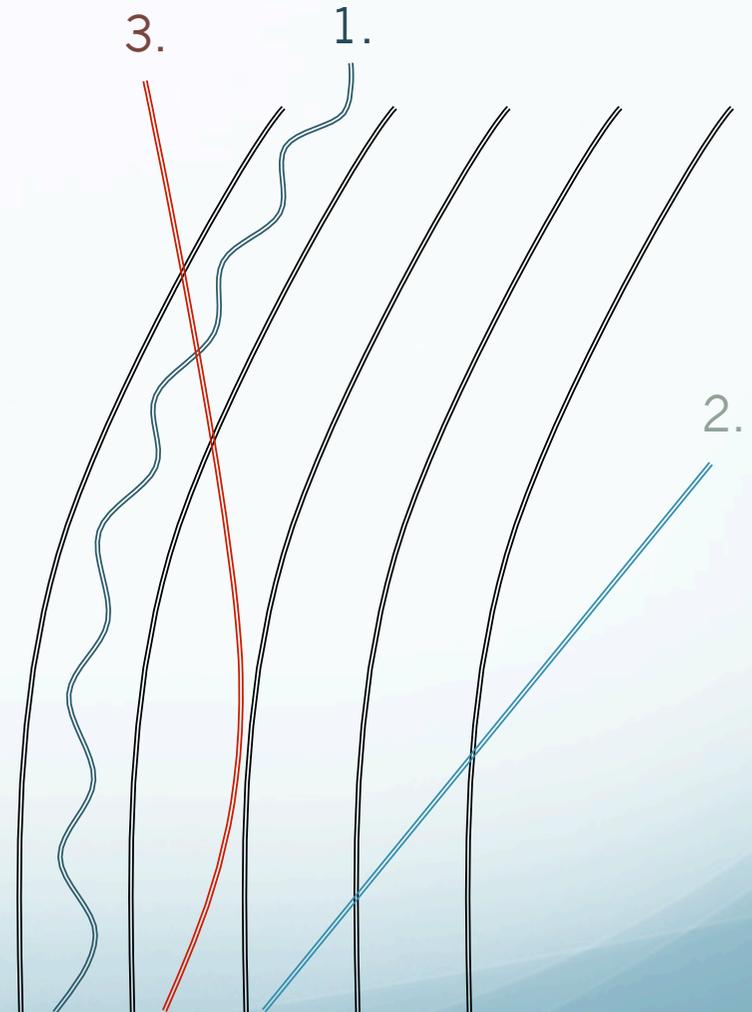


- 1. Channeled
- 2. Not channeled

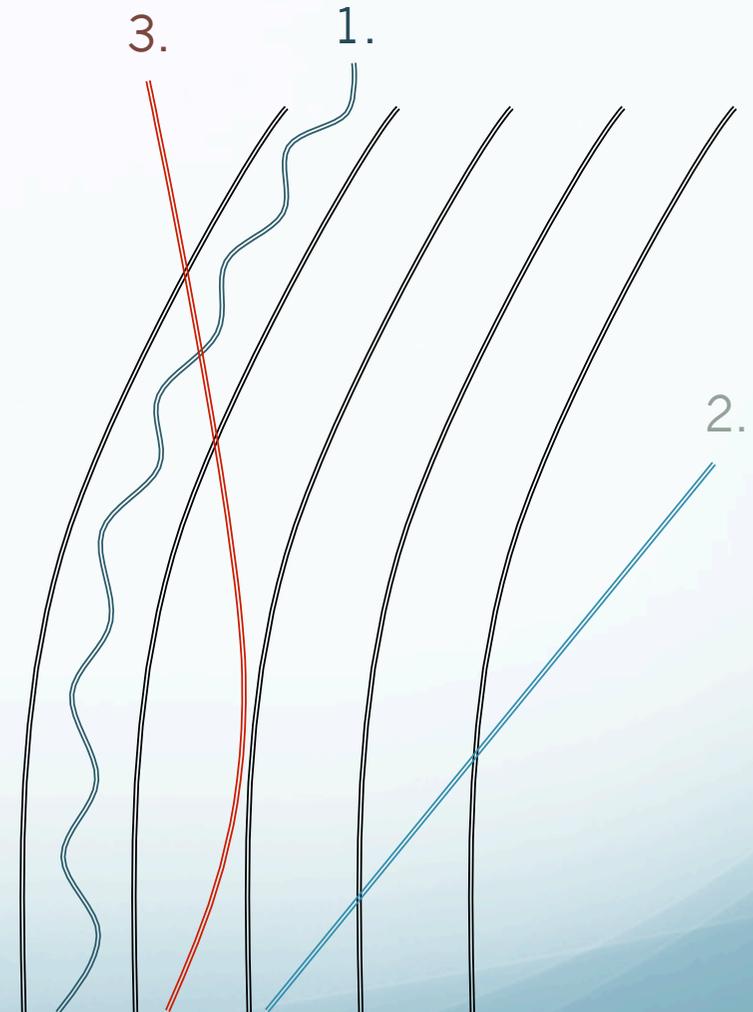
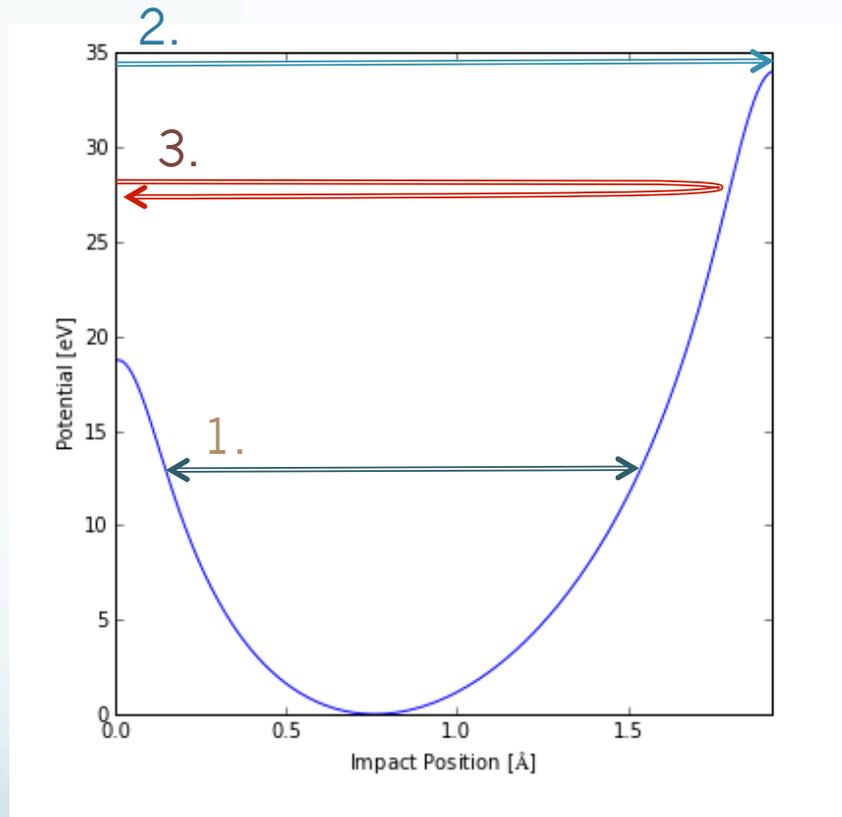


# Bent crystal

- Channeled particles follows the crystal curvature and are deflected (1.).
- Particle whose trajectories is tangent to crystalline planes are “reflected” by the potential barrier (3.)



# Bent crystal

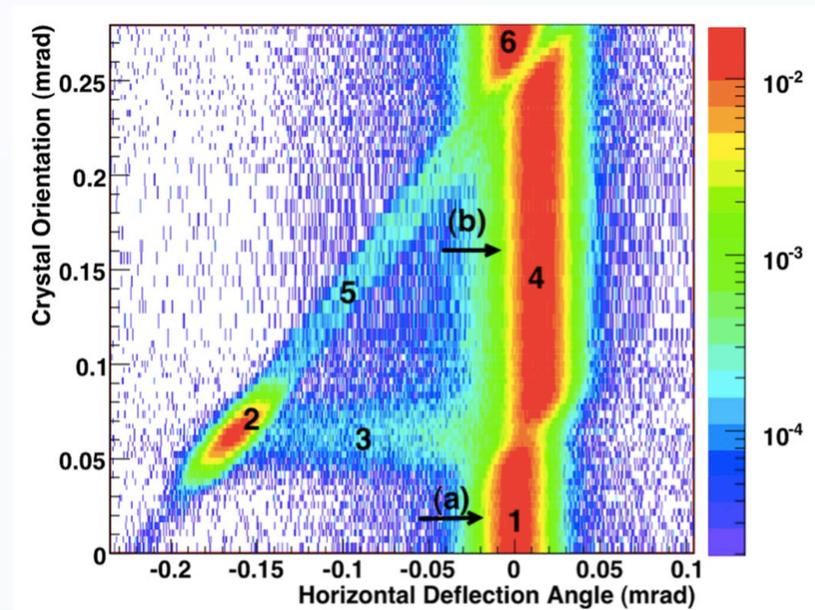


- 1. Channeled
- 2. Not channeled

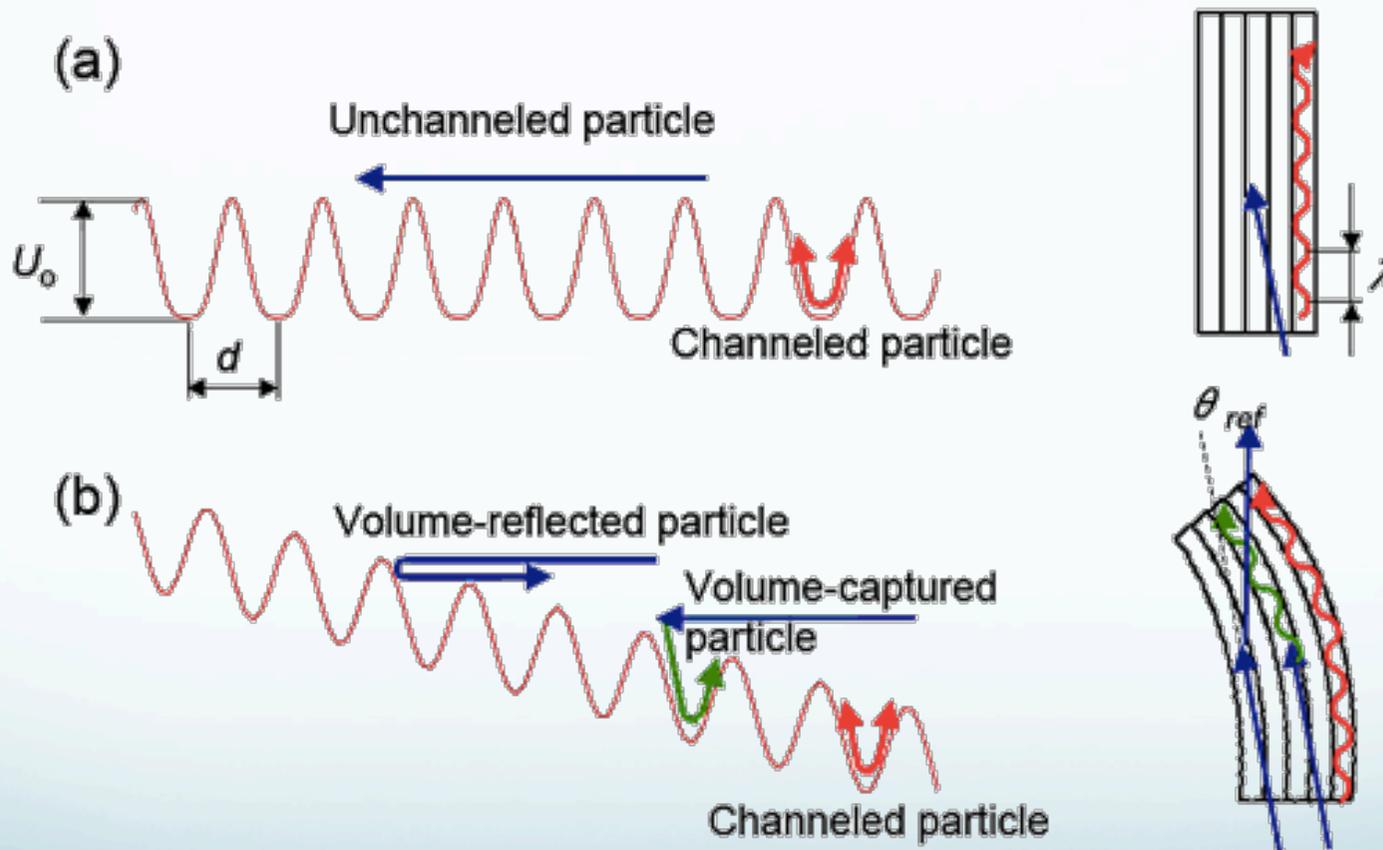
# Bent crystal

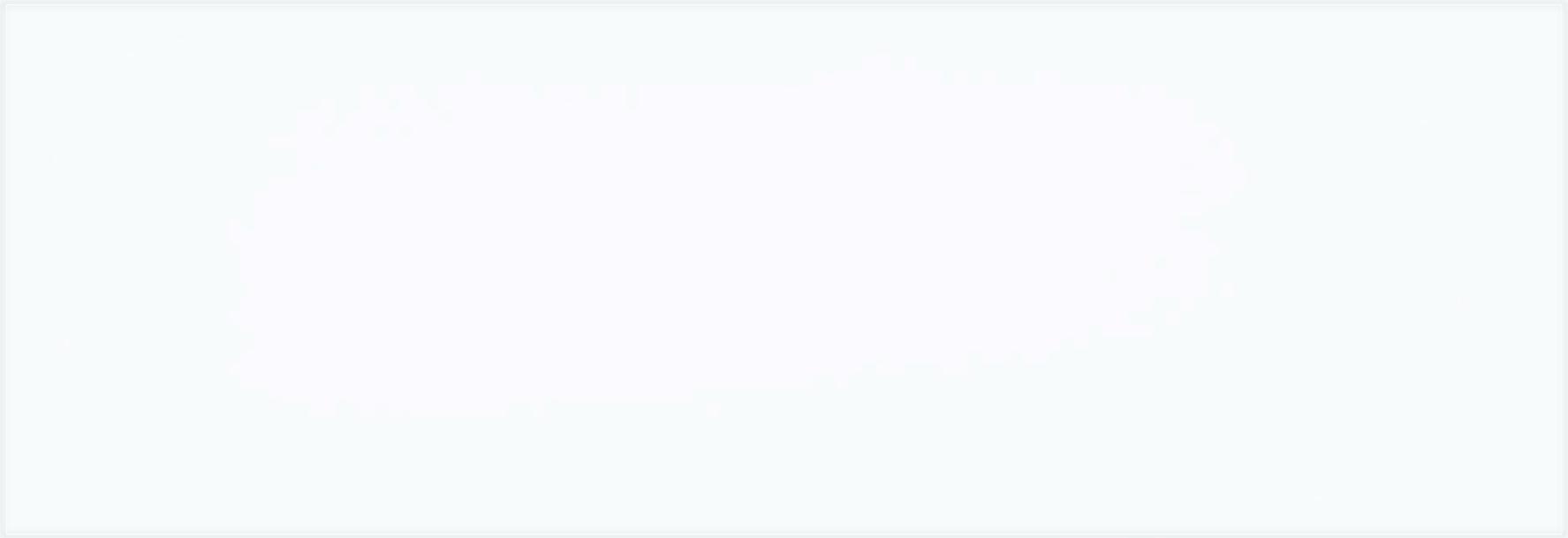
Varying the crystal orientation with respect to the beam direction orientational effects are observed:

1. No effect
2. Channeling
3. Dechanneling
4. Volume reflection
5. Volume capture
6. No effect



# High-energy coherent phenomena in crystals

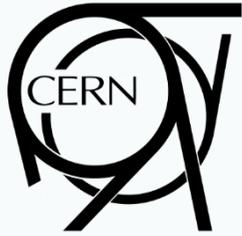




# Experiments

H8 – protons 400 GeV/c

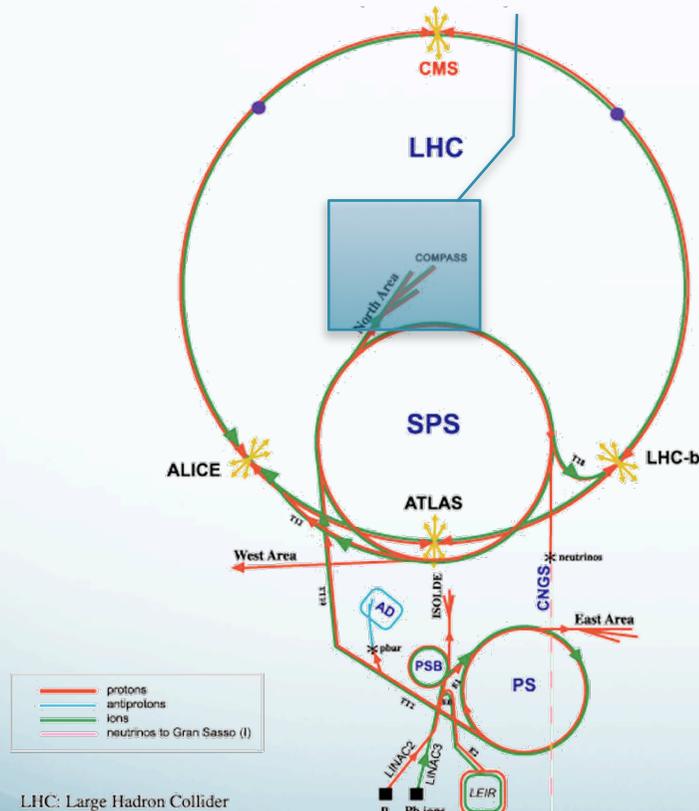
H4 –  $\pi^-$  150 GeV/c



# Experiments



## CERN SPS H8/H4 lines



## Experiments

- H4 Data-Taking:
  - 150 GeV/c  $\pi^-$
  - from 27 June to 07 July
- H8 Data-Taking:
  - 400 GeV/c protons
  - From 09 July to 18 July
- Setup
  - Si-detector tracking system
    - 1  $\mu$ rad angular resolution
  - High-resolution goniometer
    - 2  $\mu$ rad resolution



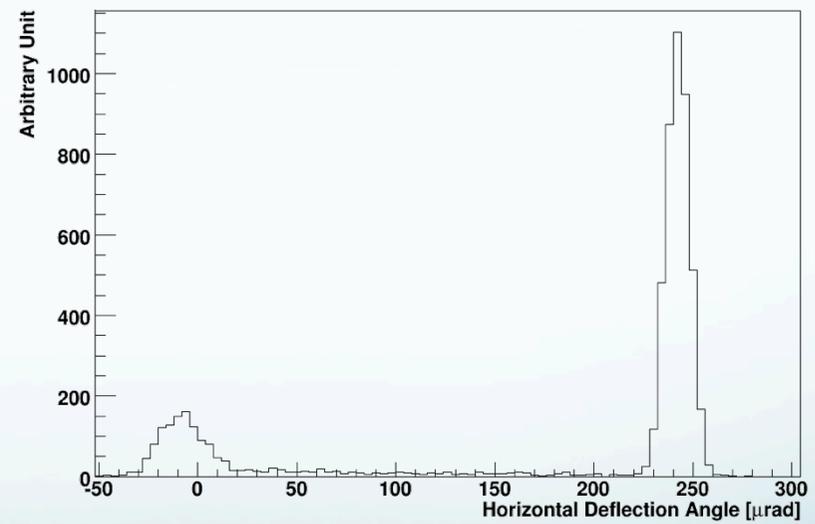
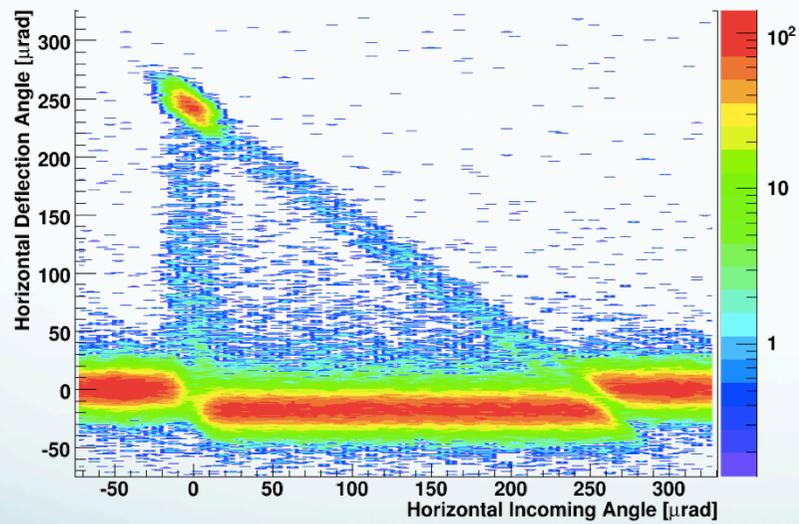
H8 – protons 400 GeV/c



# Ge bent strip

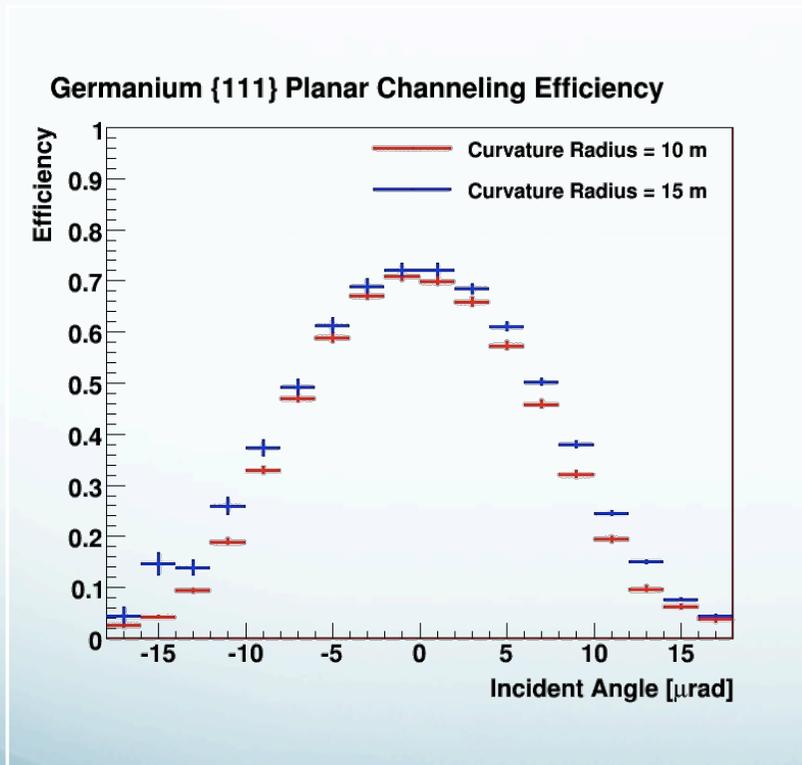
Channeling efficiency

Deflection distribution

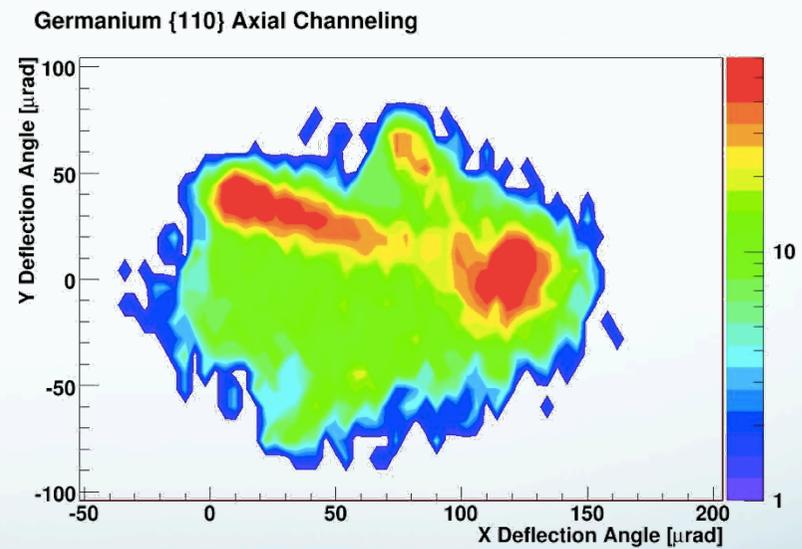


# Ge bent strip

Efficiency

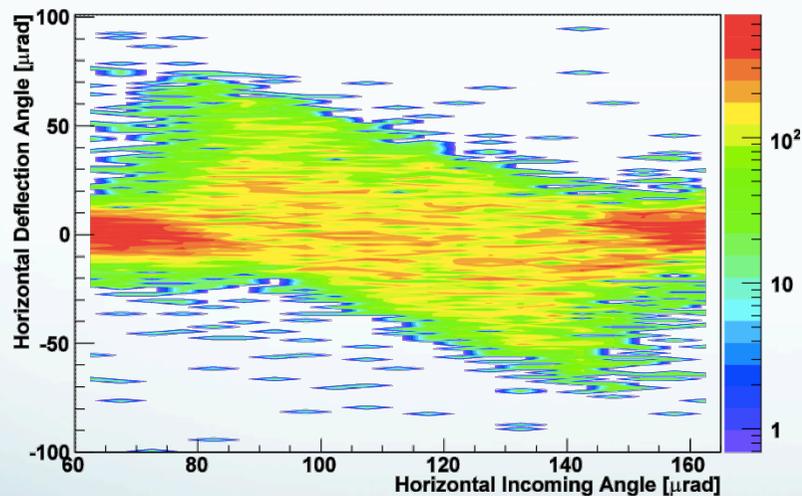


Axial channeling



# Si crystalline undulator

Goniometer scan



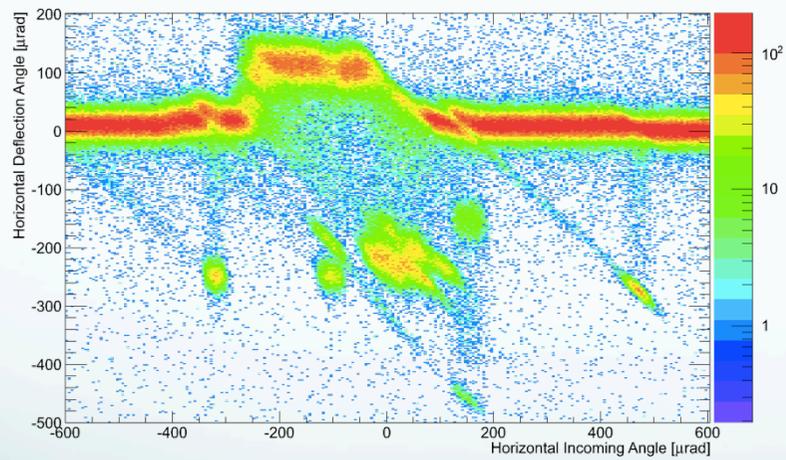
Undulator

- Fabricated in the Sensor and Semiconductor Lab (UniFE)
- Mechanically bent through grooves.
- Experimental evidence of double-sided bending.

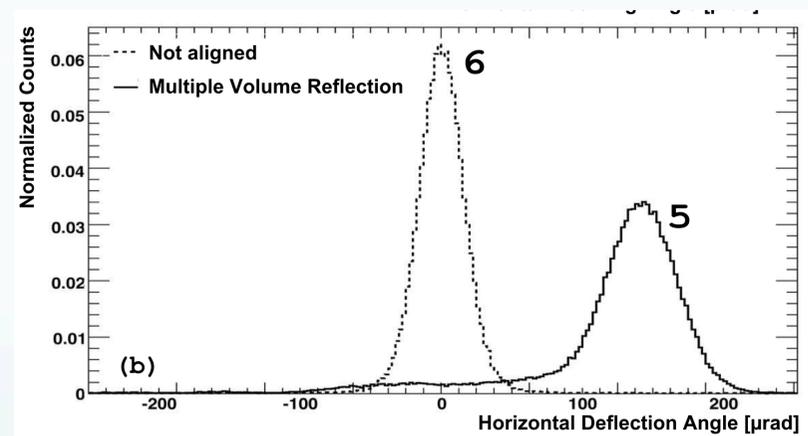
under analysis

# Multi-crystals

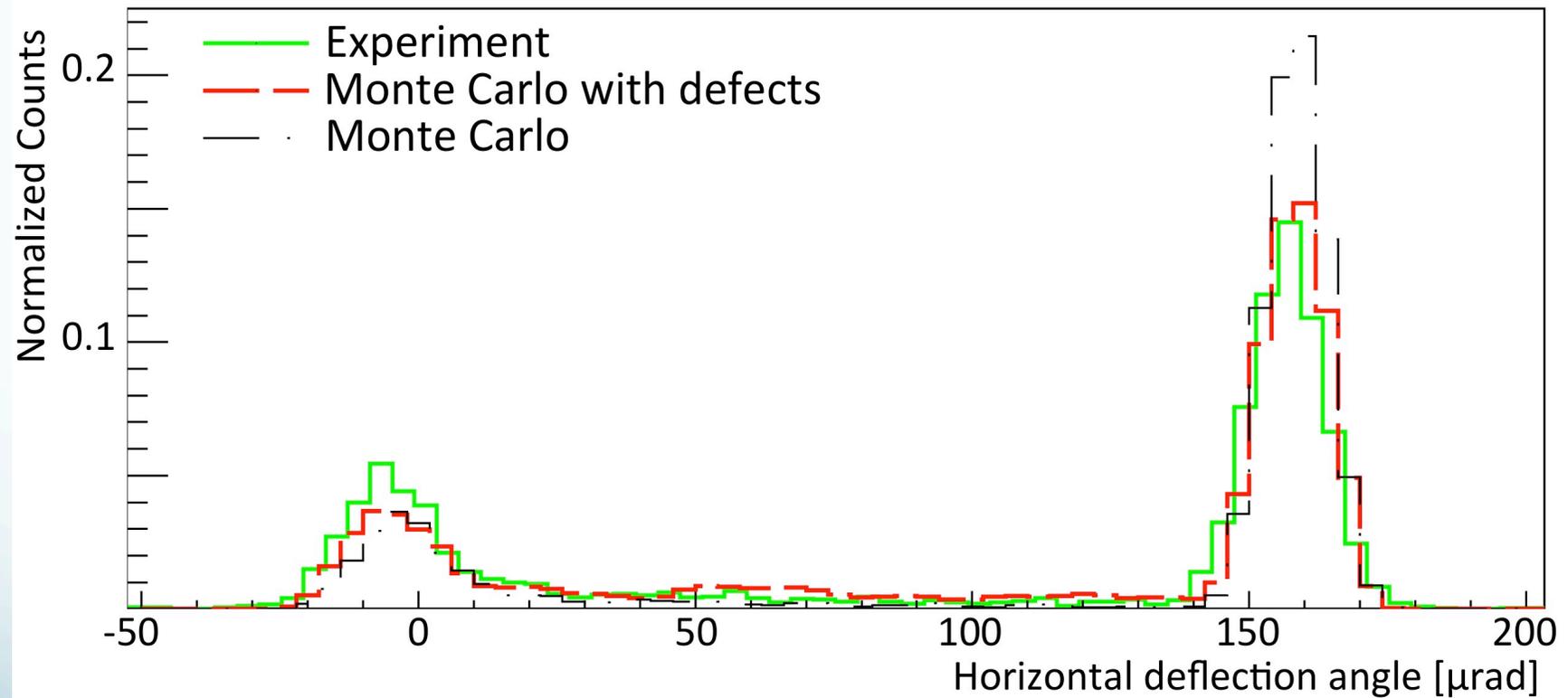
Goniometer scan



Profile MVR



# SiGe self-bent crystal



- SiGe self bent crystal
- (1 1 1) plane
- 25.6 m curvature radius
- 400 GeV/c proton
- defects

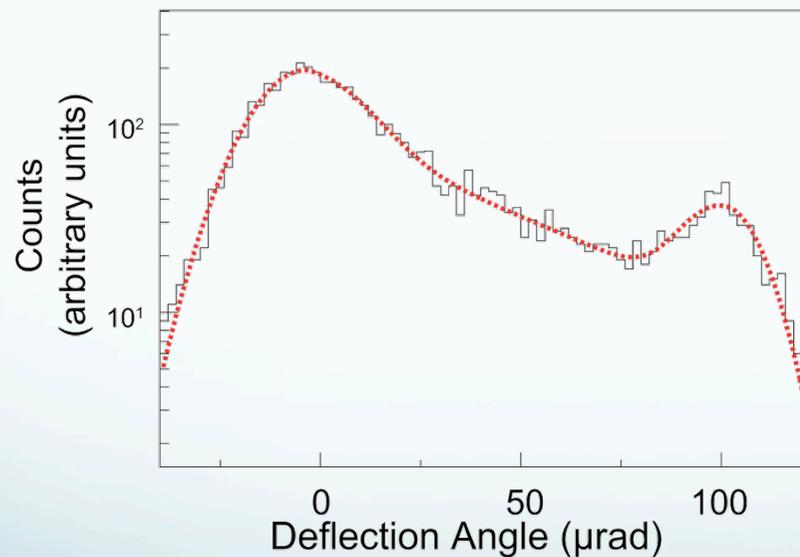


H4 –  $\pi^-$  150 GeV/c



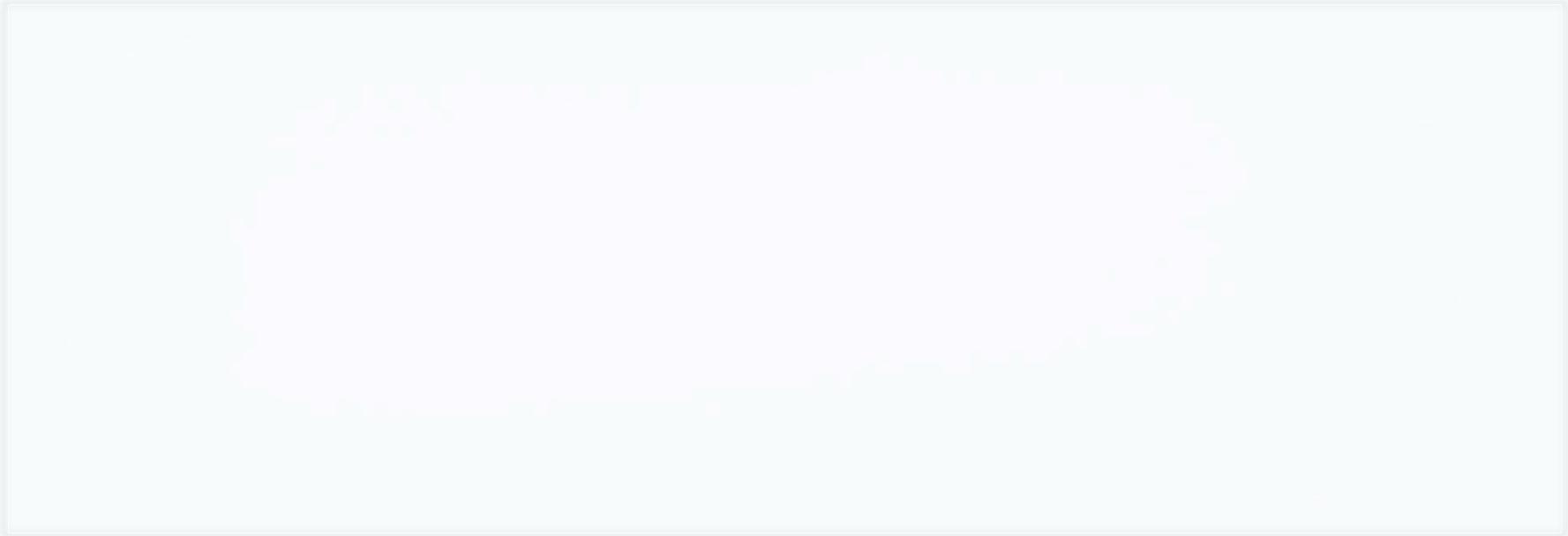
# Dechanneling length

## Deflection distribution



## Dechanneling length

- First direct experimental measurement.
- Linear correlation between deflection angle and dechanneling point.
- Definition of simple equation to evaluate deflection efficiency.



# Monte Carlo

DYNECHARM++  
DYNECHARM++\_Phi  
Geant4 Channeling

# DYNECHARM++



VNIVERSITA  
DEGLI-STVDI  
DI-FERRARA



# Goals

- Physic goal:
  - Simulation of the orientational interactions between particles and crystals;
  - Correct reproduction of existing experimental data
  - Prediction of new experiments and phenomena.
- Programming goal:
  - Fast;
  - Expandable;
  - Easily updatable;
  - Linkable.

# Method

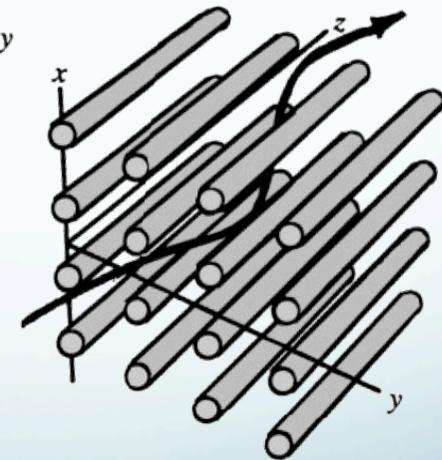
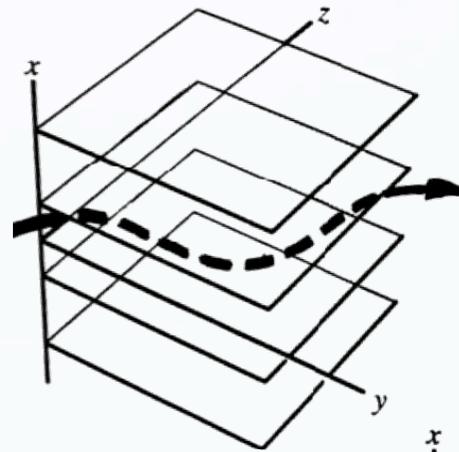
- Two Monte Carlo methods:
  - Simulation: integration of the equation of motion for every particle;
  - Emulation: usage of cross section to describe orientational phenomena.

# Method

- C++ language
  - Widespread programming language in high-energy physic community (ROOT, Geant4, etc...);
  - Object oriented programming language;
  - Compile on almost all systems;
  - Exploit parallelization at all level.

# Continuum potential approximation

- Particle impinge on a crystal close to atomic planes or axes.
- Particle “sees” aligned atoms as a unique axis.
- Aligned axes form planes.
- Particle interaction with atoms can be approximated through interaction with atomic planes or axes [1].



# Continuum potential calculation

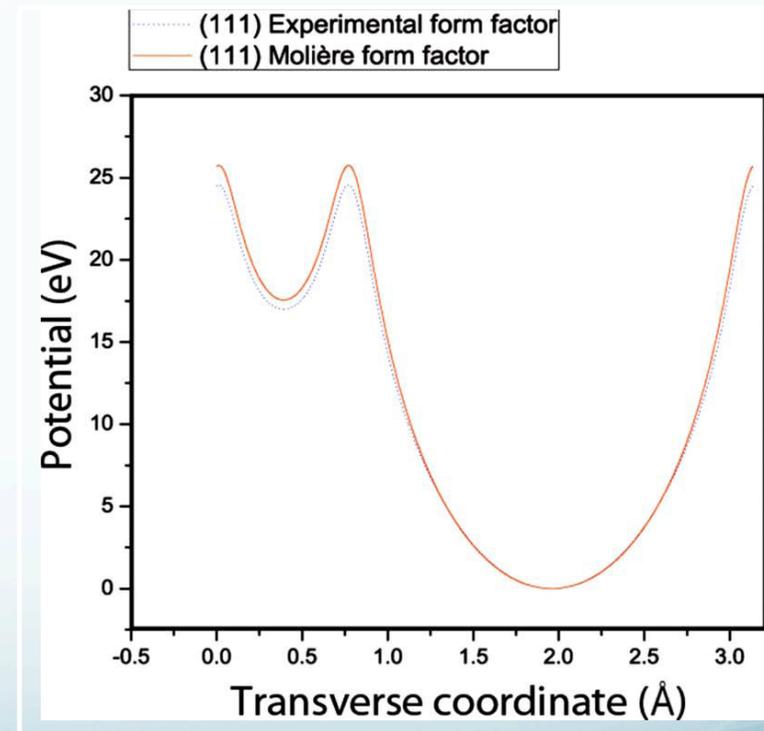
## ECHARM

- Calculation method based on the expansion of the electrical characteristics of crystals in Fourier series.

$$\varphi(\mathbf{r}) = \frac{4\pi e}{\Delta} \sum_{g \neq 0} \sum_{l=1}^N Z_l S(Z_l, \mathbf{g}) \frac{[1 - F(Z_l, g)]}{g^2} e^{-i\mathbf{g} \cdot \mathbf{r}}$$

- Electrical characteristics are averaged over planar and atomic.
- Different approximation for atomic form factor.
- Approximation for any planes or axes for cubic structure.

## Si (111) Planar Potential



# Emulation method

- Analytical approximations [1,2] and experimental data [3,4] to calculate the cross section of the phenomena.
- Less computational time than integration of the equation of motion.
- Theoretical knowledge of orientational planar phenomena has been largely verified through results to be treated via a macroscopic approach.
- It can be used to simulate known crystal effects, but can not be used to predict strange or new phenomena

[1] V.M. Biryukov, Y.A. Chesnokov and V.I. Kotov, *Crystal channeling and its application at high-energy accelerators*, Springer-Verlag, Berlin Germany (1997).

[2] V.A. Maishev, *Phys. Rev. ST Accel. Beams* 10 (2007) 084701 [physics/0607009].

[3] Y.M. Ivanov et al., *Phys. Rev. Lett.* 97 (2006) 144801

# Simulation method

- Integration of the equation of particle motion through Velocity-Verlet numerical method [1].
- Electric field experienced by particles in the interaction with the oriented crystal is evaluated through continuum potential approximation [2].
- Transverse energy variation due to interaction with electrons and nuclei is taken into consideration through Kitagawa and Ohtsuki approximation [3] applied to multiple scattering approximation [4].
- Possibility to add crystal defects to the simulation.

[1] L. Verlet, Phys. Rev. 159, 98 (1967); Phys. Rev. 165, 201 (1967)

[2] J. Lindhard, Danske Vid. Selsk. Mat. Fys. Medd. 34, 14 (1965)

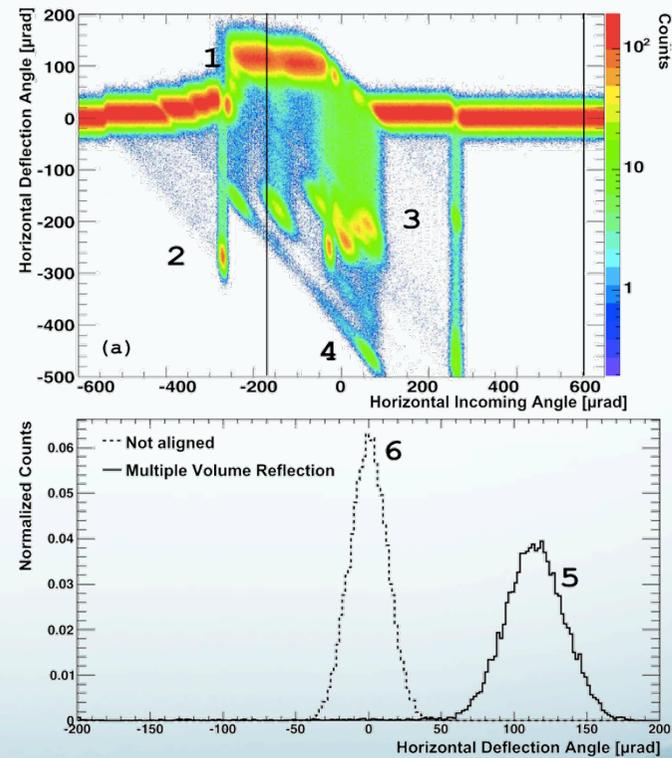
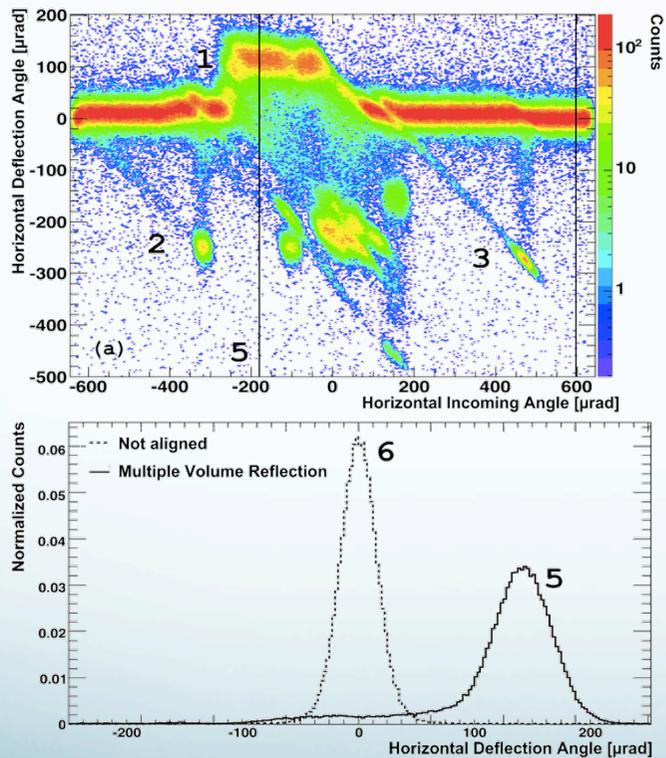
[3] M. Kitagawa and Y. H. Ohtsuki, Phys. Rev. B 8, 3117–3123 (1973)

[4] J. Beringer *et al.* (Particle Data Group), Phys. Rev. D86, 010001 (2012)

# Multi-crystal

COHERENT [1]

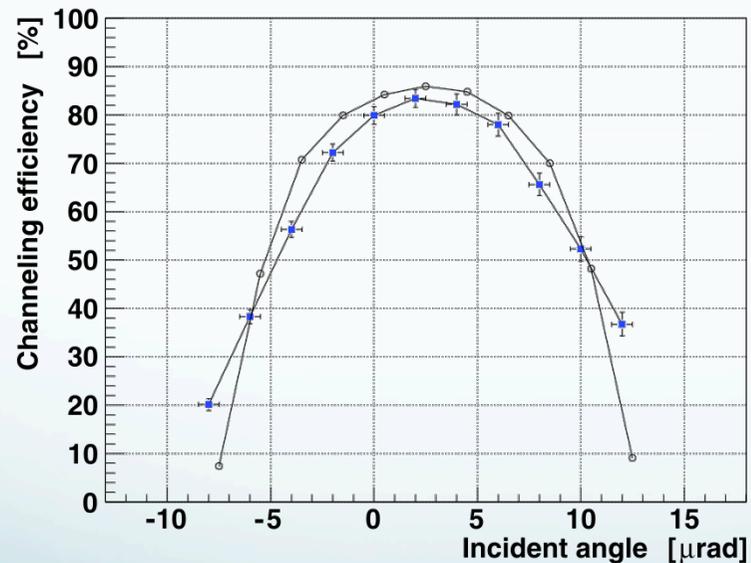
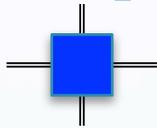
DYNECHARM++



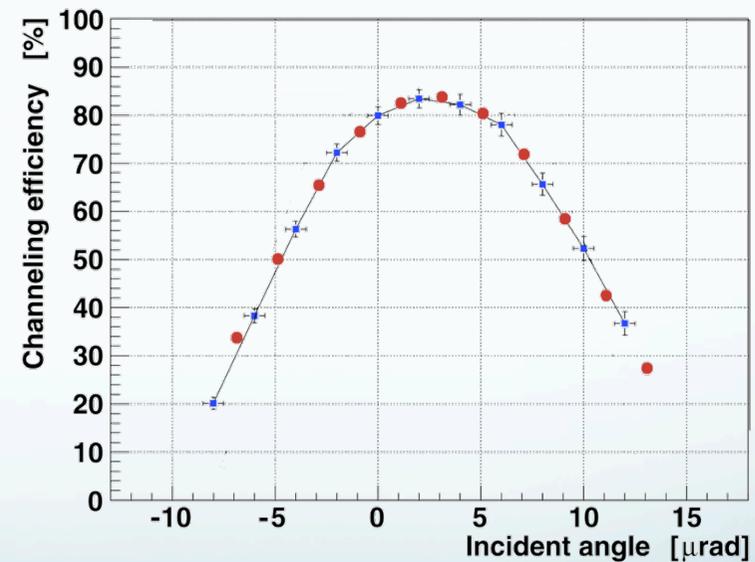
[1] E. Bagli *et al.*, JINST, 7, P04002 (2012)

# Si-efficiency simulation

H8RD22 [1]



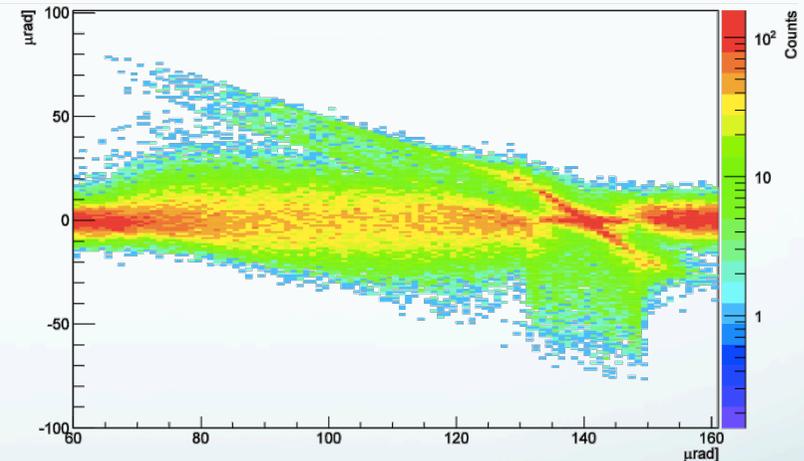
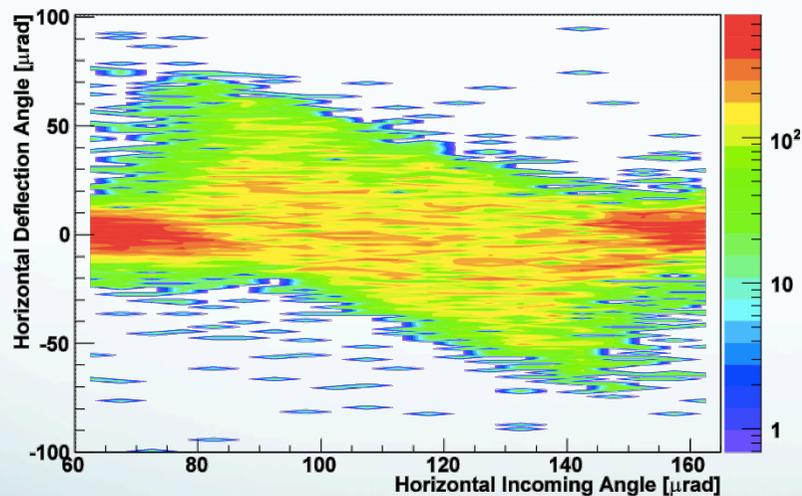
DYNECHARM++



# Si crystalline undulator

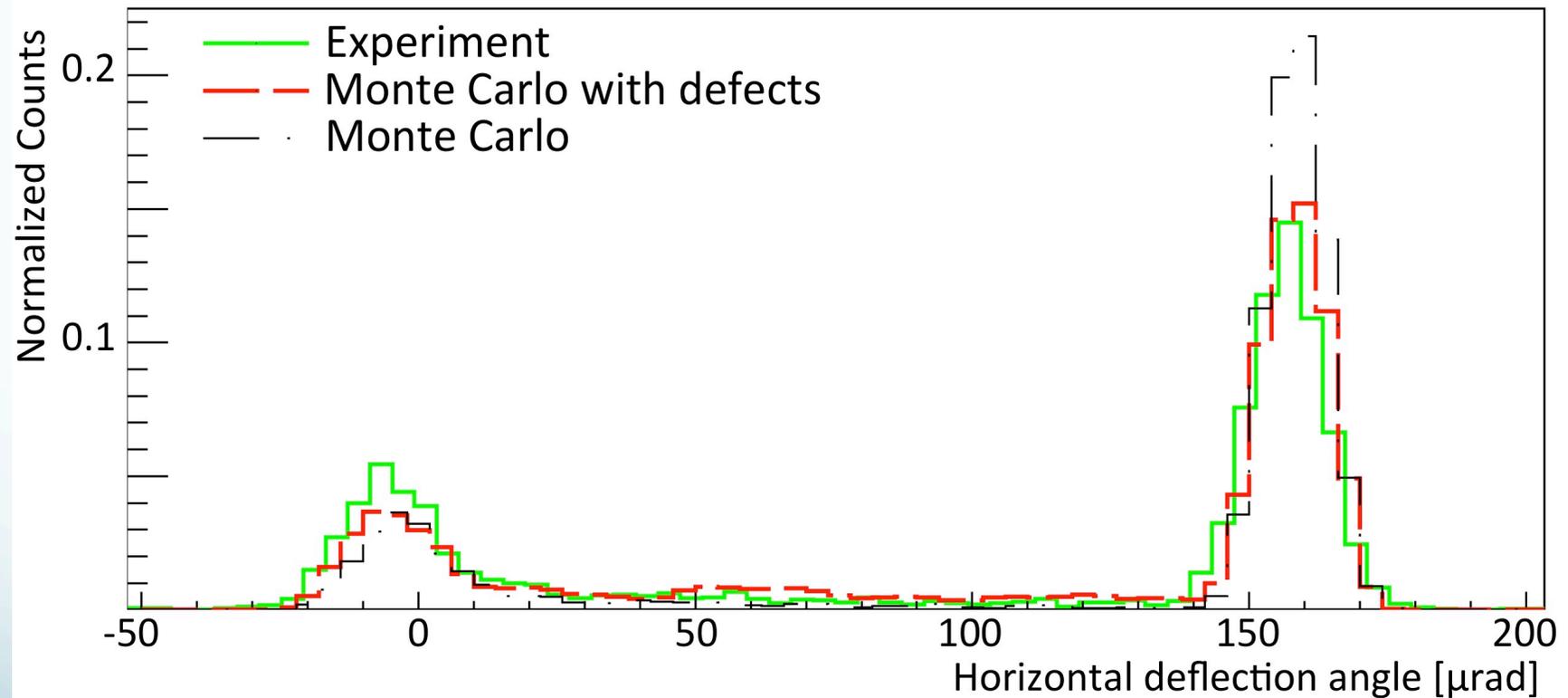
COHERENT [1]

DYNECHARM++



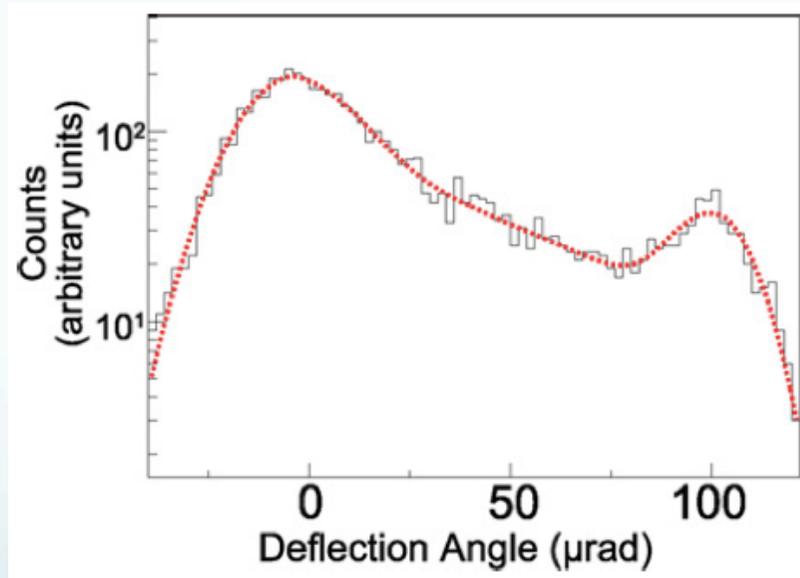
[1] COHERENT experiment, not published

# SiGe self-bent crystal



- SiGe self bent crystal
- (1 1 1) plane
- 25.6 m curvature radius
- 400 GeV/c proton
- defects

# Dechanneling length



Experiment

- $L = (0.93 \pm 0.05) \text{ mm}$
- $\varepsilon_{\text{ch}} = (12.5 \pm 1.0) \%$

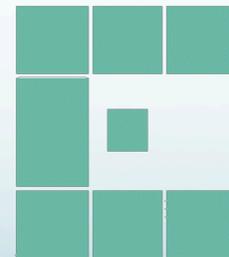
DYNECHARM++

- $L = (0.95 \pm 0.03) \text{ mm}$
- $\varepsilon_{\text{ch}} = (14.3 \pm 0.3) \%$

# DYNECHARM++\_Phi



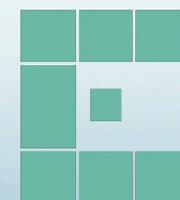
VNIVERSITA  
DEGLI-STVDI  
DI FERRARA



Colfax International

## Xeon Phi™ 5110P

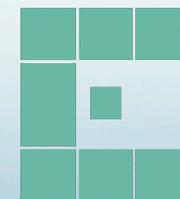
- 60 cores (240 with Hyper-threading)
- 1.053 GHz clock
- 8 GB on-board memory
- AVX-512 register scheme
- PCIe card form factor
- Up to 8 cards in parallel



Colfax International

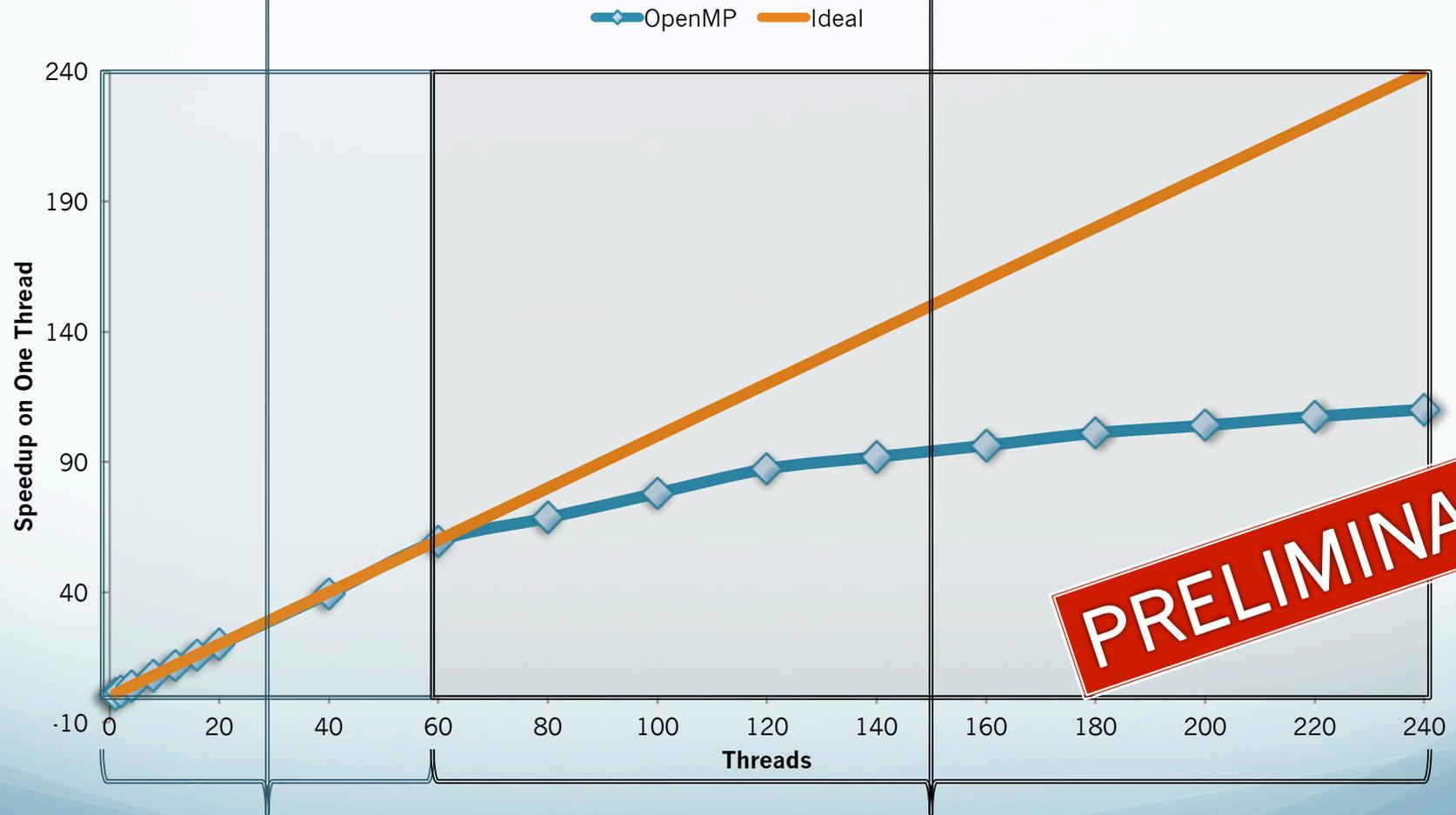
DYNECHARM++ code has been revised to exploit parallelization at two levels:

- Multithreading on 240 and more cores
- Vectorization on 512-bit wide register



Colfax International

# Multithreading

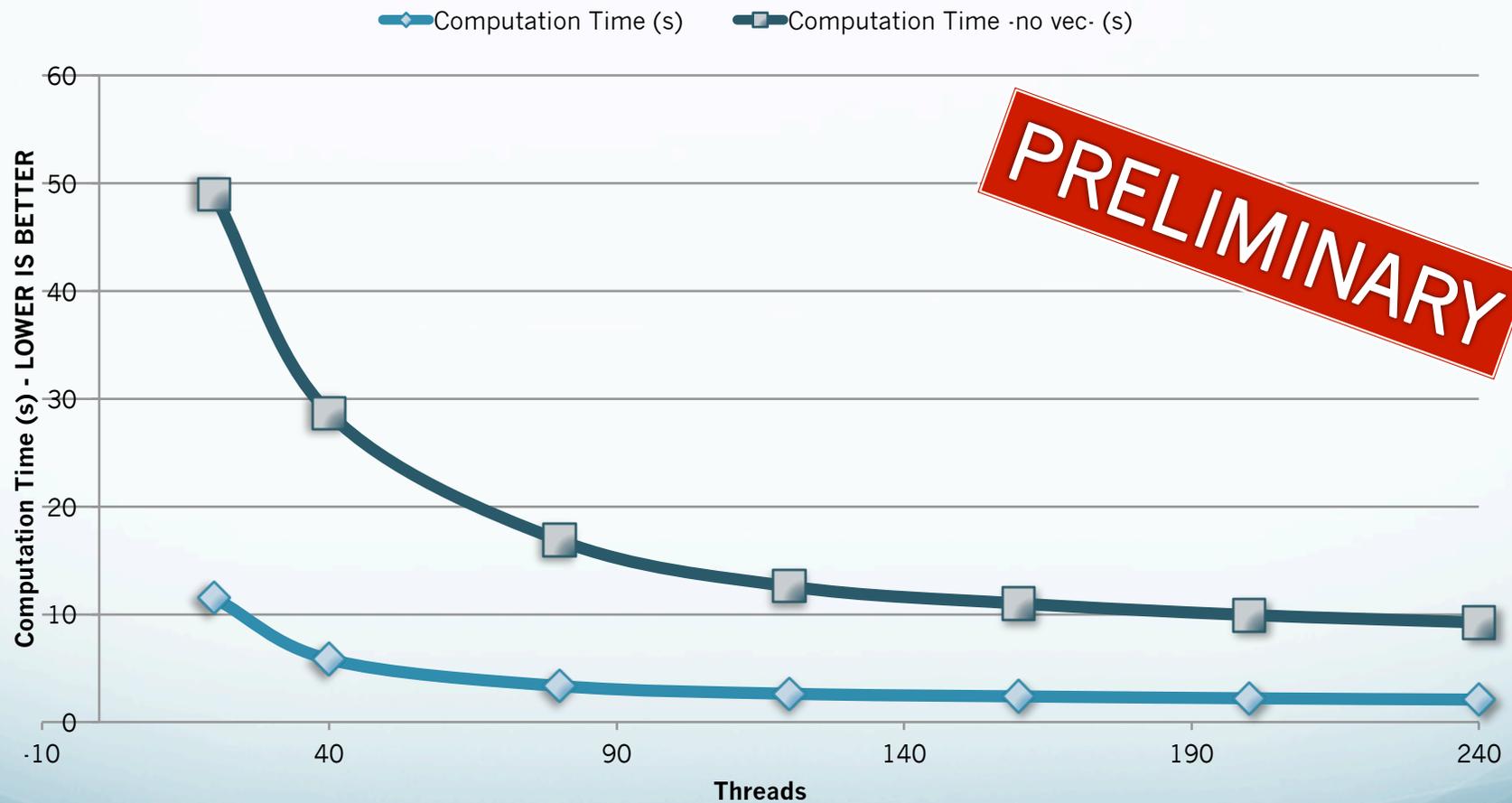


Physical  
cores

Hyper-threading

**PRELIMINARY**

# Vectorization



15360  
Particles

# Xeon vs. Xeon Phi

## Dual Xeon E2670 vs Xeon Phi 5110P



==== Same computation time

# Geant4 Channeling



UNIVERSITÀ  
DEGLI STUDI  
DI FERRARA



Unione europea  
Fondo europeo di sviluppo  
Investiamo nel vostro futuro



ASSESSORATO SCUOLA, FORMAZIONE PROFESSIONALE, UNIVERSITÀ E RICERCA LAVORO

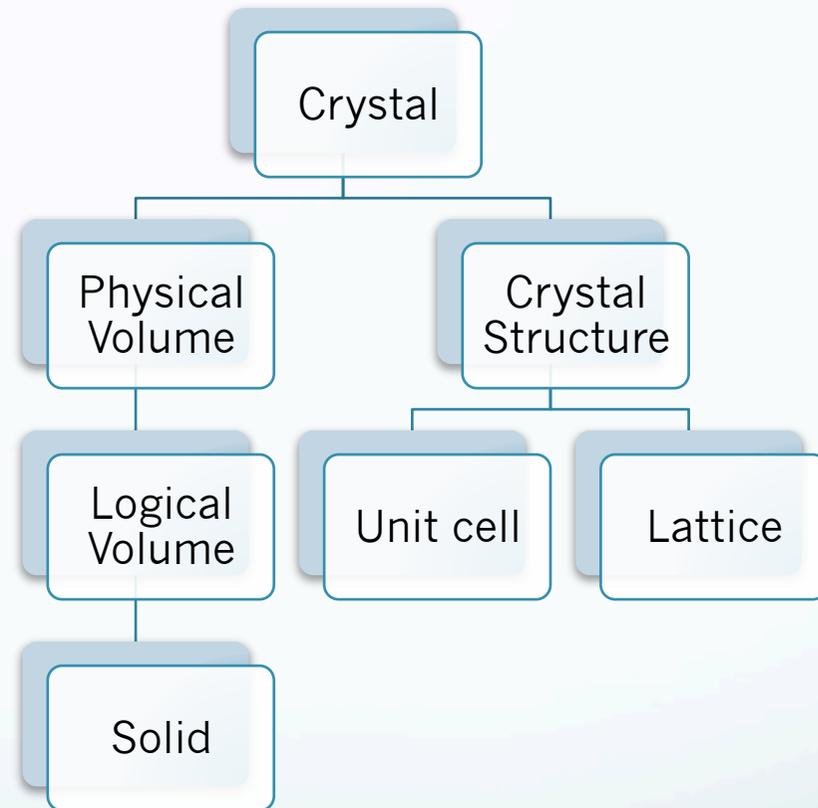


# Motivation

- *“Geant4 is a toolkit for the simulation of the passage of particles through matter. Its areas of application include high energy, nuclear and accelerator physics, as well as studies in medical and space science.”*
- In October 2012 the first Geant4 release with support for crystal structures was released.
- Implementation of channeling into Geant4 can lead to:
  - evaluation of channeling influence on current simulation made with Geant4
  - addition of the Geant4 toolkit advantages to the simulation of current and new experiments based on channeling (e.g. beam collimation and extraction with crystal)

# Crystal

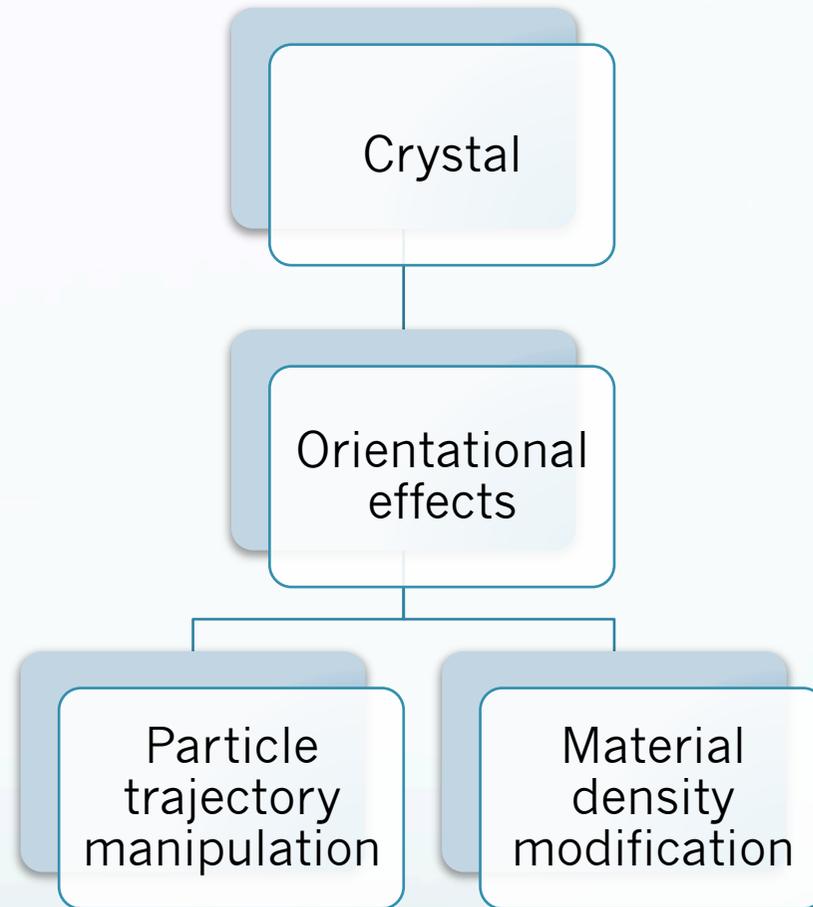
The crystal object is built adding to the standard Physical Volume the Crystal Structure in which the Unit Cell and the Lattice are defined.



# Geant4 processes modification

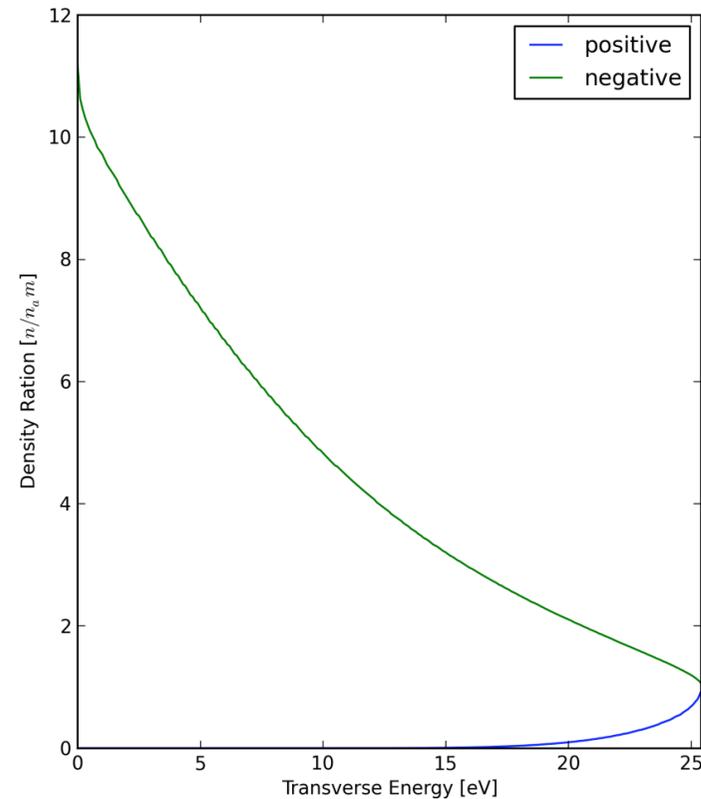
By modifying the trajectory of the particle and the density of the material “seen” by the particle the orientational effects in a crystal affect all the Geant4 physical process

As an example channeled positive particles oscillate between atomic planes interacting less frequently with nuclei and core electrons.



# Modified density

- Nuclei and electron density tables are computed for positive and negative particles as a function of the particle transverse energy.
- This approach can be used for crystal with dimension parallel to the beam much longer than the channeling oscillation period.



# Geant4 processes

## Discrete processes

- The mean free path of the discrete processes is recomputed at each step using the modified density because it is directly proportional to the density ( $\rho$ ) of the material.

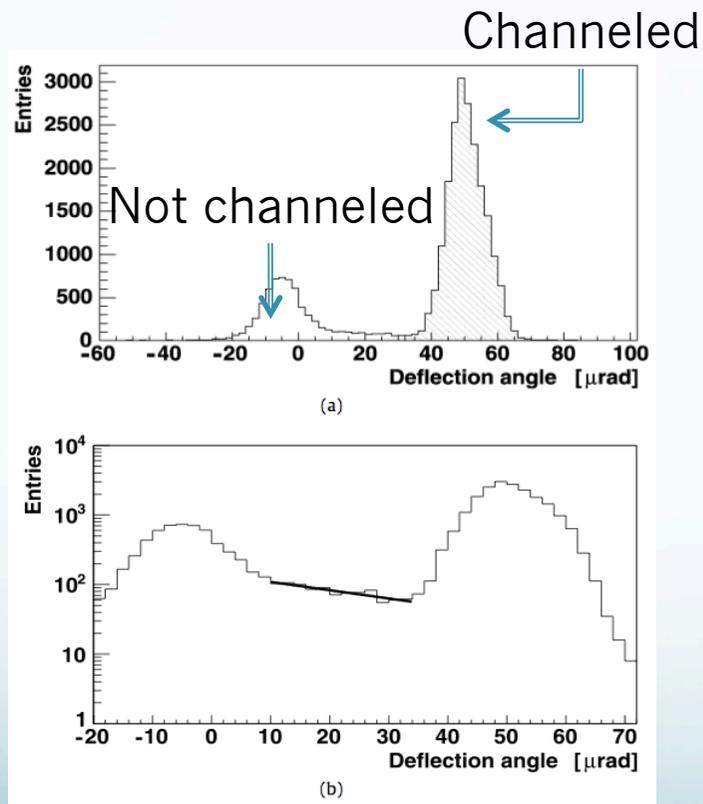
## Continuous processes

- Material density ( $\rho$ ) for the calculation of continuous energy loss ( $dE/dx$ ) is modified at each step ( $dx = \rho dz$ ) to enable the reduction or the enhancement of the energy loss due to channeling.

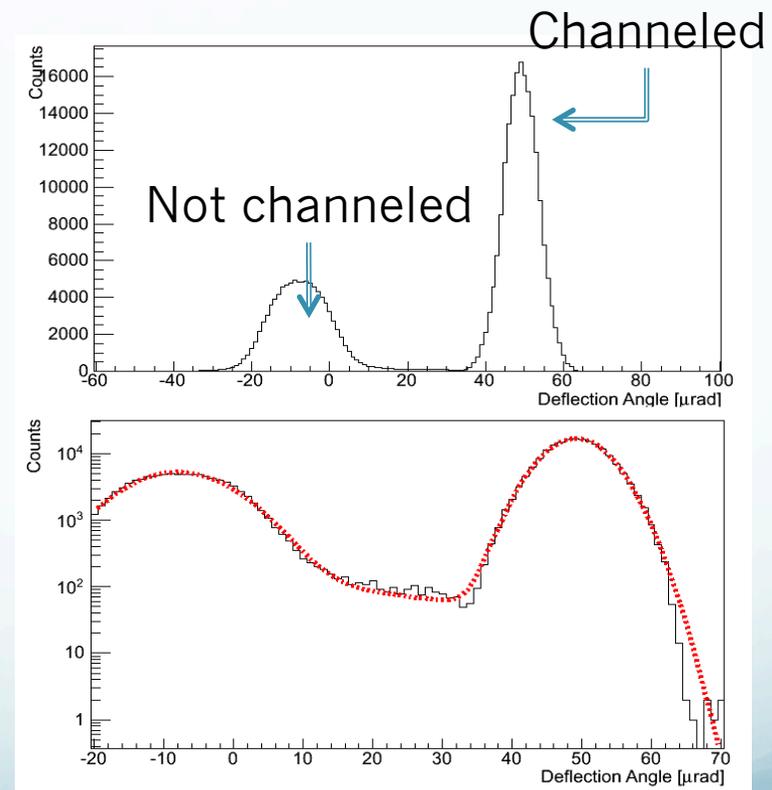
# Nuclear dechanneling length

W. Scandale et al., Phys. Lett. B 680 (2009) 129

## Geant4 Channeling



$$L_n = (1.53 \pm 0.35 \pm 0.20) \text{ mm}$$

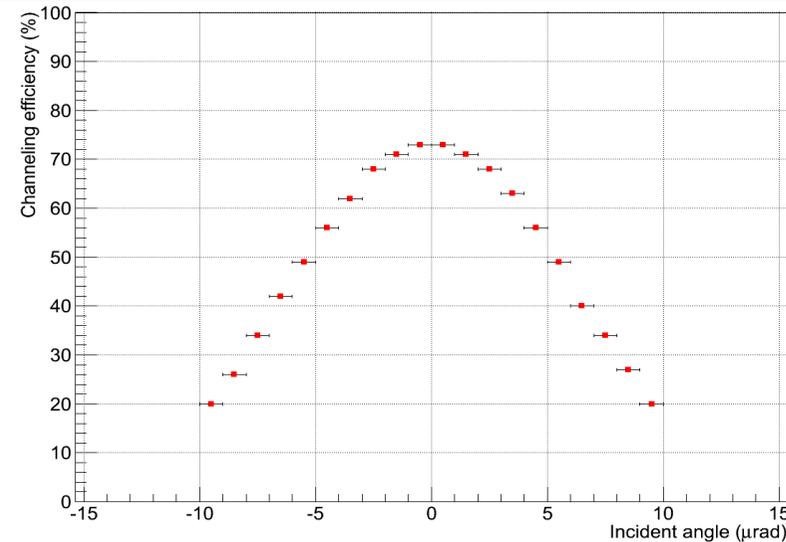
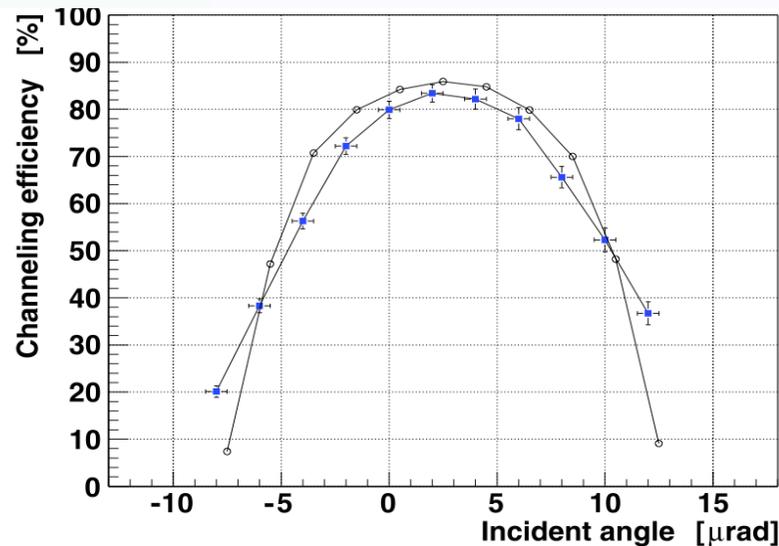


$$L_n = (1.31 \pm 0.05) \text{ mm}$$

# Channeling efficiency vs. incoming angle

W. Scandale et al., Phys. Lett. B 680 (2009) 129

Geant4 Channeling

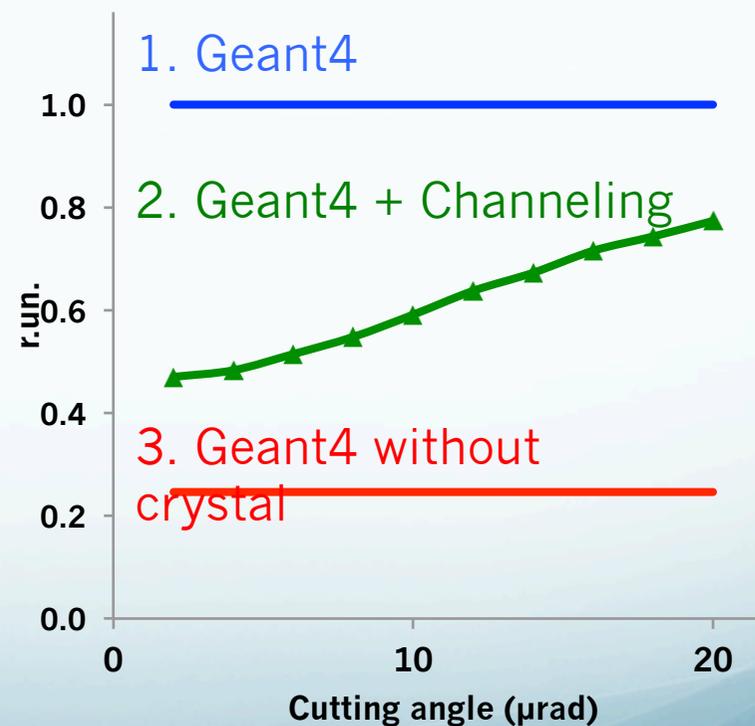
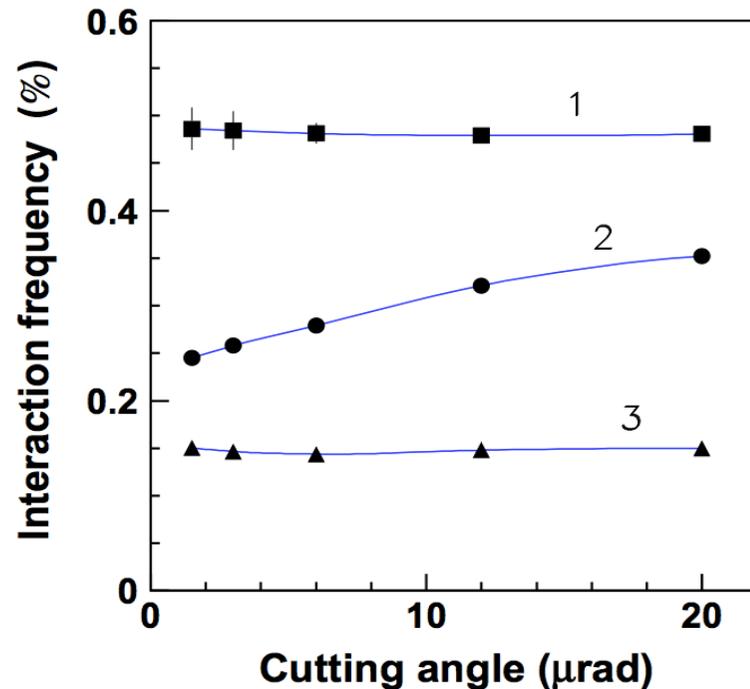


- Experimental measurements
- CERN collaboration simulations
- Geant4 Simulations (b)

# Interaction rates vs. integration angle

W. Scandale et al., NIMB  
268 (2010) 2655

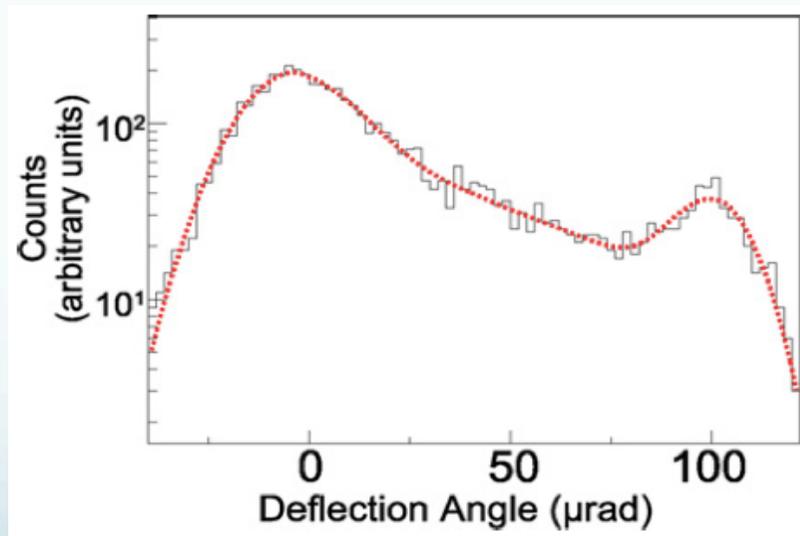
Geant4 Channeling



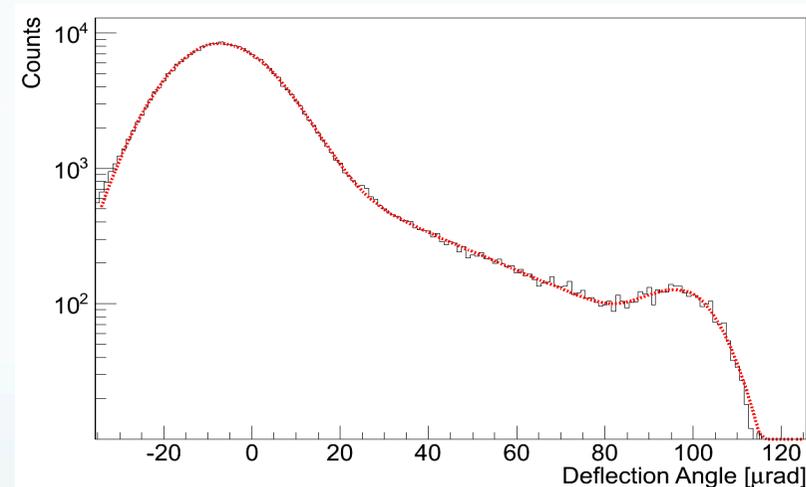
# Dechanneling length for $\pi$

W. Scandale et al., Phys.  
Lett. B 680 (2009) 129

Geant4 Channeling



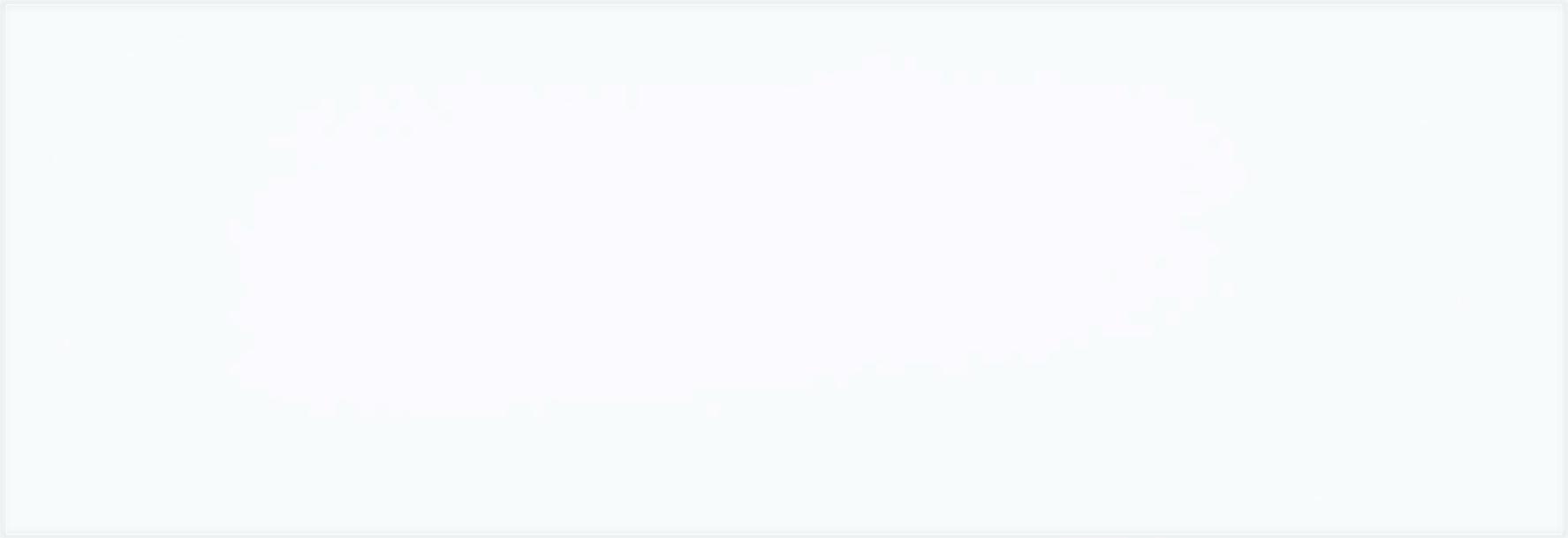
$$L = (0.93 \pm 0.05) \text{ mm}$$
$$\varepsilon_{\text{ch}} = (12.5 \pm 1.0) \%$$
$$\theta_{\text{ch}} = (99.6 \pm 0.2) \mu\text{rad}$$



$$L = (0.60 \pm 0.05) \text{ mm}$$
$$\varepsilon_{\text{ch}} = (4.5 \pm 0.2) \%$$
$$\theta_{\text{ch}} = (95.6 \pm 0.6) \mu\text{rad}$$

# Conclusions

- Experiments of orientational effects for positive and negative particle in bent crystals, multi-crystals, Si and Ge crystals, SiGe self-bent crystals, crystalline undulators.
- Monte Carlo simulation of particle trajectories in crystals (DYNECHARM++)
- Exploitation of modern computational technologies (DYNECHARM++\_Phi)
- Implementation of orientational effect in the most used Monte Carlo code for particle physics (Geant4 Channeling)



Thank you for the attention